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### 5.1 Extant Manuscripts of al-Ṣūfī’s Book

Al-Ṣūfī’s 'Book of the Fixed Stars' dating from around A.D. 964, is one of the most important medieval Arabic treatises on astronomy. This major work contains an extensive star catalogue, which lists star co-ordinates and magnitude estimates, as well as detailed star charts. Other topics include descriptions of nebulae and Arabic folk astronomy. As I mentioned before, al-Ṣūfî's work was first translated into Persian by al-Tūsī. It was also translated into Spanish in the $13^{\text {th }}$ century during the reign of King Alfonso X.

The introductory chapter of al-Ṣūfî's work was first translated into French by J.J.A. Caussin de Parceval in 1831. However in 1874 it was entirely translated into French again by Hans Karl Frederik Schjellerup, whose work became the main reference used by most modern astronomical historians. In 1956 al-Ṣūfís Book of the fixed stars was printed in its original Arabic language in Hyderabad (India) by Dārat al-Ma'aref al-‘Uthmānīa. It was later republished in Beirut (Lebanon) from the Hyderabad copy by Dār al-Āfāq al-Jadīdah in 1981. At present no English translation of this important treatise exists. In order to remedy this omission, I have made this detailed study of al-Șūfi's work, including the preparation of an English translation. However, before I started I had to identify the extant manuscripts of the 'Book of the Fixed Stars'. Then I had to identify the criteria with which to choose the manuscripts which were used as the bases for the translation and discussions.

### 5.1.1 List of Extant Manuscripts of al-Ṣūfǐ’s Book

It is a measure of the popularity of this book that many manuscripts are still preserved in libraries throughout the world Figure 17 . However, tracking down several of these manuscripts involved extensive travel worldwide and much library research. The reaction of some librarians or museums has not always been positive or helpful; however, in the end I managed to locate as many as 35 manuscripts and acquired copies of the major ones which are needed for this study. The list below shows the manuscripts of al-Ṣūfí's work which I found from the various references and library catalogs, some of which I managed to study personally. They are grouped by country or location of the library where they are being kept. However, other manuscripts might still be held in other libraries or in private collections. Some manuscripts have also been recently digitized for public viewing or research. Therefore I have included the website locations where these manuscripts can be located.


Figure 17 location of manuscripts

1. Oxford, Bodleian Library, MS Marsh 144, dated A.H. 400 / A.D. 1009.

Size: 265 x 180 mm ; 419 pages; Layout: written in 15 lines.
2. Oxford, Bodleian Library, MS Pocock 257, dated A.H. 706 / A.D. 1306.
3. Oxford, Bodleian Library, MS Huntingdon 212, dated A.H. 769 / A.D. 1367.
4. Istanbul. Topkapi Sarayi, MSS 3493, dated A.H. 525 / A.D. 1131
5. Istanbul. Topkapi Sarayi, MSS 2595, date unknown.
6. Istanbul. Topkapi Sarayi, MSS 2642, date unknown.
7. Istanbul. Sulaymania Library, Ms number unknown, dated A.H. 529 / A.D. 1135.

A facsimile copy of this manuscript is found in Beirut (American University of Beirut) (MS 520:S94sa) which is taken from a copy from another facsimile copy found at the University of Damascus in Syria.
8. Berlin, Ahlwardt 5658-5660, dated A.H. 620 / A.D. 1233.
9. Vatican, Rossi 1033, dated A.H. 621 / A.D. 1224.
10. Paris Bibliotheque Nationale de France, MS Arabe 5036, dated A.H. 833 / A.D. 1430. http://gallica.bnf.fr/ark:/12148/btv1b60006156
11. Paris Bibliotheque Nationale de France, MS Arabe 2488, date unknown.
12. Paris Bibliotheque Nationale de France, MS Arabe 2489, date unknown.
13. Paris Bibliotheque Nationale de France, MS Arabe 2490, date unknown.
14. Copenhagen, Royal Library, MS 83, dated A.H. 1010 / A.D. 1601.

This manuscript was the one used by Schjellerup in his French translation in 1874.
15. St Petersburg, Bibliotheque Imperiale de St Petersburg, MS 191 dated A.H. 1015 / A.D. 1606. This manuscript was the second one used by Schjellerup in his French translation in 1874.
16. St Petersburg, Institute des Langues Oriental, MS 185, dated A.H. 405 / A.D. 1015.

Note: the date of this manuscript is doubtful because according to Schjellerup this manuscript was written in $T a$ 'līq style which was not used as early as the $11^{\text {th }}$ century; therefore this manuscript could date to the $15^{\text {th }}$ or $16^{\text {th }}$ century A.D. (Kunitzsch, 1986).
17. St Petersburg, Bibliotheque Imperiale de St Petersburg, MS 190 dated $15^{\text {th }}$ or $16^{\text {th }}$ century A.D.
18. Beirut, American University of Beirut, MS 520:S94 sA, dated A.H. 1122 / A.D. 1711. Size: 215 x 160 mm ; 110 pages; Layout: written in 27 lines; Naskhī style.
19. New York, The Metropolitan Museum of Art, no 13.160 .10 , dated $14^{\text {th }}$ century A.D.
20. New York, The Metropolitan Museum of Art, no 1975.192.2, dated $18^{\text {th }}$ century A.D.
21. London, British Library, OR 5323, dated $14^{\text {th }}$ century A.D.
22. London, British Library, ADD 7488 , dated $17^{\text {th }}$ century A.D.
23. London, British Library, OR 1407 dated A.H. 1074 / A.D. 1663.
24. London, British Library, IO ISL 621, dated $17^{\text {th }}$ century A.D.
25. London, British Library, IO ISL 2389, dated $18^{\text {th }}$ century A.D.
26. Madrid, library Escurial, MS No 915, dated A.H. 1173 / A.D. 1760.
27. Bologna, les Manuscript Orientaux Collection Marsigli, MS 422, date unknown.
28. Tehran, Majles library, MS 197, date unknown.
29. Tehran, Majles library, MS 196, date unknown.
30. Tunis, Bibliotheque Nationale de Tunisie, MS 8093, dated A.H. 1030 / A.D. 1621.

Size: 225 x 140 mm ; 190 pages; Layout: written in 17 lines.
31. Hyderabad, Asafiya library, Ms number unknown, date unknown.
32. Washington, Library of congress, Ms Number unknown, dated A.H. 1142/A.D. 1730.

Size: $250 \times 150 \mathrm{~mm}$; 176 pages; Layout: written in 19 lines. This copy is based on Ulugh Beg's copy made in A.D. 1430 which is found at The Bibliothèque Nationale de France in Paris (MS5036). http://www.wdl.org/en/item/2484
33. Cairo, the Egyptian Dar books, Ms Number unknown, dated A.H. 1043 / A.D. 1633.
34. Princeton, Princeton University Library, Garrett no. 2259Y, dated A.H. 1015 / A.D. 1607. http://diglib.princeton.edu/view?_xq=pageturner\&_index=1\&_inset=1\&_start=1\&_doc=/met s/islamic 2259 y.mets.xml
35. Doha, The Museum of Islamic Art in Doha, Ms \# M1-02-98-90, dated A.H. 519 / A.D. 1125; this manuscript was acquired by the Museum of Islamic Art in Doha in 1998 from the Sotheby's London auction house.

There are also other manuscripts which fall under the title of 'Sufi Latinus' corpus. There are 8 extant copies of these Latin manuscripts which were based on al-Ṣūfís 'Book of
the Fixed Stars'. According to Kunitzsch $(1965 ; 1986)$ the longitude values and the style of drawing are no doubt derived from the Arabic al-Ṣūfì manuscripts. In the title of one of those manuscripts which is located at the Bibliotheque Nationale de France in Paris we find the name of the author as 'Ebennesophy'. This is one of the first examples whereby al-Ṣūfī was referred to as Ibn al-Ṣūfì. I have not included any of these manuscripts in the above list since I do not believe that the 'Sufi Latinus' corpus represent a genuine or an accurate picture on alṢūfi's work which we can rely on. These manuscripts are:

- Paris, Arsenal 1036.
- Gotha, Forschungsbibliothek, MS M II 141, dated A.D. 1428.
- Prag, Strahov Library, MS D.A. II, 13.
- Berlin, Kupferstichkabinett, MS Hamilton 556.
- Munich, Clm 826.
- Catania, MS Catin 85.
- Vienna, MS 5318.
- Kues, Cusanus-Stift, MS 207.

Finally, I would just like to make a note here on the main sources which modern scholars and historians have been using in their studies of al-Ṣūfís work and other similar topics. The first is the French translation by Schjellerup which was published in 1874. This translation was produced based on the Copenhagen Manuscript MS83 dated A.D. 1601. However, since Schjellerup used a rather late manuscript in his translation I believe that his work might lack the reliability needed to reflect the potential of al-Ṣūfìs work. The other source is the Hyderabad publication of al-Ṣūfî's 'Book of the Fixed Stars' which was printed in Arabic in 1956. This production was edited by Muḥammad Nizām al-Dīn based on five manuscripts. The first was the Istanbul MSS 3493, the second was the Vatican Rossi 1033, the third was the Berlin 5658-5660, the fourth was the Paris MS Arabe 5036 and the last was the Hyderabad copy, for which there is no manuscript number and date. This Hyderabad copy was later re-published in Beirut by Dār al-Āfāq al-Jadīdah in 1981. Even though this work was based on several manuscripts, the oldest known manuscript - which is the Marsh144 copy - was not utilized. According to Kunitzsch (1986) and the investigation which I made myself, the Hyderabad copy contains many errors which do not make it very reliable. However, it is the only clearly-printed Arabic copy of al-Ṣūfî's work readily available to the public and is found in many libraries worldwide. In a later section of this discussion (Chapter 5.12) I have identified some of the differences in coordinates and magnitude values found between these two sources and the main manuscripts which I used as the bases for this work. This exercise
was made for one constellation only in order to show some of the mistakes present in these sources and to show the importance of producing a reliable text of al-Ṣūfi's work from the oldest and best-kept manuscripts available to us.

### 5.1.2 Criteria for Identifying the Book for Translation

Unfortunately not many manuscripts can be used for this study. I have cited several criteria which I used to choose the most suitable manuscripts as the bases for translation. I will try to give examples of these criteria using several manuscripts which I found at the British Library in London.

- Dating of the Manuscript

The first and the most important criterion for choosing the manuscript was the date of the manuscript. The date in this context is the date at which the manuscript was copied or rewritten. All these manuscripts were written by hand by copyist or scribes from an original which was probably written by al-Șūfì himself. Unfortunately the original copy of al-Șūfi's manuscript is no longer extant. In many of these manuscripts the date of the copy was not mentioned. Therefore, it was sometimes a little difficult to put an exact date on a manuscript copy. However, dating can be approximated based on paleographic techniques and calligraphy types. I have indicated in the list below all those manuscripts for which the date is not known and these cannot be used for this translation exercise. However, other manuscripts carry a definite date which was usually written at the end of the manuscript, such as the example of the British library manuscript number OR1407. On the last page of this manuscript we can clearly see that it is dated A.H. 1074 which is equivalent to A.D. 1663 (Figure 18). The criterion for the date which I selected for choosing the best manuscript is that it should not be older than A.H. 500, which is almost 100 years after al-Ṣūfi's death. The younger the manuscript the more likely the mistakes of the copyist will grow.


- Legibility of Handwriting

In addition to questions of date, the legibility of handwriting was another issue which I considered in identifying a manuscript for study. The handwriting of some of these manuscripts was not very clear. This reflected the style or the interest of the copyist. For example, the copyist of British Library manuscript number OR1407 again was not only very neat, but took a real interest in the substance of what he was copying. This scribe, for instance, compiled an index of the constellations at the beginning of the manuscript which was not originally a part of al-Ṣūfí's work (Figure 19). Unfortunately this manuscript was not among the manuscripts used in this study because it is dated to A.H. 1074 which is more than 600 years after al-Ṣūfî's death.

- Complete Manuscript

Another criterion for choosing a manuscript was whether it was complete. I have found several manuscripts of the 'Book of the Fixed Stars' which were deficient, some with many diagrams, star charts or tables incomplete or even missing. Such an example is manuscript IO ISL 621 in the British Library which dates to the 17 th century (Figure 20). As we can see, the tables in this manuscript were not completed. Even though the images of the constellations and stars were drawn in gold (Figure 21), the stars were not numbered and many stars were missing. Several constellation tables were also not complete with the last two constellations missing.


Figure 20


Figure 21

- Obvious Mistakes

The last of the criteria was the obvious mistakes which I found in some of these manuscripts. In the Manuscript ADD 7488 in the British Library which was dated to the 17 th century we have an example of an obvious mistake, with 'Abd al-‘Azīz rather than 'Abd al-Raḥmān cited as part of al-Ṣūfís name. This particular manuscript is also incomplete. The last constellation listed is Argo Navis. The last eight constellations, from Hydra to Piscis Austrinus, are missing. Therefore, such a manuscript could not be a suitable candidate in our work on alṢūfī's book.

- Table 3: The Manuscripts and Identification Criteria.

| Manuscript | Copy Date of <br> Manuscript | Legibility | Completeness <br> \& Mistakes | Criteria <br> Description |
| :--- | :--- | :--- | :--- | :--- |
| Oxford, MS Marsh 144 | A.H. 400 | Clear hand <br> writing | Incomplete <br> manuscript | Before A.H. 500 <br> however the last <br> chapter is in- <br> complete. |
| Oxford, Ms Pocock <br> 257 | A.H. 706 | Clear hand <br> writing | Complete <br> manuscript | After A.H. 500 |
| Oxford, Ms <br> Huntingdon 212 | A.H. 769 | Clear hand <br> writing | Complete <br> manuscript | After A.H. 500 |
| Istanbul, MSS 3493 | A.H. 525 | Clear hand <br> writing | Complete <br> manuscript | After A.H. 500 |
| Istanbul, MSS 2595 | Unknown | Clear hand <br> writing | Complete <br> manuscript | Unknown date |
| Istanbul, MSS 2642 | Unknown | Clear hand <br> writing | Complete <br> manuscript | Unknown date |
| Istanbul Ms number | A.H. 529 | Clear hand | Complete | After A.H. 500 |


| Unknown |  | writing | manuscript |  |
| :---: | :---: | :---: | :---: | :---: |
| Berlin, 5658-5660, | A.H. 620 | Clear hand writing | Complete manuscript | After A.H. 500 |
| Vatican, Rossi 1033 | A.H. 621 | Clear hand writing | Complete manuscript | After A.H. 500 |
| Paris, MS Arabe 5036, | A.H. 833 | Very clear hand writing | Complete manuscript | After A.H. 500 a very well written copy |
| Paris, MS Arabe 2488 | Unknown | Clear hand writing | Complete manuscript | Unknown date |
| Paris, MS Arabe 2489 | Unknown | Clear hand writing | Complete manuscript | Unknown date |
| Paris, MS Arabe 2490 | Unknown | Clear hand writing | Complete manuscript | Unknown date |
| Copenhagen, MS 83 | A.H. 1010 | Clear hand writing | Complete manuscript | After A.H. 500 |
| St Petersburg, MS 191 | A.H. 1015 | Clear hand writing | Complete manuscript | After A.H. 500 |
| St Petersburg, MS 185 | A.H. 405 Date uncertain | Clear hand writing | Complete manuscript | Date uncertain should be $15^{\text {th }}$ century A.D. |
| St Petersburg, MS 190 | 15th century <br> A.D. | Clear hand writing | Complete manuscript | After A.H. 500 |
| Beirut, MS 520:S94sA | A.H. 1122 | Clear hand writing | Complete manuscript | After A.H. 500 |
| New York, 13.160.10 | 14th century A.D. | Clear hand writing | In-complete manuscript | After A.H. 500 |
| New York, 1975.192.2 | 18th century A.D. | Clear hand writing | Complete manuscript | After A.H. 500 |
| London, ADD 7488 | 17th century A.D. | Clear hand writing | Incomplete manuscript with mistakes | After A.H. 500 |
| London, OR 5323 | 14th century A.D. | Clear hand writing | Complete manuscript | After A.H. 500 |
| London, OR 1407 | A.H. 1074 | Very clear hand writing and tables | Complete manuscript | After A.H. 500 |
| London, IO ISL 621 | 17th century | Clear hand writing | Incomplete manuscript | After A.H. 500 |
| London, IO ISL 2389 | $\begin{aligned} & \text { 18th century } \\ & \text { A.D. } \end{aligned}$ | Clear hand writing | Incomplete manuscript | After A.H. 500 |
| Madrid, MS No 915 | A.H. 1173 | Clear hand writing | Complete manuscript | After A.H. 500 |
| Bologna, MS 422 | Unknown | Clear hand writing | Complete manuscript | Unknown date |
| Tehran, MS 197 | Unknown | Clear hand writing | Complete manuscript | Unknown date |
| Tehran, MS 196 | Unknown | Clear hand writing | Complete manuscript | Unknown date |
| Tunis, MS 8093 | A.H. 1030 | Clear hand writing | Complete manuscript | After A.H. 500 |
| Hyderabad, Ms \# unknown | Unknown | Clear hand writing | Complete manuscript | Unknown date |


| Washington, <br> Ms \# unknown | A.H. 1142 | Clear hand <br> writing | Complete <br> manuscript | After A.H. 500 |
| :--- | :--- | :--- | :--- | :--- |
| Cairo, <br> Ms \# unknown | A.H. 1043 | Clear hand <br> writing | Complete <br> manuscript | After A.H. 500 |
| Princeton, Islamic <br> Manuscripts, Garrett <br> no. 2259Y, dated | A.H. 1015/ <br> A.D. 1607 | Clear hand <br> writing | Incomplete <br> manuscript, no <br> tables, only <br> single <br> illustration per <br> constellations | After A.H. 500 |
| Doha, The Museum of <br> Islamic Art in Doha, <br> dated. Ms \# M1-02-98- <br> 90 | A.H. 519 / <br> A.D. 1125 | Clear hand <br> writing | Complete <br> manuscript | After A.H. 500 |

### 5.1.3 The Main Manuscripts Identified for Translation and Discussion.

The two main manuscripts which I have identified to be the bases of the translation and discussion are manuscript ‘Marsh144 and manuscript 'MS5036'. However, I have also found some slight differences in coordinates and magnitude values between these two manuscripts. In a later section of these discussions I have identified some of these differences, which were probably due to scribal error at the time the manuscripts were copied. As we said earlier, all these manuscripts were written by hand over and over again and were handed down from one generation to another. So there must have been hundreds of these copies circulating at any one time. Unfortunately we do not have the original manuscript which was written by the author himself but we have the next best thing which is the copy by the author's sons. However, I believe that the values in the Marsh144 manuscript are probably more accurate since it is an older manuscript; therefore the values which I indicated in the translation of the main text are based on the Marsh144 figures.

- The Marsh144 Manuscript

The Marsh144 manuscript is the earliest-known manuscript of the 'Book of the Fixed Stars'. It is dated A.H. 400 / A.D. 1009 only 23 years after al-Ṣūfi's death. According to the inscription on the last page of this manuscript (Figure 22) this copy was copied and illustrated by al-Ḥusaīn Ibn ‘Abd al-Raḥmān Ibn ‘Umar Ibn Muḥammad. The Marsh144 manuscript was
actually written by al-Husaīn who was the eldest son of al-Ṣūfi. It is now located at the Bodleian Library in Oxford. In 1959 a study of the Islamic constellation images was made by Emmy Wellesz based on this manuscript. The manuscript is 419 pages of the size 265 by 180 mm written in Nasta'lik style with 15 lines on each page. Black ink was used to draw all the figures as well as the tables and writing. The stars drawn in red and labeled in black, in both images, are part of the constellation. The stars drawn in black and labeled in red are outside the constellation. The stars drawn in black and not labeled are those not mentioned by Ptolemy.

According to the Bodleian Library records it was purchased by 'Narcissus Marsh' at the Jacob Golius's Library in Leiden in 1696 . On page 419 of this manuscript we find the inscription of the previous owner by the name of 'Christianus Ravius' who purchased this copy in 1644 . However from page 405 onward the manuscript shows more or less drastic repairs with the last page of this manuscript showing an incomplete table. According to the Latin inscription found at the margin on the last page 'Christianus Ravius' wrote that he supplied the missing parts of the text after having compared it with a more recent copy of the same work. These missing pages were probably the first eleven folios of this manuscript. This can be seen from the difference in handwriting between these folios compared to the remaining text. These first eleven folios also exhibit many mistakes as well as correction which were made by hand. The folios 252 to 269 have also been incorrectly arranged and should have been inserted between the folio 211 and 212. However, even with these shortcomings this manuscript is still considered the oldest and most reliable copy available of al-Ṣūfís book. Therefore I have chosen this manuscript to be the basis for this study and I managed to acquire a facsimile copy of this work.


Figure 22 The Last Page of Marsh 144 Manuscript

- The MS5036 Manuscript

The MS5036 manuscript is found at the National Library in Paris. It is dated A.H. 833 / A.D. 1430. The final page of his manuscript is shown in Figure 11. This copy was written for King Ulugh Bēg as is mentioned at the last page of this manuscript. As I said earlier, the text next to the last table of this manuscript states that the pictures were drawn according to the instructions of Ibn al-Ṣūfĩ and the data were taken from the copy of Naṣīr al-Dīn al-Ṭūsī. This is a very well-written manuscript with clear tables and pictures of the constellations. The stars which are part of the main constellation picture were drawn in gold while the stars drawn in red are outside the constellation. The manuscript contains 494 pages of the size 285 by 205 mm also written in Nasta'lik style with 13 lines on each page. Even though this manuscript was written much later, I needed another well-written but reliable copy to compare with and complete the last missing page of the Marsh144 manuscript. Since this copy was written for Ulugh Bēg from al-Ṭūsi’s copy I believe that it is a good reliable copy of al-Ṣūfi's work which I could utilize. Therefore I have chosen this copy and I included the text of this manuscript whenever I needed to complement the work.

### 5.2 The Structure of al-Ṣūfī's Book and Star Catalog

The original Arabic name of al-Ṣūfi's book was 'Șuwar al-Kawākib al-Thamāniyah wa-al$\bar{A} r b a ' e e n '$ which is simply translated as 'The 48 Constellations'. However, it was later known by other names, the most famous of which are: 'Kitāb al-Kawākib al-Thäbitah' or the 'The Book of the Fixed Stars' and 'Kitāb al-Kawākib al-Thäbitah Mușawaran' or the 'The Illustrated Book of the Fixed Stars'. This book was also known by another name which was: 'Kitäb Șuwar al-Samawīyah Muşawaran' or 'The Illustrated Book of the Heavenly Signs'. I will begin this study of al-Ṣūfi's work with the description of the structure and layout of the ‘Book of the Fixed Stars'. Al-Ṣūfi's original Arabic text contained 55 astronomical tables as well as star charts of 48 constellations. Al-Ṣūfi commented in detail on every constellation before every section of those star charts. These tables and charts were written in the same order using the same structure and layout as in the Almagest. Al-Șūfi's book is divided into four main sections:

## 1. The Introductory Chapter

Al-Ṣuff's introductory chapter is a very important part of his work. In it he explained the reasons for writing his book. He also included his strong criticisms of other works, especially those of al-Battān̄̄ and al-Daīnawari. He explained the method he used in writing his book and the technique he used for calculating the precession value. Al-Ṣufi also identified the 48 constellations which, as he mentioned, were taken from Ptolemy's Almagest. He also mentioned that some ancient astronomers counted the number of stars in each constellation to be 917 stars that are included in the main constellations and 118 stars outside of the constellations. He then mentioned that other people also mistook the number of the stars in the sky to be 1025 stars only and this is wrong also because as he explained, there are many other stars of the $5^{\text {th }}$ and $6^{\text {th }}$ magnitude. He finally summarized the total number of brightlyobserved stars to be 1022 except the three stars that are part of the Asterism 'al-Dafira'. He also explained how the tables were compiled and the reason and method for using the dual constellations charts and images. (See translation and comments on al-Ṣūfi's introduction chapter)
2. The 21 Chapters of the Northern Constellations (Table 4):

| $\#$ | Constellation <br> name | \# stars <br> in | \#stars <br> out | Arabic names according to al-Sūfī |
| :--- | :--- | :--- | :--- | :--- |
| 1 | Ursa Minor | 7 | 1 | al-Dub al-Aṣghar |


| 2 | Ursa Major | 27 | 8 | al-Dub al-Akbar |
| :---: | :---: | :---: | :---: | :---: |
| 3 | Draco | 31 | - | al-Tinnīn |
| 4 | Cepheus | 11 | 2 | Qīqāwūs; al-Multaheb |
| 5 | Bootes | 22 | 1 | al- 'Awwā; al-Sayyāh ; al-Naqqār; Hāaris alShamāl |
| 6 | Corona Borealis | 8 | - | al-Iklīl al-Shamālī; al-Fakka |
| 7 | Hercules | 28 | 1 | al-Jāthì 'ala Rukbateh; al-Rāqes |
| 8 | Lyra | 10 | - | al-Silyāq; al-Wazza; al-Subeḥ; al-Ma'refa; alSulahfāt |
| 9 | Cygnus | 17 | 2 | al-Țā'er; al-Dajāja |
| 10 | Cassiopeia | 13 | - | Dhāt al-Kursīy |
| 11 | Perseus | 26 | 3 | Barshāūsh; Hāmel Ra's al-Ghūl |
| 12 | Auriga | 13 | - | Mumsek al- 'Inān; al- 'Inān; Mumsek al-A 'ina |
| 13 | Ophiuchus | 24 | 5 | al-Hawwa' |
| 14 | Serpens | 18 | - | al-Hayyā |
| 15 | Sagitta | 5 | - | al-Sahem |
| 16 | Aquila | 9 | 6 | al- 'Uqāb; al-Nasr al-Ṭà'er |
| 17 | Delphinus | 10 | - | al-Dalfin |
| 18 | Equuleus | 4 | - | Qut'at al-Faras |
| 19 | Pegasus | 20 | - | al-Faras al-A'zam |
| 20 | Andromeda | 23 | - | al-Mara' al-Musalsala |
| 21 | Triangulum | 4 | - | al-Muthallath |

The total number of stars in the northern constellations is 330 which form the main body of the northern constellations and 29 stars outside of the constellations making a total of 359 stars. However, in his introductory chapter al-Ṣūfī mentioned that the total numbers of stars was 331 that are part of the northern constellations and 29 that are outside of the constellations totaling 360. This is because Ptolemy assigned 14 stars to the constellation Auriga whereas al-Ṣūfì only found 13; the last was not seen by him.
3. The Twelve Chapters of the Constellations of the Zodiac (table 5):

| \# | Constellation name | $\begin{aligned} & \text { \# stars } \\ & \text { in } \end{aligned}$ | \#stars out | Arabic names according to al-Ṣūfī |
| :---: | :---: | :---: | :---: | :---: |
| 1 | Aries | 13 | 5 | al-Hamal |
| 2 | Taurus | 32 | 11 | al-Thawr |
| 3 | Gemini | 18 | 7 | al-Tawāmān |
| 4 | Cancer | 9 | 4 | al-Sarațān |
| 5 | Leo | 27 | 8 | al-Asad |
| 6 | Virgo | 26 | 6 | al-'Adhrā'; al-Sunbula |
| 7 | Libra | 8 | 9 | al-Zubānayn ; al-Mīzān |
| 8 | Scorpio | 21 | 3 | al-'Aqrab |
| 9 | Sagittarius | 31 | - | al-Rāmī; al-Qaws |
| 10 | Capricorn | 28 | - | al-Jadī |
| 11 | Aquarius | 42 | 3 | Sākib al-Mā'; al-Dalw |
| 12 | Pisces | 34 | 4 | al-Samakatān ; al-Hиūt |

The total number of stars in the Zodiac constellations is 289 which form the main body of the constellation and 60 stars outside of the constellation, with a total of 349 stars. However, in his introductory chapter al-Ṣūfì mentioned that the total numbers of stars was 289 that are part of the Zodiac constellations and 57 outside of the constellations, totaling 346 except for the asterism called 'al-Dafira' which is a 3-star group.
4. The Southern Constellations which are 15 Constellations Chapters (table 6):

| \# | Constellation name | \# stars <br> in | \#stars out | Arabic names according to al-Ṣūfì |
| :---: | :---: | :---: | :---: | :---: |
| 1 | Cetus | 22 |  | Qītus |
| 2 | Orion | 38 |  | al-Jabbār; al-Jauzä' |
| 3 | Eridanus | 34 |  | al-Nahr |
| 4 | Lepus | 12 |  | al-Arnab |
| 5 | Canis Major | 18 | 11 | al-Kalb al-Akbar |
| 6 | Canis Minor | 2 |  | al-Kalb al-Mutaqadem; al-Kalb al-Asghar |
| 7 | Argo Navis | 45 |  | al-Safina |
| 8 | Hydra | 25 | 2 | al-Shuja' |
| 9 | Crater | 7 |  | al-Bātıīya |
| 10 | Corvus | 7 |  | al-Ghurāb |
| 11 | Centaurus | 36 |  | Qanturūs |
| 12 | Lupus | 18 |  | al-Sab ${ }^{\text {c }}$ |
| 13 | Ara | 7 |  | al-Jamra; al-Majmara |
| 14 | Corona Australis | 13 |  | al-Iklīl al-Janūb̄̄ |
| 15 | Piscis <br> Austrinus | 11 |  | al-Ḥūt al-Janūb̄̄ |

The total number of stars in the southern constellations is 295 which form the main body of the constellation and 13 outside of the constellation, with a total of 308 stars. However, in his introductory chapter al-Ṣūfī mentioned that the total numbers of stars was 297 that are part of the northern constellations and 19 outside of the constellations totaling 316 stars. This is because Ptolemy assigned 37 stars to the constellation Centaurus and 19 stars to the constellation Lupus, whereas al-Ṣūfi found one less star in each of these two constellations. The other difference is that Ptolemy added 6 stars to the last constellation Piscis Austrinus whereas al-Ṣūfī did not include these in his catalog nor does he mention them in the comments on this constellation in his book.

Each constellation chapter is in turn divided into three parts. The first part is a detailed written commentary describing the position of the stars, their numbers, magnitudes as well as many other details. Al-Ṣūfī also tried to identify the stars or group of stars according to the old Arabic tradition, by giving their old Arabic names and what the Arabs said about
them. The Arabic text in Figure 23 is from a copy of a manuscript which was written by Ulugh Bēg in the $15^{\text {th }}$ century. As we can see it is a very well-written and clear manuscript. It is one of the manuscripts that I used in the translation.

The second part of the constellation chapter is a table showing the coordinates and magnitude values for every constellation (see Figure 24). The stars in every constellation were divided into two groups. The first groups of stars were those that form the main image of the constellation. The other groups were the stars outside the image. Al-Ṣūfī used ecliptical coordinates, as did Ptolemy before him.

The last parts for each constellation chapter are the charts (see Figure 25). These were the dual charts depicting the stars as they appear in the sky and as they were drawn on a globe.


Figure 23 written commentary


Figure 24 Tables


Figure 25 the charts

### 5.2.1 Method Used in Translating 'The Book of the Fixed Stars'

The main effort to search for the hidden treasures in al-Ṣūfīs book started with the translation of this work from Arabic to English, especially the constellation commentaries. For every constellation al-Ṣūfì wrote a commentary which describes in detail the number of stars, their location and their magnitudes. Therefore, the information regarding the magnitude estimate in particular can be more reliably taken from the text than from the tables which might not be correctly copied.

The layout of the translation was as depicted in Figure 26 which shows the table or the star catalog for the constellation Ursa Major. Next to it is the corresponding English translation. At the top of this table al-Ṣūfī noted that he added 12 degrees 42 minutes to

Ptolemy's longitude to allow for precession. The first column gives the number of the star in the constellation. The second gives the description or name of the star. This sometimes included the star color, Arabic name and explanation on the position of the star in the constellation. The third group of columns gives the ecliptical longitude coordinates. It was also customary to divide the ecliptic into twelve 30 degrees divisions. Therefore when describing the longitude, al-Ṣūfī first wrote the number of that division then the remaining degrees and minutes in order to depict the complete longitude value. The fourth column gives the latitude direction of the star relative to the ecliptic. The fifth group of columns gives the latitude coordinates. And the last column gives the apparent magnitude estimates as the author found them.


Figure 26 The Layout of the Translation

### 5.3 Maps in al-Ṣūfī’s Book

Cartography or mapmaking has been an integral part of the human development for thousands of years. There is some evidence that suggest that the figurative paintings which were produced in the Lascaux Caves more than 12,000 years ago might have some reference to the phases of the Moon and the animal figures depicted in these caves might also suggest some reference to seasonality changes (Krupp, 1997: 122). Almost all ancient cultures such as the Babylonians, Greeks and Chinese created and used maps in order to help them explain and navigate their way through out the world. The first known maps were those of the heavens. Stellar cartography or 'Uranography' is the science of mapping or projecting representations of stars and other celestial bodies on to flat surfaces such as paper or stone or onto spherical objects. The art or science of Uranography started by observation of the sky, then by measuring the position of the stellar objects in order to produced star tables and maps or charts for use by astronomers and astrologers. A variety of instruments and techniques was developed to help produce these tables and charts such as angular measurements, light or magnitude determination methods, quadrants, astrolabes, globes and others.

The earliest ancient Greek scientist who is believed to have constructed a map of the world is Anaximander of Miletus (B.C. 611-546). One of the first Greek philosophers to draw the stars on a globe was Eudoxus of Cnidus (B.C. 408-355). He was considered the first to represent the sky from outside looking in rather than as seen by an observer on the Earth (Harley \& Woodward, 1987). In classical antiquity, maps were drawn by Hecataeus, Herodotus, Eratosthenes and Ptolemy using astronomical and mathematical techniques. The oldest available representation of the celestial sphere is the Farnese Atlas which is a $2^{\text {nd }}$ century Roman marble copy of a statue of Atlas kneeling with a globe on his shoulders. The globe depicts the night sky as seen from outside the celestial sphere showing 41 out of the 48 classical Greek constellations as mentioned by Ptolemy. Chinese mapping of the stars began at much the same time as Greek celestial cartography. However, in general this did not make a significant contribution to the development of Islamic astronomy.

In the Middle Ages, Arab and Islamic scholars continued to produce stellar maps using methods which they found in Greek sources such as Ptolemy's Almagest and Geography. Astronomers and geographers working under Caliph al-Ma'mūn in the $9^{\text {th }}$ century re-measured the distance on the Earth that corresponds to one degree of the celestial meridian in order to help them calculate the circumference of the Earth. al-Ma'mūn also patronized the production of a large map of the world, which has not survived. Historical records point to many important Arab and Islamic astronomers who worked on this subject
and produced works resembling the Greek classical globes such as the Farnese Atlas and illustrated astronomical maps. The works of these scholars must have been known during the Middle Ages because al-Ṣūfī mentioned in his book that he saw a book by 'Uṭārid with celestial maps and a celestial globe by al-Harrānī which he both criticized because of the errors he found in them. Unfortunately none of these works is extant today. The earliest surviving celestial map in Islamic culture is to be found in an $8^{\text {th }}$ century Umayyad palace called Qaser al-Ūmāra'. This palace contains a room with a dome on to which a painted fresco of the celestial heaven is drawn on the ceiling. The design of this fresco was drawn as if you are looking down on a globe and not as you would be looking to the sky. The constellations of Qaser al-Ūmāra' were based on classical or early medieval western Byzantine style.

### 5.3.1 The Characteristics and Development of al-Ṣūfís Constellations Images

The Marsh144 manuscript by al-Șūfī is one of the oldest illustrated Islamic manuscripts which we know of today. One of al-Ṣūfi's innovations in charting the stars was the production of dual illustrations of each of Ptolemy's constellations. One illustration was as portrayed on a celestial globe. The other illustration as viewed directly in the night sky. At the end of the chapter on the constellation Ursa Minor, al-Ṣūfī explains why he produced two different sets of pictures and outlined the method of using these maps as follows:
> "For every constellation we have drawn two pictures: one as it is projected on the globe and the other as it is seen in the heavens. Hence we have covered both of the different cases, so there is no confusion for anyone who sees that what is viewed on the globe is different from what is in the heavens. When we want to see the constellation as it (really) is we lift the book over our heads and we look at the second picture (in the book). From beneath (the book) we are viewing (the constellation) as it is seen in the heavens."

Figure 27 is a picture of the constellation Equuleus from the manuscript Marsh144. The right figure shows the constellation as seen on a celestial globe. The left figure shows the constellation as it is seen in the sky. Figure 28 is a picture of the constellation Cancer from the Paris manuscript MS5063. In this latter illustration, the upper figure shows the constellation Cancer as seen on the celestial globe. The lower figure shows the constellation as it is seen in the sky. In this Figure the stars drawn in gold are considered part of the
constellation picture while the stars drawn in red are bright enough to be noticed but are outside the constellation.


Figure 27


Figure 28

It is interesting to note that all the Arab and Islamic astronomers including al-Șūfī were inconsistent and incorrect in their depiction of the constellations. Ptolemy's original description of the constellations was based on an interior point of view; therefore Ptolemy described the figures of the constellation as if the observer would see the constellation figure from a central position looking up. However when the constellations are projected on a celestial globe then the exterior observer should be seeing the reverse of the constellation figures looking down on the globe. However in all Arab and Islamic globes the constellation figures are all drawn in front view therefore the images are mirrored in order to depict them looking towards the observer. It is unknown why the Arabs used such a system for drawing the constellations on the globes. Most probably they wanted to avoid depicting the figures whereby they are represented from the rear.

Since al-Ṣūfí's work was based on Ptolemy's Almagest therefore most of the rendering of the constellation figures resemble classical style similar to the Farnese globe constellations. However some of the figures have undergone a process of 'orientalization' which probably began before al-Ṣūfī started to write his work. This process was the result of misunderstanding some of the Greek mythology figures as well as copyist errors in some of the versions of the Almagest. The other diversion from classical style constellations was also due to influence of the $A n w \bar{a}$ ' tradition in which al-Ṣūfī was very much interested. An example of such addition is to be found in the constellation Andromeda. Al-Ṣūfì makes three illustrations for this constellation. The first is the figure of Andromeda with her arms
stretched out. The second is the figure of Andromeda with a fish covering her legs (Figure 29). The third illustration is with two fishes covering her body (Figure 30). Another example of this $A n w \bar{a}$ ' tradition is the illustration of a full horse figure which is to be found between the constellation Equuleus and Pegasus (Figure 31). All these iconographies were not part of the original classical Greek tradition (Wellesz, 1965).


The constellation figures of manuscript Marsh144 especially the facial outlines were drawn according to style of the $9^{\text {th }}$ century Abbasid period. They were rendered in a flat twodimensional style. Their faces were drawn almost in profile while their bodies in full view usually with their arms stretched out. The turbans were depicted from a later $10^{\text {th }}$ century style, an example of which can be found in the decorative pottery of that era. In later manuscripts of al-Ṣūfî's book the turbans as well as garments were also altered to reflect the dressing style of the era when these manuscripts were copied. However it is interesting to note here that the drawings of the jewelry, the garments and some of the constellations in the Marsh144 manuscript were also influenced by a much earlier period in history, as is found in the Art of the Sassanid era. An example of such Sassanid influence can be found in the illustration of the flying wings of Pegasus (Figure 32) which resembles Simurgh the Sassanian mythical flying creature (Figure 33).


Figure 32


Figure 33

By the time we reach the manuscript MS5063 we see that some of the illustrations have undergone an iconographical change which reflects the time that this manuscript was produced. This is evident in the illustration of constellation Cetus; when this is compared to the Marsh144 manuscript (Figure 34) we find a strong Chinese influence in the iconography of the beast which now resembles a Chinese dragon (Figure 35).


Figure 34


Figure 35

Another interesting constellation to note is the constellation Lyra or Lyre meaning the Harp. Al-Ṣūfī gave several names for this constellation: al-Silyāq; al-Wazza; al-Subh; alMa'arefa and al-Sulaḥfāt. The word al-Silyāq was also written as al-Shilyāq; however, Kunitzsch corrected this name to Salbāq which was a kind of harp used by ancient Arabs (Kunitzsch \& Smart, 2006: 44). The Marsh144 manuscript indeed depicts this constellation as a type of harp (Figure 36). However in many other eastern manuscripts Lyra was illustrated as a Sulaḥāt or tortoise. Al-Ṣūfì mentioned that he saw this constellation drawn on some celestial globes as a Sulaḥfāt. An example of this is seen in the manuscript MS5063 (Figure 37). The other name given to this constellation which was probably based on the $A n w \vec{a}$,
tradition was al-Wazza meaning the Goose. This depiction was used in later western illustrations while adding the image of the harp superimposed on the image of the goose. Such an illustration can be found in Andreas Cellarius’ Harmonia Macrocosmica which is a stellar catalogue published in 1660 and in Johann Hevelius' Uranographia printed in 1690 (Figure 38).


Figure 36


Figure 37


Figures 38

### 5.3.2 Accuracy of the Maps

An important issue concerns the accuracy of these maps. Were they really used as they were intended by al-Ṣūfî? It is apparent that as an observational astronomer and an instrumentmaker al-Ṣūfĩ was very much concerned with the accuracy of the data he had and the way the maps should be used when observing the heavens or when constructing a celestial globe. Since the Marsh 144 manuscript was written by the al-Ṣūfîs son therefore it might have been copied as close to the original as possible with regards to the illustrations and images of the constellation provided the son was as good as the father. However, these star maps might be considered an accurate depiction of the heavens according to al-Ṣūfí. Therefore it might also be safe to assume that these star charts were used to help the observer locate the main celestial bodies in the sky with ease and accuracy. As for the other manuscript MS5063, which was written for Ulugh Bēg who was also an important astronomer, his copy might have also been accurately produced and illustrated under the guidance of Ulugh Bēg himself for this purpose.

Therefore in order to investigate this question I have reproduced two star charts from al-Ṣūfís manuscripts Marsh144 and MS5063 and a projection upon a modern chart showing the location of these stars in the constellation was then made. As can be seen from the projection of the chart from the manuscript Marsh144 for the constellation Orion (Figure 39) the chart is somewhat accurate and it could have been used as al-Ṣūfĩ intended it to be used.

The other projection of the chart is from the manuscript MS5063 for the constellation Ursa Minor (Figure 40). This chart can also be considered as a fairly accurate presentation of the constellation.


Figure 39 Projection of the Chart Manuscript Marsh144 for the Constellation Orion


Figure 40 Projection of the Chart Manuscript MS5063 for the Constellation Ursa Minor

### 5.4 Al-Şūfi’s Data Analysis and 3-step Magnitude System

As discussed above, al-Ṣūfís star catalog was based on Ptolemy's classical work the Mathematike Syntaxis which was later called the Almagest by the Arabs. In his introductory chapter al-Ṣūfì corrected several observational errors in the works of his predecessors, like the famous Arab astronomer al-Battānī. He also exposed many of the faulty observations found in the various versions of the Almagest. However his major endeavor was to carefully define the boundaries of each constellation, and record the magnitudes and positions of stars using new and independent observations he made himself. For the epoch of his catalog al-Ṣūfī adopted the beginning of the year 1276 of the era of Alexander (Th $\bar{u}$ al-Qarnain) which corresponds to the year A.D. 964 (Kunitzsch, 1986). Al-Ṣūfī updated Ptolemy's stellar longitudes from A.D. 125 to A.D. 964 by adjusting for precession. However al-Ṣūfì mentioned that "Ptolemy used the observations of Menelaus' who made his observations in the year 845 of the year of Nabūkhat Nassar. Al-Ṣūfī also mentioned that: "The time difference between the observations of Menelaus and the date of Ptolemy is 41 years". He concluded that Ptolemy added 25 minutes to Menelaus' longitude values to account for precession. However it is still unknown why al-Ṣūfī refers to this fact because at this time there is no evidence or available text that mentions that Ptolemy used Menelaus observations other than al-Ṣūfî's claim (Grasshoff, 1990: 21).

At the end of al-Ṣūfí's introductory chapter he described in detail the method he used in constructing his catalog especially in calculating precession. For his epoch of A.D. 964 he applied the most accurate Arabic precession constant at that time of 1 deg in 66 years rather than the correct value of 1 deg in 71.2 years, thereby adding 12 degrees 42 minutes on Ptolemy's longitude value to allow for precession. Over the 839 years between the tables of Ptolemy and al-Ṣūfí, precession would actually amount to 11 deg 47 min . Hence by using 12 deg 42 min , al-Ṣūfí over-corrected Ptolemy's stellar longitudes by 55 min . Therefore, it would be unreasonable to compare the accuracy of al-Sufi's data with those of Ptolemy's because of this overcorrection which renders al-Ṣūfí's coordinates to be slightly more accurate then Ptolemy's. Al-Ṣūfī could not have been aware of this over-correction because his calculations were based on the Almagest and thus he did not discover the systematic error in Ptolemy's longitude even though Arabic and Islamic astronomers recognized earlier on that Ptolemy's value of precession was false. As for the ecliptic latitudes, al-Ṣūfî also explained in his introductory chapter that: "...since they (the stars) rotate around the poles of the ecliptic therefore they do not ever change".

The study and analysis of al-Ṣūfî's stellar data can be divided into two parts. The first is the study of the ecliptical longitude and latitude coordinates which where included in the stellar catalog. The second is the analysis of magnitude values which are found in both the chapters on the constellations as well as in the stellar catalog. As I mentioned earlier the study or analysis of the coordinate values is closely related to the study of the Almagest. Al-Suūì relied heavily on Ptolemy's values where-by he merely adopted these coordinates which he found in the Almagest while adding 12 degrees 42 minutes on Ptolemy's longitude values to allow for precession. However, in many instances al-Ṣūfĩ mentioned that the coordinates of Ptolemy are incorrect. For example in the constellation Ursa Minor al-Ṣūfī states:
> "In some of (Ptolemy's) stars both the latitude and longitude are incorrect. This is because if they are marked on a (celestial) globe according to (Ptolemy's) table of latitude and longitude, especially (the stars of) al$N a$ 'esh, we notice that the image (of the constellation) in the heavens does not correspond with what is (seen) on the globe"

Such a statement was repeated many times throughout the book, however it is again a surprise that our author did not follow up on these comments and correct what he thought to be Ptolemy's errors. This again might have been out of respect and in order to keep with the data which was found in the Almagest. The study of Ptolemy's coordinates was extensively covered in many research papers and books by prominent scholars such as Knobel, Peters, Newton, Toomer, Kunitsch and Grasshoff. Therefore the major analysis which I made for this study was to compare al-Ṣūfi's star magnitudes with modern values and with those found in the Almagest. I have tabulated the magnitude values of al-Ṣūfì and Ptolemy, together with the modern star magnitudes (table to be found in Appendix-A). Ptolemy's magnitude values and the star identification have been taken from G.J Toomer's book while the modern magnitude values were taken from the Bright Star Catalogue.

At first glance it would seem that about $50 \%$ of al-Ṣūfi’s magnitude values were identical with those of Ptolemy's. The results showed that the magnitude values of 520 stars out of the total 1022 stars were identical between al-Ṣūfī and Ptolemy. Therefore one might wonder whether al-Ṣūfì only re-estimated the magnitudes of about half of the stars observed by Ptolemy. However, upon detailed comparison I found that out of these 520 stars only 206 stars have difference in values from the modern visual magnitude by more than 0.5 magnitude and only 56 stars where the difference in values from the visual magnitude is more than 1 magnitude. The results also showed that out of these 56 stars 22 stars have magnitudes of 5 or 6. This can also be understood because it is difficult to visually estimate some of these faint
stars. Therefore a level of accuracy of 0.5 magnitudes is more than can be expected of eye estimation, either by al-Ṣūfì or Ptolemy for these stars. This conclusion is confirmed by the calculation of the standard error. Consequently I do not believe that al-Șūfī could have been more accurate in these stars by more than the 0.5 magnitudes. Another study conducted by Tomoko Fujiwara and Hitoshi Yamaoka (2005) on the magnitude estimates of old star catalogs also confirm the above result. Fujiwara and Yamaoka found that the $1^{\text {st }}$ and the $6^{\text {th }}$ magnitude stars in the old star catalogs should not be used in determining the current magnitude system because they exhibited a Malmquist bias where as all other stars magnitude in the old catalogs fit a logarithmic scale consistent with the light ratio of $\mathrm{R}=2.512$. However all this does not prove that al-Ṣüfì did or did not himself re-estimate all stars again.

Al-Șūfi and Ptolemy both added intermediate values to the magnitude class system for some stars. Ptolemy mentioned the words 'more-bright' and 'less-bright' for certain stars. However al-Șūfì expressed these intermediate magnitude values by the words 'Aṣghareh' which means 'less' or 'Akbareh' which means 'greater' and ' $A$ 'zameh' which means 'muchgreater'. Most scholars who studied al-Ṣūfi's work used the translation of Schjellerup (1874), who did not differentiate between the two words 'Akbareh' and ' $A$ 'zameh'. In Schjellerup's translation the magnitude was written as a middle value; for example 4-5 (between 4 and 5 magnitude). In their work on Ptolemy, Knobel \& Peters (1915) and later Toomer (1998) as well as Grasshoff (1990) also relied upon Schjellerup's translation of al-Ṣūfi's data. They expressed Ptolemy's magnitudes by the words 'greater' and 'less'. They expressed these magnitudes on a 2 -step system. By the $20^{\text {th }}$ century this 2 -step intermediate magnitude was numerically interpreted by a constant difference of ( 0.33 ) magnitude especially by Grasshoff. However, when we look at al-Şūfi's text in detail it is evident that he made a clear distinction between three intermediate magnitudes. I believe that al-Ṣüfĩ used what I have termed a 3step intermediate magnitude system, which was more accurate than Ptolemy 2 -step intermediate system. I think that with this system al-Ṣūfì managed to express all magnitude values by a constant difference of 0.25 . For example the magnitude of the star 19 Ursa Major was expressed by al-Ṣūfi as "much greater than $3^{\text {rd }}$ magnitude". This can be interpreted on the 3 step scale as ( 3 minus 0.5 ) which is equal to 2.5 magnitudes. The modern star magnitude is 2.44 which is a fairly close value. However if we are to interpret this on a 2 -step scale as in Ptolemy then we get the magnitude value of 2.7. However it is unclear why al-Șūfĩ did not make this distinction in the tables when he clearly expressed this difference in the constellation chapters and comments.

One of the main topics of this study was to research this 3-step intermediate magnitude system which would shed new light on the accuracy and independence of al-Ṣūfi's
work. Therefore in this part of the study I have made a complete analysis on al-Șūfi's magnitude values where the magnitude values were numerically interpreted by a constant difference of 0.25 magnitudes: that is +0.25 for 'less', -0.25 for 'greater' and -0.5 for 'muchgreater'. Ptolemy's 2 -step intermediate magnitude difference was interpreted by a constant of (0.3) magnitude. However, in order to analyze this topic further, all the data and information from al-Șūfi's book were collected in a table (see Appendix 8.1). The first three columns of this table show the number and the number sequence of the stars and constellations. The $4^{\text {th }}$ to the $9^{\text {th }}$ columns are the coordinated values according to al-Șufi's tables. The $10^{\text {th }}$ column shows the magnitudes of the stars according to al-Ṣūfi. I used the letters (s) for 'less', (k) for 'greater' and ( m ) for 'much-greater'. The $11^{\text {th }}$ column shows the magnitudes after adjustment for the 3 -step system and the $12^{\text {th }}$ column for the 2 -step system. This was done by adding the values +0.25 for 'less', -0.25 for 'greater' and -0.5 for 'much-greater' for the 3 -step system while I added the values +0.3 or -0.3 for the 2 -step system. The $13^{\text {th }}$ column shows the magnitude according to Ptolemy. Here I used the magnitude which al-Șūfi attributed to Ptolemy. The $14^{\text {th }}$ column shows Ptolemy's magnitudes after adjustment for the 2 -step system. The $15^{\text {th }}$ and $16^{\text {th }}$ columns show the modern visual magnitude and the HR number for each star. Then I conducted an accuracy analysis for the magnitudes of al-Șūfi and Ptolemy by calculating the difference $(\Delta)$ between those values and the visual magnitudes in order to see if al-Șūfí had in mind a two-step or three-step magnitude systems. The statistical results of this analysis are summarized in (Table 7) which shows the Mean and the Standard Deviation for all 1022 stars combined:

Table 7 Statistical Data.

|  | Mean | standard <br> deviation |
| :--- | :--- | :--- |
| al-Ṣūfi 3-step | -0.06 | 0.59 |
| al-Şūfi 2-step | -0.09 | 0.59 |
| Ptolemy | +0.07 | 0.71 |

From the above values it seems that the mean for the 3 -step system is slightly better but barely statistically significant. The standard deviation is the same whether we apply the 3 or 2 step system whereas it is higher with Ptolemy. The dispersion in al-Sūfi's data is thus significantly less than in Ptolemy. The statistical results for al-Sūfì values according to the above table are not entirely conclusive between the 2 -step and the 3 -step systems. However, I still believe that al-Șūfi intended to use the 3 -step system. The main reason for this assumption is the way al-Ṣūfī expressed or described the values of the stellar magnitudes in
his book. For example, if we look at magnitude values in the constellation Gemini, it is clear that al-Ṣūfī was referring to three separate intermediate magnitudes (Table 8).

Table 8 al-Ṣūfì magnitudes for Constellation Gemini.

| 1 | GEMINI | 2 |
| :--- | :--- | :--- |
| 2 | GEMINI | 2 |
| 3 | GEMINI | $4(\mathrm{~m})$ |
| 4 | GEMINI | 4 |
| 5 | GEMINI | 4 |
| 6 | GEMINI | 4 |
| 7 | GEMINI | $4(\mathrm{k})$ |
| 8 | GEMINI | $5(\mathrm{~s})$ |
| 9 | GEMINI | 5 |
| 10 | GEMINI | $3(\mathrm{~s})$ |
| 11 | GEMINI | 3 |
| 12 | GEMINI | $4(\mathrm{~m})$ |
| 13 | GEMINI | $3(\mathrm{~s})$ |
| 14 | GEMINI | $4(\mathrm{k})$ |
| 15 | GEMINI | $4(\mathrm{k})$ |
| 16 | GEMINI | $3(\mathrm{~s})$ |
| 17 | GEMINI | 3 |
| 18 | GEMINI | 4 |
| 19 | GEMINI | $4(\mathrm{~s})$ |
| 20 | GEMINI | $4(\mathrm{~s})$ |
| 21 | GEMINI | $5(\mathrm{~s})$ |
| 22 | GEMINI | $5(\mathrm{~s})$ |
| 23 | GEMINI | $5(\mathrm{~s})$ |
| 24 | GEMINI | $5(\mathrm{~s})$ |
| 25 | GEMINI | $4(\mathrm{~s})$ |

From the various magnitude values which we can see in the constellation Gemini, alṢūfī made the distinction between (m) and (k) and he was not really concerned with word repetition or correct sentence structure. The above example shows that he expressed 4(m) and $4(\mathrm{k})$ consecutively then $4(\mathrm{k})$ twice. He also mentioned several (s) successively. These word repetitions for the various terms are to be found in many places through out the work. For example in the constellation Taurus, al-Ṣūfī wrote:
"The third (star) is south of the second, close to it, and is much greater than $4^{\text {th }}$ magnitude, but it was mentioned by Ptolemy as $4^{\text {th }}$ magnitude exactly. The fourth (star) is the southernmost star of the four, south and close to the third, and is much greater then $4^{\text {th }}$ magnitude, but it was mentioned by Ptolemy as $4^{\text {th }}$ magnitude exactly".

Here also the term $A$ 'zameh (much-greater) was used repeatedly in order to give the exact value which was intended. Therefore the assumption of word repetition is not valid in this case. Al-Șūfi also used the word Aşghareh (s) throughout his entire work and he repeated it many times consecutively in many locations through out his book. Therefore, if al-Ṣūfī was concerned with correct grammatical structure, why did he not use other words for the term 'less' (s) Asghareh even though there are many other words in Arabic vocabulary which could have been used for this case?

However, the question arises is why did al-Șūfì not include these distinctions in his tables of the constellations? One answer to this question might be that the original tables which were written by al-Șūfì possibly included these values, but they might have been omitted when the work was copied even by al-Șūfi's son. However, the other reason which is much more reasonable is that al-Ṣūfi did not deviate too much from the format of Ptolemy's catalogue out of respect for this standard reference work since he asserted that he is compiling the tables according to the Ptolemy's Almagest.

### 5.5 Stars Mentioned by al-Şūfī and not in the Almagest

In his written comments on the constellations, al-Ṣūfī mentioned some additional stars that were not included in Ptolemy's star catalog. However, it is surprising that al-Ṣūfí did not include these stars in his tables even though he identified many of them in detail and described their magnitudes and he even estimated their locations. One reason why al-Ṣūfĩ did not include these additional stars might have been out of respect for Ptolemy's catalogue which had long been a standard reference work in this field. In his introductory chapter alṢūfi's clearly stated that the tables he produced were made according to Ptolemy's work; therefore he might have been inclined to follow the classical tradition to which he and all other scholars before him were used.

It is also surprising that there are very few Arabic or Islamic historical sources that mention these additional stars. However the major text which makes reference to these stars is the Alfonsine IIII Libros de la Ochaua Espera (Four Books of the Eight Spheres) which was also called Libros de las Estrellas Fixas (Books on the Fixed Stars). These works were produced in Toledo in A.D. 1256 but were based on the al-Ṣūfís Book of the Fixed Stars. Book four of these Alfonsine texts was a statistical summary which included the number of stars in each constellation as well as Arabic names of stars according to Arabic folk astronomy (Samso et al., 1988). This book also included a general list of 84 stars taken from al-Ṣūfí's work which were not mentioned by Ptolemy.

In this part of the study I have identified a total number of 134 of these additional stars; 65 were located in the Northern constellations, 41 in the Zodiac constellations and 28 in the Southern constellations. Al-Ṣūfì mentioned these stars in his constellation commentaries but not in the tables and he clearly said that these stars were not mentioned by Ptolemy. In many instances al-Ṣūfí mentions that in several areas of the sky there are many stars but he fails to mention a definite number because of their large numbers. For example in the comments on the constellation Ursa Major al-Ṣūfì wrote that: "Throughout (the main image of the) constellation and outside of it, there are many stars of the $5^{\text {th }}$ and $6^{\text {th }}$ magnitudes. Additionally there is an infinite number of dim (stars) which are outside of the $6^{\text {th }}$ magnitude (classification)."

Therefore I have tried to identify in the below tables all the major stars that were mentioned by al-Ṣūfì. I have also tried to identify these stars by their HR number and I have included the magnitude that al-Ṣūfī assigns together with the modern magnitude for these
stars. In the star number column, I continued with the sequence of the star number as per alṢūfì in order to include these numbers in the star charts.

Table 9: Northern Stars mentioned by al-Ṣūfī but not by Ptolemy.

| Number | Star number (as per al-Ṣūfī) | Star/s (HR) | Al-Ṣūfī <br> Magnitude | Modern Magnitude | Explanations and Comments |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 36 Ursa Major | 5062 | Not mentioned | 4.01 | This is the star named Alcor. The Arabic name is al-Suh $\bar{a}$. This star was not mentioned in Ptolemy; therefore it was not presented in al-Ṣūfî's chart. However al-Ṣūfī mentioned this star in his written explanation of this constellation. <br> This is a very famous star in Arabic tradition, as al-Ṣūfī explained that this star was used to test eyesight. |
| 2 | 37 Ursa Major | 4518 | 4 | 3.71 | Al-Ṣūfi mentioned this star in his written explanation of this constellation and he mentioned that it was not included in Ptolemy. |
| 3-7 | 38 Ursa Major 39 Ursa Major 40 Ursa Major 41 Ursa Major 42 Ursa Major | $\begin{aligned} & 4392 \\ & 4248 \\ & 4277 \\ & 4288 \\ & 4380 \end{aligned}$ | Al-Ṣūfí mentioned that these are of magnitude 5 or 6 | $\begin{aligned} & 4.99 \\ & 4.71 \\ & 5.05 \\ & 5.08 \\ & 4.78 \end{aligned}$ | Al-Ṣūfī mentioned in the written explanation that there is a group of stars that together with the twenty-second star form a circle. These stars were not mentioned by Ptolemy. These stars are all part of Ursa Major. |
| 8 | 43 Ursa Major | 4728 | 5.25 | 5.02 | Al-Ṣūfi mentioned that this star is between the second of the two (stars) outside of the constellation, close to Kabd alAsad and (the star) on the kneebend. It is less than the $5^{\text {th }}$ magnitude. It is much closer to the second (star) that is outside of constellation. This star is now included in constellation CVn. |
| 9 | 44 Ursa Major | 3648 |  | 5.13 | Al-Ṣūfĭ explained that this star together with the seventh and eighth form a triangle and which form together with the ninth and the tenth another open angle (obtuse) triangle. |
| 10-11 | 45 Ursa Major 46 Ursa Major | $\begin{aligned} & 5023 \\ & 5112 \end{aligned}$ | $\begin{aligned} & 6 \\ & 6 \end{aligned}$ | $\begin{aligned} & 5.15 \\ & 4.7 \end{aligned}$ | Al-Ṣūfī explained these two stars (5023 \& 5112) are one dhirā ‘ (2 deg 20 min ) distance |


|  |  |  |  |  | from each other. The actual distance between these two stars is approximately 2 deg 26 min. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 12 | 32 Draco | 6618 | 6 | 5.75 | Al-Șūfì mentioned that in the middle of the 4 stars which are the second, third, fourth, and fifth there is a very faint star which was not mentioned by Ptolemy and which the Arabs call al-Ruba'. |
| 13 | 14 Cepheus | 8591 | 6 | 5.50 | The Arabs call this star Kalb al$R \bar{a} t \bar{\imath}$ (shepherd's dog). <br> Al-Ṣūfi mentioned that this is a faint star located between the left and right leg but closer to the left leg. |
| 14-17 | $15,17,18,19$ Cepheus | $\begin{aligned} & 7701 \\ & 7633 \\ & 7740 \\ & 7955 \end{aligned}$ | Not mentioned | $\begin{aligned} & 5.39 \\ & 4.96 \\ & 4.30 \\ & 4.51 \end{aligned}$ | Al-Sūfí mentioned that the fifth and sixth stars together with other stars form a circle of stars between the constellations of Draco and Cygnus. This circle of stars was called al-Qidr. In the image al-Ṣūfī drew four of these stars with the fifth and sixth which form the circle. |
| 18-21 | $20,21,22,23$ Cepheus | $\begin{aligned} & 8317 \\ & 8468 \\ & 8615 \\ & 8819 \end{aligned}$ | 6(k) or 5(s) | $\begin{aligned} & 4.56 \\ & 4.79 \\ & 5.08 \\ & 4.41 \end{aligned}$ | Al-Sūfi mentioned that there is a line of stars between the second and third stars whose magnitude is either greater than $6^{\text {th }}$ magnitude or less than $5^{\text {th }}$ magnitude. I have tried to identify only a few of these stars. Al-Ṣūfi also mentioned that there are many $5^{\text {th }}$ and $6^{\text {th }}$ magnitude stars on the body and between the legs however these cannot be identified accurately since their location is a little vague. |
| 22-24 | 24,25,26 Bootes | $\begin{aligned} & 5502 \\ & 5544 \\ & 5575 \end{aligned}$ | $\begin{aligned} & 5 \\ & 5 \\ & 6 \end{aligned}$ | $\begin{aligned} & 4.6 \\ & 4.55 \\ & 5.71 \end{aligned}$ | These stars are above the nineteenth star which is on the right heel and they form a triangle. |
| 25-28 | $\begin{aligned} & 27,28,29,30 \\ & \text { Bootes } \end{aligned}$ | $\begin{aligned} & 5370 \\ & 5365 \\ & 5330 \\ & 5159 \end{aligned}$ | $\begin{aligned} & 5 \\ & 5 \\ & 5 \\ & 4 \end{aligned}$ | $\begin{aligned} & 4.86 \\ & 5.41 \\ & 5.29 \\ & 5.36 \end{aligned}$ | Al-Șūfi mentioned that there is a line of stars between the constellation Bootes and Virgo; however he identified the magnitudes of 4 stars: 3 of the $5^{\text {th }}$ magnitude and 1 of the $4^{\text {th }}$ magnitude. |
| 29 | 31 Hercules | 6159 | 6 | 4.84 |  |
| 30-31 | 32,33 Hercules | $\begin{aligned} & 6355 \\ & 6337 \end{aligned}$ | $\begin{aligned} & 6 \\ & 6 \end{aligned}$ | $\begin{array}{r} 4.91 \\ 4.98 \\ \hline \end{array}$ |  |


| 32-36 | 34,35 Hercules | $\begin{aligned} & \hline 6781 \\ & 6685 \\ & 6644 \\ & 6571 \\ & 6480 \\ & \hline \end{aligned}$ | $\begin{array}{\|l} \hline 5(\mathrm{~s}) \text { or } 6 \\ 5(\mathrm{~s}) \text { or } 6 \\ 5(\mathrm{~s}) \text { or } 6 \\ 5(\mathrm{~s}) \text { or } 6 \\ 6(\mathrm{~m}) \\ \hline \end{array}$ | $\begin{aligned} & \hline 5.86 \\ & 5.46 \\ & 5.12 \\ & 5.77 \\ & 5.74 \\ & \hline \end{aligned}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 37 | 36 Hercules | 6677 | 6 | 5.16 |  |
|  | 37,38 Hercules | $\begin{aligned} & 6793 \\ & 6872 \end{aligned}$ | Not mentioned | $\begin{aligned} & 5.48 \\ & 4.33 \end{aligned}$ | Al-Şūfì mentioned that there are many $6^{\text {th }}$ magnitude stars between the eighteenth star of Hercules and the constellation Lyra which were not mentioned by Ptolemy. He also mentioned that there are many $6^{\text {th }}$ magnitude stars between the twenty-fifth star of Hercules and the constellation Draco and one particular star of the $5^{\text {th }}$ magnitude which is closer to the tip of the tongue of Draco; however it was not possible to identify this star with an acceptable degree of accuracy. |
| 38 | 11 Lyra | 7262 | 5 | 5.28 |  |
| 39 | 20 Cygnus | 8146 | 5 | 4.43 | Al-Şūfí mentioned that this star is between the two stars outside of the constellation (the eighteenth and the nineteenth) and the twelfth star. |
| 40-43 | 21,22,23,24 Cygnus | $\begin{aligned} & \hline 7834 \\ & 7942 \\ & 7866 \\ & 7806 \end{aligned}$ | $\begin{aligned} & \hline 4(\mathrm{~s}) \\ & 4(\mathrm{~s}) \\ & 6 \\ & 5 \end{aligned}$ | $\begin{aligned} & 4.01 \\ & 4.22 \\ & 4.61 \\ & 4.43 \end{aligned}$ | Al-Șūfi also mentioned that between these stars and the constellation Sagitta are many stars of the $6^{\text {th }}$ magnitude which were not mentioned by Ptolemy. |
|  |  |  |  |  | Al-Sūfí also mentioned that between the twelfth star and the constellation Delphinus are many stars of the $6^{\text {th }}$ magnitude which were not mentioned by Ptolemy. |
| 44 | 25 Cygnus | 7405 | 5 | 4.44 | Al-Ṣūfì mentioned that this star should have been on the beak and that it is brighter than the star on the head (second star which he mentioned to be 6 magnitude). |
| 45-47 | 14, 15,16 Cassiopia | $\begin{aligned} & \hline 580 \\ & 575 \\ & 548 \end{aligned}$ | $\begin{aligned} & \hline 4 \\ & 4 \\ & 6 \end{aligned}$ | $\begin{aligned} & 3.98 \\ & 4.54 \\ & 4.99 \end{aligned}$ | Al-Ṣūfí mentioned that there are three stars north of the seventh stars; two of the $4^{\text {th }}$ magnitude and one of the $6^{\text {th }}$ magnitudes. He also mentioned that next to these stars are many $6^{\text {th }}$ magnitude stars which were not mentioned by Ptolemy. |


| 48 | 14 Auriga | 1995 | 5 | 4.52 | This forms a double star with the fifth star. Al-Ṣūfī did not mention its magnitude, however he mentioned that the fifth star was of the $5^{\text {th }}$ magnitude while Ptolemy mentioned it to be $4^{\text {th }}$ magnitude. Al-Ṣūfī might have made a mistake here and switched between the two. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 49 | 30 Ophiuchus | 6493 | 5(m) | 4.54 |  |
| 50 | 31 Ophiuchus | 6243 | 5 | 4.65 |  |
| 51 | 32 Ophiuchus | 6770 | 5 or 6 | 4.64 | The double star with the twenty-ninth star of Ophiuchus. Al-Ṣūfì mentioned that it is a small or faint star. |
| 52 | 33 Ophiuchus | 6093 | 6 | 4.83 |  |
| 53 | 34 Ophiuchus | 6524 | 6 | 5.59 |  |
| 54 | 19 Serpens | 5843 | 5 | 5.33 |  |
| 55 | 20 Serpens | 5895 | 5 or 6 | 5.11 | The double star with the eleventh star of the Serpens. AlSuūfi mentioned that it is a small or faint star. |
| 56 | 16 Aquila | $\begin{aligned} & \mathrm{Cr} \\ & 399 \end{aligned}$ |  |  | Al-Ṣūfī identified this Nebula between the ninth star of Aquila and the constellation Sagitta. It is the open cluster Cr 399 which is also called Brocchi's cluster. <br> He mentioned that this nebula contains stars of the $4^{\text {th }}, 5^{\text {th }}$ and $6^{\text {th }}$ magnitude but most are of the $5^{\text {th }}$ magnitude. |
| 57 | 17 Aquila | 7437 | 6 | 5.00 | Al-Ṣūfì mentioned that this star is between the nebula and the constellation Sagitta. |
| 58 | 18 Aquila | 7193 | 4(s) | 4.02 |  |
| 59 | 19 Aquila | 7149 | 6 | 4.83 |  |
| 60 | 20 Aquila | 7063 | 5 | 4.22 |  |
| 61 | 21 Aquila | 7032 | 5 | 4.90 |  |
| 62 | 22 Aquila | 7020 | 5 | 4.72 |  |
| 63 | 23 Aquila | 6973 | 4(m) | 3.85 |  |
| 64 | 24 Aquila | 7007 | 6 | 5.84 |  |
| 65 | 5 Triangulum | 655 | 6 | 5.28 | Double star with the fourth star of Triangulum. |

Table 10: Zodiac Stars mentioned by al-Ṣūfĩ but not by Ptolemy.

| Number | Star number <br> (as per al-Șūfī) | Star/s <br> (HR) | Al-Ṣūfī <br> Magnitude | Modern <br> Magnitude | Explanations and Comments |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 19 Aries | 1005 | 4 | 5.28 | Al-Ṣūfĭ did not exactly specify <br> a magnitude; however, he <br> mentioned that this star is |


|  |  |  |  |  | similar to the tenth star which he stated as $4^{\text {th }}$ magnitude. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 2-3 | 20 Aries <br> 21 Aries | $\begin{aligned} & \hline 569 \\ & 623 \end{aligned}$ | $\begin{aligned} & 4(\mathrm{~s})=4.25 \\ & 5(\mathrm{~s})=5.25 \end{aligned}$ | $\begin{aligned} & \hline 4.79 \\ & 4.98 \end{aligned}$ | Al-Șūfī mentions that these two stars are similar in magnitude to the two stars on the muzzle, which are 4(s) and 5(s). |
| 4 | 22 Aries | 613 | 6 | 5.03 | Al-Süfī mentioned that this star is close to the star al-Nātih (which is the fourteenth star of Aries). |
| 5 | 44 Taurus | 1153 | 6 | 5.35 |  |
| 6 | 45 Taurus | 1159 | 6 | 5.91 |  |
| 7 | 46 Taurus | 1268 | 5 | 5.20 |  |
| 8 | 47 Taurus | 1990 | $5(\mathrm{~s})=5.25$ | 5.49 |  |
| 9 | 48 Taurus | 1253 | 6 | 5.33 |  |
| 10 | 49 Taurus | 1381 | 6 | 5.12 |  |
| 11 | 50 Taurus | 1389 | $6(\mathrm{~m})=5.5$ | 4.29 |  |
| 12 | 51 Taurus | 1427 | $5(\mathrm{~s})=5.25$ | 4.78 |  |
| 13 | 52 Taurus | 1394 | 6 | 4.49 |  |
| 14 | 53 Taurus | 1356 | 6 | 5.26 |  |
| 15 | 54 Taurus | 1149 | Not mentioned | 3.87 | Additional stars of the Pleiades. |
| 16 | 55 Taurus | 1165 | Not mentioned | 2.87 | Additional stars of the Pleiades. |
| 17 | 56 Taurus | 1142 | Not mentioned | 3.70 | Additional stars of the Pleiades. |
| 18 | 26 Gemini | 2852 | 5 | 4.18 |  |
| 19 | 27 Gemini | 2973 | 5 | 4.28 |  |
| 20-22 | 28 Gemini <br> 29 Gemini <br> 30 Gemini | $\begin{aligned} & 2456 \\ & 2503 \\ & 2506 \end{aligned}$ | $\begin{array}{\|l\|} \hline 5 \\ 5 \\ 5 \\ \hline \end{array}$ | $\begin{aligned} & 4.66 \\ & 4.77 \\ & 4.47 \end{aligned}$ | Al-Sūfī mentioned that these three stars form an arc which is between the constellation Orion and the asterism al-Han'a (the $6^{\text {th }}$ lunar mansion) |
| 23 | 33 Virgo | 5044 | Not mentioned | 5.37 | Double star with HR 5019. |
| 24 | 34 Virgo | 4824 | 6 | 6.19 | Next to the eleventh star HR4828. |
| 25 | 18 Libra | 5824 | 6 | 4.96 |  |
| 26 | 25 Scorpio | 6143 | 6 | 4.23 |  |
| 27 | 26 Scorpio | 6166 | 6 | 4.16 |  |
| 28 | 27 Scorpio | 6081 | $5(\mathrm{~s})=5.25$ | 4.55 |  |
| 29 | 28 Scorpio | 6141 | $5(\mathrm{~s})=5.25$ | 4.79 |  |
| 30 | 29 Scorpio | 5885 | 6 | 4.64 |  |
| 31 | 30 Scorpio | 5904 | 6 | 4.59 |  |
| 32 | 32 Sagittarius | 7120 | Not mentioned | 5.00 | Double star with 8 Sagittarius HR7116. |
| 33 | 33 Sagittarius | 7337 | Not mentioned | 4.01 | Double star with 23 Sagittarius (HR7343). |
| 34 | 34 Sagittarius | - | 3 | - | Al-Şūfì mentioned that there is a $3^{\text {rd }}$ magnitude star between 23 Sagittarius and the constellation Piscis Australis; however the location was not precise enough |


|  |  |  |  |  | to locate this star. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 35 | 46 Aquarius | 7845 | 5 | 5.65 |  |
| 36 | 47 Aquarius | 8496 | 6 | 5.34 |  |
| 37 | 48 Aquarius | 8590 | Not mentioned | 5.89 | Al-Sūfī mentioned that this star is between 12 Aquarius and 23 Aquarius |
| 38 | 49 Aquarius | 8890 | 6 | 5.20 | Al-Șūfī mentioned that this star is north of 30 Aquarius |
| 39 | 50 Aquarius | 8987 | 6 | 5.28 | Double star with 31 Aquarius (HR8968) |
| 40 | 39 Pisces | 389 | 5 | 5.23 |  |
| 41 | 39 Pisces | 274 | 5 | 5.42 |  |

Table 11: Southern Stars mentioned by al-Ṣūfī but not by Ptolemy.

| Number | Star number (as per al-Ṣūfī) | Star/s (HR) | al-Ṣūfī <br> Magnitude | Modern Magnitude | Explanations and Comments |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 23 Cetus | 775 | 5 | 6.21 | Between 3 and 5 Cetus. |
| 2 | 24 Cetus | 531 | 5 | 4.67 | Close to 14 Cetus. |
| 3 | 25 Cetus | 583 | 5 | 5.41 | South of 13 Cetus. |
| 4 | 26 Cetus | 329 | 6 | 5.82 | Double star with 16 Cetus (HR 334). |
| 5 | 39 Orion | 2130 |  | 5.14 | Double star with 12 Orion (HR 2135). |
| 6 | 40 Orion | 1931 | 4 | 3.81 |  |
| 7 | 35 Eridanus | 917 | 5 | 5.32 | Double star with 15 Eridanus (HR925). |
| 8 | 36 Eridanus | 994 | 4 | 4.88 | Double star with 21 Eridanus (HR1003). |
| 9 | 37 Eridanus | 794 | 4 | 4.11 |  |
| 10 | 38 Eridanus | 789 | 5 | 4.75 |  |
| 11 | 39 Eridanus | 1008 | 4 | 4.27 |  |
| 12 | 40 Eridanus | 963 | $3(\mathrm{~s})=3.25$ | 3.87 |  |
| 13 | 46 Argo | 3307 | $3(\mathrm{~s})=3.25$ | 1.86 |  |
| 14 | 47 Argo | 2787 | Not mentioned | 4.66 | Double star with 12 Argo (HR2773). |
| 15 | 48 Argo | 3037 | Not mentioned | 5.23 | Double star with 34 Argo (HR3055). |
| 16 | 49 Argo | $\begin{aligned} & \hline \mathrm{NGC2} \\ & 669 \\ & \mathrm{IC} \\ & 2391 \end{aligned}$ |  |  | Al-Ṣūfī mentioned that next to 37 Argo is a nebula. He is probably referring to NGC2669. |
| 17 | 28 Hydra | 3492 | 5 | 4.36 | Double star with 3 Hydra (HR3482). |
| 18 | 29 Hydra | 3709 | 5 | 4.80 |  |
| 19 | 30 Hydra | 3706 | 5 | 4.79 |  |
| 20 | 31 Hydra | 3636 | 6 | 5.77 |  |
| 21 | 38 Centaurus | 4933 |  | 4.27 | Double star with 22 Centaurus. |
| 22 | 20 Lupus | 5457 | 6 | 6.07 | Close to 2 Lupus. |
| 23 | 21 Lupus | 5494 | 6 | 5.74 | Close to 2 Lupus. |
| 24 | 8 Ara | 6897 | 4 | 3.51 | Double star with HR6934. |
| 25 | 9 Ara | 6934 | 6 | 4.96 |  |


| 26 | 10 Ara | 6905 | 5 | 4.13 |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 27 | 14 Corona <br> Australis | 6938 | 5 | 5.07 |  |
| 28 | 12 Piscis <br> Austrinus | 8447 | Not <br> mentioned | 4.92 | Double star with 6 Piscis <br> Austrinus (HR8431). |

### 5.6 Color of Stars in al-Ṣūfí’s Book

The color of the stars was never an important topic for ancient observers of the sky. There are very few ancient records on this subject or in ancient star catalogs. 'Red' was the color that attracted the most attention whilst the other colors such as 'white' or 'blue' were rarely mentioned. Ptolemy gave the color red to six stars in his catalog. These stars were Aldebaran, Arcturus, Betelgeuse, Pollux, Antares and strangely enough Sirius. One of the first Arab and Islamic authors to mention the color of the stars was al-Farghān̄̄. In his discussion of Ptolemy's book al-Farghānī mentioned only the color of three red stars, Antares, Pollux, and Aldebaran. On the other hand al-Battānī did not attribute any color to any of the stars in his star catalog whereas Ulugh Bēg mentioned the color of four red stars, Antares, Pollux, Betelgeuse and Aldebaran but neglected Arcturus and Alpha Hydrae. The Alfonsine authors do not mention any remarks on the color of stars except the red color of Antares (Qalb al'Aqrab) (Samso\&Comes, 1988). By the time we reach the catalog of Tycho Brahe we find that it only mentions the color of Antares: as ruby red.

In the 'Book of the Fixed Stars' al-Ṣūfi described seven stars with red color in particular. These stars were Aldebaran, Arcturus, Betelgeuse, Pollux, Alpha Hydrae, Algol and Antares. However al-Ṣūfì stays silent about the color of Sirius. He only describes it as a bright star on the mouth called al-Kalb (Dog). I have tried to give in the table below (Table 12) a brief summary on each of these eight stars along with what al-Ṣūfì mentioned about them. These stars were sometimes mentioned in the tables and other times in his comments on the constellations:

Table 12: Color of the stars according to al-Ṣūfì.

| Number | Modern Star name \& (HR) \& Color Index | Star Numbers according to al-Ṣūfī | Description according to al-Ṣūfī |
| :---: | :---: | :---: | :---: |
| 1 | Aldebaran <br> HR1457 $B-V=1.54$ | 14 Taurus | From the table: <br> The bright star, the reddish one of the letter ( $\Delta$ ) al-D $\bar{a} l$ on the southern eye and it is al-Dabarān. <br> From the comments: <br> The fourteenth is the large bright red (star) on the south edge of the stars that resemble al-D $\bar{a} l$. It is located on the south eye and is drawn on al-Īsterlāb (the Astrolabe). It is called al-Dabarān and 'Ayn al-Thawr (the eye of Taurus) and is of |


|  |  |  | the $1^{\text {st }}$ magnitude. |
| :---: | :---: | :---: | :---: |
| 2 | Arcturus <br> HR5340 <br> $B-V=1.23$ | 23 Bootes | From the table: <br> The star between the thighs called al-Simāk al-Rāmih. <br> From the comments: <br> As for the one outside the constellation image it is the bright red star between the thighs. It is of the $1^{\text {st }}$ magnitude and it is drawn on the al-Īsterlāb (Astrolabe). It is called al-Simāk alRāmih. |
| 3 | Betelgeuse <br> HR2061 <br> $B-V=1.84$ | 2 Orion | From the table: <br> The bright reddish star on the right shoulder. <br> From the comments: <br> The second is the great bright red star located on the right Mankib (shoulder). It is less than the $1^{\text {st }}$ magnitude. The distance between it and the three stars on the head is three Thira. It is (one of the stars that are) drawn on an Astrolabe. It is called Mankib al-Jauz $\vec{a}^{\prime}$ (the shoulder of Orion) and also Yad al-Jauzā' (the hand of Orion). |
| 4 | Pollux <br> HR2990 <br> $B-V=1.00$ | 2 Gemini | From the table: <br> The reddish star on the head of the rear twin. <br> From the comments: <br> The second (star) follows the first on the head of the rear twin. It is a little south (of the first) with a distance of more than 2 dhirā' between them. It is also of the $2^{\text {nd }}$ magnitude. |
| 5 | Alpha Hydrae <br> HR3748 <br> $B-V=1.45$ | 12 Hydra | From the table: <br> The bright one of these two close stars called al-Fard. <br> From the comments: <br> The twelfth star is the bright red star at the end of the neck and at the beginning of the back. It is of the $2^{\text {nd }}$ magnitude. It is drawn on the al-İsterläb (Astrolabe). It is called 'Unuk alShujā ' (the Neck of Hydra). It is also called al-Fard. |
| 6 | Algol <br> HR936 <br> $\mathrm{B}-\mathrm{V}=$ <br> -0.05 | 12 Perseus | From the table: stars in the Gorgon's head: the bright one. <br> From the comments: <br> The twelfth star is the bright red star less than $2^{\text {nd }}$ magnitude. Ptolemy mentioned it is exactly of the $2^{\text {nd }}$ magnitude. It is on the gorgon's head. It is further than the eleventh star by two Thira. It is drawn on the Astrolabe. It is called Rae's al-Ghūl (Gorgon's Head). |
| 7 | Antares <br> HR6134 <br> $B-V=1.84$ | 8 Scorpio | From the table: <br> The middle one of these which is reddish and called Qalb al'Aqrab (Antares). <br> From the comments: <br> The eighth is the bright red (star) that is close to the seventh. |


|  |  |  | It is of the $2^{\text {nd }}$ magnitude. It is (one of the stars that are) drawn on an Astrolabe. It is called Qalb al- 'Aqrab (the heart of Scorpio). It is the eighteenth of the lunar mansions. |
| :---: | :---: | :---: | :---: |
| 8 | Sirius <br> HR2491 $B-V=0.00$ | 1-anis Major | From the table: <br> The star in the mouth, the brightest, which is called al-Kalb (Dog) and al-Shi'ra al-Yamāniya and al-'Abūr. <br> From the comments: <br> The first star is the great bright star on the mouth. It is drawn on the Astrolabe. It is called al-Yamāniya. |

The color index is a numerical expression that determines the color of a stellar object and thus its temperature. These indices are measured by determining the magnitude of an object using different kinds of filters; the U filter which transmits ultraviolet rays, the B filter which transmits blue light, and the V filter visible (green-yellow) light. The difference in magnitudes found with these filters is called the U-B or B-V color index. The smaller the color index, the bluer (or hotter) the object is. Conversely, the larger the color index, the redder (or cooler) the object is. Starting from the least red color (B-V) index of 1.0 for the star Pollux to the high color index of 1.84 for both the stars Betelgeuse and Antares, the above color indices are an obvious evidence for the reliability of the data for most of these stars except when it comes to the two stars Sirius and Algol. The Sirius problem and consequent debate will be discussed in depth in the section below. As for the color of Algol, it is surprising for an acute observer such as al-Ṣūfi to assign the red color to this star. The star Algol is a short period close binary eclipsing system that changes magnitude from maximum 2.12 to minimum 3.39 in few days and the color index scarcely varies. al-Șūfĭ considered this star to be a bright star with less than $2^{\text {nd }}$ magnitude (2.25) while Ptolemy assigned it the $2^{\text {nd }}$ magnitude. Therefore the nature of the variability of this star is not a reason which explains the error of assigning the red color to this star. The only other explanation is that al-Ṣüfĩ was mistaken in this regard. A similar mistake was also made by Julius Schmidt who was the Director of Athens Observatory. He also observed Algol to be 'reddish yellow' in 1841 (Ceragioli, 1995).

### 5.6.1 The Debate on Color of the Sirius

A puzzling question in the history of astronomy concerning the star Sirius is whether this star changed color in the last 2000 years. For a long time in the past there used to be confusion on
the actual color of Sirius. Ptolemy and many other Greek and Latin astronomers mentioned that the color of Sirius is red. Ptolemy described this star as "...the star in the mouth and is the brightest and is reddish in color." More than 1000 years later al-Ṣūfī stopped from attributing any color to Sirius, even though he mentioned the colors for other stars. It is a very well known fact today that the color of Sirius is bright white. So the question arises why there is such a difference in what the Greeks said about this star and what al-Sūfī wrote and what we know as a fact today? Has there been a change in the color of this star in the lat two millennia and why?

The first and most obvious answer to this problem is that Ptolemy might have made an error in assigning the color red to this star. Another answer is that during the course of history there might have been some errors in copying the ancient manuscripts which we know of today especially the Almagest. The reason for this is that Ptolemy does not mention the red Sirius in his astrological treatise, the Tetrabiblos. Therefore, during the course of history many Arabic, Islamic and Western astronomers might have overlooked this matter for these reasons. However such a description of a major star could not be easily disregarded especially since there were many other ancient Greek and Latin philosophers, poets and astronomers who corroborate Ptolemy by calling Sirius "Reddish" such as Aratus ( $3^{\text {th }}$ century B.C.), Cicero ( $1^{\text {st }}$ century B.C.), Horace ( $1^{\text {st }}$ century B.C.), and Seneca ( $1^{\text {st }}$ century A.D.). This fact was also enforced by an Assyrian cuneiform tablet which mentioned this star as "...reddishwhite like molten copper..." (Rietschi, 1995).

According to Aristotelian philosophy the heavens or the 'Cosmos' was a physically unchanging order. This physical concept was the dominant view to which most scholars, philosophers and astronomers adhered to through out the Middle Ages. Therefore, the idea of Sirius changing color was not considered until the time of Tycho and Kepler. The Sirius debate seriously began in the eighteenth century with the study of variable stars. In 1790 Thomas Baker published a short article in the Philosophical Transaction of the Royal Society in favor of Sirius being red. The first physical mechanism for the redness of Sirius was proposed in 1839 by John Herschel. In his study of variable stars he mentioned that a 'cosmic' cloud might be an explanation for this phenomenon. However, in the nineteenth century with the development of the first theories of stellar evolution the idea of a red star changing color was dismissed. This argument was further confirmed by studies of ancient manuscripts especially with the publication in 1874 of Schjellerup's translation of al-Ṣūfi’s Book of the Fixed Star. In his introduction to this translation Schjellerup discredited the evidence of Sirius being red and he attributed Ptolemy's remarks of a red Sirius to errors in copying and translating the Almagest. In 1882 yet another reason was added to this debate by
W.T. Lynn, which was the effect of atmosphere condition on observation. He explained that Sirius is the only bright star which can actually be seen at sunset or sunrise from the horizon and Ptolemy might have been referring to an observation of this star at this time close to the horizon when it could appear to be red due to the effect of the atmosphere.

The counter attack to these arguments did not take a very long time to happen. In 1892 a controversial astronomer by the name of T.J.J. See published a series of articles in the Astronomy and Astrophysical Journal in favor of the redness of Sirius. He also disregarded the atmospheric effect, since Ptolemy made his observations from Egypt where the atmosphere is usually clear at night and the fact that Ptolemy could not have made such a mistake on this most important of stars (See, 1927). However, See’s historical arrangements were not favorably received by the scientific community-mainly due to See's personality as well as the scientific nature of this subject. By this time most astronomers preferred to endorse the astronomical facts, which have been achieved up to that date. These attacks have been spearheaded by astronomers such as Schiaparelli and Newcomb and continued in a series of articles between See and Schiaparelli until 1930's. This debate later died down with most astronomers favoring the idea of atmospheric effects rather then a star changing color.

In the mid-twentieth century the debate started again with the ever-emerging theories of binary star evolution. By this time Sirius was known to be a binary system composed of Sirius-A which is a 2.25 solar-mass main-sequence star and Sirius-B which is a 1.05 solarmass white dwarf. Research also indicated that this system is surrounded by dust. Several astronomers tried to explain the redness of Sirius by several astrophysical mechanisms such as mass loss through solar wind, nova ejection, supernova explosions, interstellar dust absorption as well as a thermonuclear runaway (Holberg, 2007). However, none of these astrophysical explanations stood scientific ground and accurately explained the redness of Sirius. When we turn to records of ancient China the color of Sirius is described as white. Early details of this can be found in Edouard Chavannes (1898) translation of Sima Qian historical (Shiji) records compiled around B.C. 100 (Rietschi, 1995).

The Sirius debate will probably continue in the future until a reasonably accurate explanation is achieved. The study of variable stars is a fairly young science with abundant data available for only the past 100 years. The study of color change and long term variability of stars can only be made if what has been written about these stars is properly authenticated. The main ancient data which are available to researchers are to be found in the old star catalogs such as those produced by Ptolemy's and al-Șūfi's. Therefore, once the stellar identification and comparisons are made, it is possible to identify some of the reasons for
change in the magnitudes and star colors. The final results from al-Ṣūfís data will hopefully be better used in the field of applied historical astronomy such as the changing of star magnitudes, proper motion, or variable star analysis and will hopefully open new doors of investigations in these fields.

### 5.7 Stars Used on the Astrolabe in al-Ṣūfī's Book

The Astrolabe is an ancient analog calculator capable of working out several different kinds of problems in spherical astronomy. It was used for solving problems relating to the time and position of the Sun and stars in the sky. The astrolabe is thought to be a Greek invention. The stereographic projection was probably known by Hipparchus as early as B.C. 150. The oldest available treatise about stereographic projection and the astrolabe was the Planispherium, which was written by Ptolemy (Evans, 1998). However Ptolemy's astrolabe was a simple instrument, which was used as a star finder and not as an observational instrument for measuring the altitude of stars. It did not include many of the features found in later instruments (Webster, Roderick \& Marjorie, 1998).

In his al-Fahras, al-Nadīm reported that the first person credited with constructing an Isterlāb (astrolabe) in the Islamic world was the eighth century mathematician and astronomer Muḥammad al-Fazārī. In A.D. 856 al-Faraghānī wrote one of the first detailed descriptions on this instrument (Lorch, 2005). By the $9^{\text {th }}$ century the astrolabe was very much in use in the Arabic and Islamic world. It was later introduced to Europe from Islamic Spain (Andalusia) in the early $12^{\text {th }}$ century. It was also introduced to China from the Islamic world in the $13^{\text {th }}$ century (Webster, Roderick \& Marjorie, 1998). Several types of astrolabes in the Arab and Islamic world were made. The most popular type was the planispheric astrolabe, on which the celestial sphere is projected onto the plane of the equator. Other types include the spherical astrolabe, Azarquil (al-Zarqālī) astrolabe and the mariner astrolabe which was a crude instrument used in navigation. The astrolabe was very much developed in the Arab and Islamic world and was extensively used as an astronomical instrument. Most of the astrolabes constructed in that period were made of brass and were about $10-15 \mathrm{~cm}$ in diameter. There are more than 600 surviving Arabic and Islamic astrolabes, the oldest are from the $9^{\text {th }}$ and $10^{\text {th }}$ centuries (King, 2005).

An astrolabe consists of a hollow disk (called mater) which holds one or more flat plates (called climates). Each plate is specially made for a specific latitude. They are engraved with a stereographic projection of circular lines which represent the celestial sphere. The disk also holds another frame or net called a spider (also called rete- in Arabic al- 'Ankabūt) which is free to rotate on top of the flat plates. This frame or spider which acts as a star map is a projection of the ecliptic plane with pointers or indicators pointing to the position of the brightest stars in the sky. The early astrolabes included no more than 20 stars of the $1^{\text {st }}$ and $2^{\text {nd }}$ magnitudes. The earliest extant eastern astrolabe dated A.D. 927 contained only 17 stars,
however later astrolabes had more than sixty stars positioned on the rete. The back of the disk (mater) includes a number of trigonometric scales which are used in various astronomical, timekeeping and other applications. The final piece of the astrolabe is a movable rectangular rod (alidade- in Arabic al-'Iḍadah) attached to the back face of the instrument. When the astrolabe is held vertically, the alidade can be rotated and a star sighted along its length, so that the star's altitude in degrees can be read from the graduated edge of the astrolabe. To use an astrolabe, you adjust the moveable components to a specific date and time. Once set, the entire sky, both visible and invisible, is represented on the face of the instrument. This allows a great many astronomical problems to be solved in a very visual way. Figure 41 shows the parts of the astrolabe with the spider at the top of the image.


Figure 41

Al-Ṣūfī wrote extensively on the construction and use of the astrolabe (see biography section). In one of his treatises al-Ṣūfī described more than 1000 different uses for an astrolabe in fields such as astronomy, astrology, timekeeping, navigation, construction and surveying. Kunitzsch mentioned that in several of the al-Ṣūfi’s works he identified as many as 55 stars which could be used on the astrolabe spider. Al-Ṣūfi's Book of the Fixed Stars, which included 44 of these stars, was the best and most accurate of al-Ṣūfís works (Kunitzsch, 1990). This was one of the main reference to which many later astronomers and instrument makers used to identify the stars of the astrolabe.

However al-Ṣūfi did not make a list of the astrolabe stars but rather the information on these stars were scattered throughout the various sections of al-Ṣūfís book. Therefore I have tried to identify below (Table 13) all the astrolabe stars found in al-Ṣūfi's book. I also included a brief summary on every one of these stars as they were mentioned by al-Ṣūfi. This summary included all the descriptions both from the tables as well as from the comments in the constellation chapters which mentioned these stars according to al-Ṣūfi. As can be seen from the various comments below, al-Ṣūfì very clearly indicated which stars were to be used on this instrument. He also indicated the various known names and the magnitudes either in the tables or in the comments. Al-Ṣūfī also mentioned 5 stars which were used on the southern astrolabes. Southern astrolabes were probably those instruments which were constructed and used by people living in the Southern Hemisphere.

Table 13: Stars used on the astrolabe in al-Ṣūfí's book.

| Num | Modern star name $+(\mathrm{HR})$ | Numbers according to al-Ṣūfī | Magnitude According to al-Ṣūfī | Names and Description according to al-Ṣūfī |
| :---: | :---: | :---: | :---: | :---: |
| 1 | Arcturus <br> HR5340 | 23 Bootes | 1 | al-Simāk al-Rāmih <br> From the table: <br> The star between the thighs called al-Simāk alRāmiḥ. <br> From the comments: <br> As for the one outside the constellation image it is the bright red star between the thighs. It is of the $1^{\text {st }}$ magnitude and it is drawn on the astrolabe. It is called al-Simāk al-Rāmiḥ. |
| 2 | HR5793 | 1 Corona Borealis | 2 | al-Munīr Min al-Fakka <br> From the table: <br> The bright star in the crown. <br> From the comments: |


|  |  |  |  | The first star is the bright one of the $2^{\text {nd }}$ magnitude. It is used on the astrolabe and is called al-Munīr Min al-Fakka. |
| :---: | :---: | :---: | :---: | :---: |
| 3 | HR6406 | 1 Hercules | $3(\mathrm{~s})=3.25$ | Rae's al-Jāthī <br> From the table: <br> The star on the head. <br> From the comments: <br> The first star is the one on the head. It is in advance of the bright star on the head of alHawwa (constellation Ophiuchus). It is less than $3^{\text {rd }}$ magnitude. Ptolemy mentioned it is exactly of the $3^{\text {rd }}$ magnitude. It is incorrect to consider the magnitude of this star the same as the star on the head of al-Hawwā. It is drawn on the astrolabe and called Rae's al-Jāthī. |
| 4 | $\begin{array}{\|l} \hline \text { Vega } \\ \text { HR } 7001 \end{array}$ | 1 Lyra | 1 | al-Nasr al-Wāqi' <br> From the table: <br> The bright star on the shell called Lyra called alNasr al-Wäqi'. <br> From the comments: <br> The first one is the famous bright star of the $1^{\text {st }}$ magnitude which is drawn on the astrolabe. It is called al-Nasr al-Wāqi'. |
| 5 | HR7417 | 1 Cygnus | $3(\mathrm{~s})=3.25$ | Minqār al-Dajāja <br> From the table: <br> The star on the beak. <br> From the comments: <br> The first of the constellation al-Ta'er (Cygnus) is the bright star on the beak behind the constellation of al-Nasr al-Wāqi'. Ptolemy mentioned it is exactly of the $3^{\text {rd }}$ magnitude; however, it is less than $3^{\text {rd }}$ magnitude. It is drawn on the astrolabe and called Minqār al-Dajāja. |
| 6 | $\begin{aligned} & \hline \text { Deneb } \\ & \text { HR7924 } \end{aligned}$ | 5 Cygnus | 2 | Dhanab al-Dajāja <br> From the table: <br> The bright star in the tail. <br> From the comments: <br> The fifth star is the bright one on the tail. It is of the $2^{\text {nd }}$ magnitude. It is drawn on the astrolabe and is called Dhanab al-Dajāja. |
| 7 | HR12 | $12$ <br> Cassiopeia | 3 | al-Kaff al-Khaḍīb <br> Sinām al-Nāqa <br> From the table: <br> The star on the middle of the back of the throne |


|  |  |  |  | called al-Kaff al-Khadīb. <br> From the comments: <br> The twelfth star is the one on the middle of the back of the throne. It is drawn on the astrolabe. It is called al-Kaff al-Khadīb and Sinām al-Nāqa. |
| :---: | :---: | :---: | :---: | :---: |
| 8 | HR 1017 | 7 Perseus | 2 | Janb Barshāūsh <br> From the table: <br> The bright star in the right side. <br> From the comments: <br> The seventh is the bright star on the right side next to the sixth star. It is also outside of the galaxy touching its western edge. It almost forms a straight line with the sixth and fourth stars. It is of the $2^{\text {nd }}$ magnitude. It is drawn on the astrolabe and called Janb barshāūsh. |
| 9 | $\begin{aligned} & \hline \text { Algol } \\ & \text { HR936 } \end{aligned}$ | 12 Perseus | 2 | Ra's al-Ghūl <br> From the table: <br> The stars in the gorgon head: the bright one. <br> From the comments: <br> The twelfth star is the bright red star less than $2^{\text {nd }}$ magnitude. Ptolemy mentioned it is exactly of the $2^{\text {nd }}$ magnitude. It is on the gorgon's head. It is distant from the eleventh star by two Thira. It is drawn on the astrolabe. It is called Ra's al-Ghūl (Gorgon's Head). |
| 10 | Capella <br> HR1708 | 3 Auriga | 1 | al- 'Ayyūq <br> From the table: <br> The star on the left shoulder called al- 'Ayyūq <br> From the comments: <br> The third is the very bright star on its left shoulder. It is on the southern edge of the galaxy. It is of the $1^{\text {st }}$ magnitude. It is drawn on the astrolabe and called al-'Ayy $\bar{u} q$. |
| 11 | HR 6556 | 1 Ophiuchus | 3 | Ra's al-Hawwā <br> From the table: <br> The star on the head. <br> From the comments: <br> The first of its stars is the one on the head in front of al-Nasraīn (the two eagles). Together they form an isosceles triangle with this star on the top and al- Nasraīn its base. It is drawn on the astrolabe and called Ra's al-Hawwā. |
| 12 | HR5854 | 9 Serpens | 3 | 'Unuq al-Hayya <br> From the table: |


|  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| 13 | Altair | 3 Aquila | The middle one of the three. <br> From the comments: <br> The ninth star is the one drawn on the astrolabe <br> and called 'Unuq al-Hayya. |  |
| al-Nasr al-Tāir |  |  |  |  |
| From the table: |  |  |  |  |
| The bright star on the place between the shoulders |  |  |  |  |
| called al-Nasr al-Tāir. |  |  |  |  |
| From the comments: |  |  |  |  |
| The third star is the famous bright one which is |  |  |  |  |
| drawn on the astrolabe. It is called al-Nasr al- |  |  |  |  |
| Täir. It is much greater than the 2 |  |  |  |  |


|  |  |  |  |
| :--- | :--- | :--- | :--- |


|  |  |  |  | From the comments: <br> The fifteenth star is the bright one on the left foot. It is of the $3^{\text {rd }}$ magnitude. It is drawn on the astrolabe and is called Rijl al-Musalsala. |
| :---: | :---: | :---: | :---: | :---: |
| 22 | HR544 | 1 Triangulum | 3 | Ra's al-Muthallath <br> From the table: <br> The star in the apex of the triangle. <br> From the comments: <br> The first of its stars is one on the apex of the triangle. It is of the $3^{\text {rd }}$ magnitude. It is drawn on the astrolabe and is called Ra's al-Muthallath. |
| 23 | HR617 | 14 Aries | $3(\mathrm{k})=2.5$ | al-Nätih <br> From the table: <br> The star over the head, which Hipparchus calls "the one on the muzzle". <br> From the comments: <br> As for the stars outside of the constellation the first is the bright star north of the two stars on the horn. It is greater then $3^{\text {rd }}$ magnitude. The distance between it and the northernmost of its stars is a distance of two Thira. It is drawn on the astrolabe and is called al-Nätih. |
| 24 | Aldebaran <br> HR1457 | 1 Taurus | 1 | al-Dabarān <br> From the table: <br> The bright star: the reddish one of the letter $(\Delta)$ $a l-D \bar{a} l$ on the southern eye and it is al-Dabarān. <br> From the comments: <br> The fourteenth is the large bright red (star) on the south edge of the stars that resemble al-Dāl. It is located on the south eye and is drawn on the astrolabe. It is called al-Dabarān and 'Ain alThawr (the eye of Taurus) and is of the $1^{\text {st }}$ magnitude. |
| 25 | $\begin{aligned} & \hline \text { Pollux } \\ & \text { HR2990 } \end{aligned}$ | 2 Gemini | 2 | Ra's al-Taw'am <br> From the table: <br> The reddish star on the head of the rear twin. <br> From the comments: <br> The second (star) follows the first on the head of the rear twin. It is a little south (of the first) with a distance of more than 2 Thira between them. It is also of the $2^{\text {nd }}$ magnitude. |
| 26 | Regulus <br> HR3982 | 8 Leo | 1 | Qalb al-Asad <br> al-Malikī <br> From the table: <br> The star on the heart, called al-Malikī and Qalb |


|  |  |  |  |
| :--- | :--- | :--- | :--- |


|  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| 31 | HR 7343 |  |  |  |


|  |  |  |  | From the comments: <br> The twenty-first is drawn on the astrolabe and is called Dhanab Qītus. |
| :---: | :---: | :---: | :---: | :---: |
| 36 | Betelgeuse <br> HR2061 | 2 Orion | 1 | Mankib al-Jauzā ' <br> Yad al-Jauzá <br> From the table: <br> The bright reddish star on the right shoulder. <br> From the` comments: <br> The second is the great bright red star located on the right Mankib (shoulder). It is less than the $1^{\text {st }}$ magnitude. The distance between it and the three stars on the head is three Thira. It is (one of the stars that are) drawn on an astrolabe. It is called Mankib al-Jauzā' (the shoulder of Orion) and also Yad al-Jauz $\bar{a}$ ' (the hand of Orion). |
| 37 | Rigel <br> HR1713 | 35 Orion | 1 | Rijl al-Jauzā' (the leg of Orion). <br> From the table: <br> The bright star in the left foot, which is (applied in) common to the water (of Eridanus). <br> From the comments: <br> The thirty-fifth is the large bright star on the left leg. It is of the $1^{\text {st }}$ magnitude. It is (one of the stars that are) drawn on an astrolabe. It is called Rijl alJauz $\bar{a}$ ' (the leg of Orion). |
| 38 | HR897 | 34 Eridanus | 1 | Ākhir al-Nahr <br> From the table: <br> The last star of the river, the bright one. <br> From the comments: <br> The thirty-fourth is in front of these three close stars. The distance between it and the closest of these three stars is four Thira. It is of the $1^{\text {st }}$ magnitude. It is drawn on the southern astrolabes and is called $\bar{A} k h i r ~ a l-N a h r . ~$ |
| 39 | Sirius <br> HR2491 | 1 Canis Major | 1 | ```al-Shi'ra al-Yamāniya al- 'Ayyūq al-Kalb``` <br> From the table: <br> The star in the mouth, the brightest, which is called al-Kalb (Dog) and al-Shi'ra al-Yamāniya and al-'Ayyūq. <br> From the comments: <br> The first star is the great bright star on the mouth. It is drawn on the astrolabe. It is called alYamāniya. |
| 40 | Procyon | 2 Canis <br> Minor | 1 | al-Shi'ra al-Shāmīya <br> al-Shi'ra al-Ghumaisa |
|  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
|  |  |  | The star on the end of the right front leg. <br> From the comments: <br> As for the thirty-fifth it is the rearmost of the two. <br> It is of the $1^{\text {st }}$ magnitude. It is located on the tip of <br> the right hand of the animal. It is drawn on the <br> southern astrolabes. It is called Rijl Qantūris (leg <br> of Centaurus). It is very close to the horizon. Its <br> height in all localities is less than (the star) Suhail. |
| :--- | :--- | :--- | :--- | :--- |

### 5.8 Double Stars in al-Ṣūfī’s Book

The word Muḍ'af was used many times in al-Ṣūfî's book to mean double star. For example in the constellation Orion, al-Ṣūfī wrote: "The twelfth star is to the rear of the two. It is less than the $5^{\text {th }}$ magnitude. Ptolemy mentioned that it is exactly $5^{\text {th }}$ magnitude. It is a Mud'af (double star) because there is a star next to it." In many cases al-Ṣūfī only mentioned the presence of a double star but in other cases he describes the location and the magnitude of these double stars. For example in the constellation Ara he wrote: "Behind the second star is another star also of the $4^{\text {th }}$ magnitude. The distance between them is one third of a Thira. It was not mentioned by Ptolemy. This star is a double star because next to it is a star of the $6^{\text {th }}$ magnitude which makes it a double". It is not clear whether these stars are actually physically double stars or are visually close stars as was seen at the time of al-Ṣūfi. Most of these stars are probably not double stars in the modern understanding of the word. However I have tried to make a small investigation on this subject to identify these stars and check if any are actually double stars or not. This exercise can also shed some light on the level of accuracy and the ability of this astronomer to resolve close pairs of stars. It also gives us an estimate on what was the minimum angular separation which al-Ṣūfī managed to achieve in his observation of these stars.

From al-Ṣūfî's description I tried to identify below all the double stars found in alṢūfís book (Table 14). In Column 3 of this table I included the HR number and magnitude of these stars with the first HR number for the main star as mentioned in the catalog. The second HR number and magnitude is for the companion star as per the description of al-Ṣūfi. I also included the coordinate of these stars after accounting for precession for the epoch of A.D. 960. For example the HR number for the first star is HR1995 which according to al-Ṣūfī has the magnitude of 5 and a modern magnitude of 4.52 . Its RA coordinates is $4: 38: 8$ and Dec $+39: 10: 52$. Whereas the HR number for the companion star is HR2012. Al-Ṣūfĩ did not assign a magnitude for this star however it has a modern magnitude of 3.97 . Its RA coordinate is 4:40:25 and Dec $+38: 02: 38$. In column 4 of this table I calculated the angular distance between these stars in order to identify the minimum angular distance which al-Ṣūfì managed to achieve. In the last column of the table I included a brief summary on every one of these stars as they were mentioned by al-Ṣūfi. This summary included all the descriptions both from the tables as well as from the comments in the constellation chapters which mentioned these stars according to al-Ṣūfì.

Table 14: Double stars according to al-Ṣūfī

| Number | Star Number according to al-Ṣūfī | -HR <br> -Al-Ṣūfí <br> Magnitude <br> -Modern <br> Magnitude <br> -Coordinates | Angular Distance | Description according to al-Ṣūfī |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 5 Auriga | HR 1995 <br> (5) <br> (4.52) <br> 4:38:8 <br> +39:10:52 <br> HR2012 <br> (not <br> mentioned) (3.97) <br> 4:40:25 <br> +38:02:38 | 1.22 deg | From the table: <br> The star on the right elbow. <br> From the comments: <br> The fifth is on its right elbow. It is of the $5^{\text {th }}$ magnitude. Ptolemy mentioned it as the $4^{\text {th }}$ magnitude. This is a double star because next to it is a close star. |
| 2 | $29$ <br> Ophiuchus | HR6771 <br> (4) <br> (3.73) <br> 17:18:22 $+09: 59: 46$ <br> HR6770 (small-faint star) $=5$ or 6 (4.64) 17:12:58 $+09: 10: 17$ | $\begin{aligned} & 1.57 \\ & \operatorname{deg} \end{aligned}$ | From the table: <br> The lone star north of these 4 . <br> From the comments: <br> The fifth (which is the twenty ninth star fifth out side of the constellation) is the lone star to the north. It is farthest from the other four by a distance of two dhira $\bar{a}$. It is a double star because next to it is a small (faint) star close to it. |
| 3 | 11 Serpens | HR5881 <br> (4) <br> (3.53) <br> 14:56:10 <br> $+00: 13: 20$ <br> HR5895 <br> (small-faint star) $=5$ or 6 (5.11) <br> 14:57:54 $+00: 31: 44$ | $\begin{aligned} & 0.53 \\ & \operatorname{deg} \end{aligned}$ | From the table: <br> The star after the next bend which is in advance of the left hand of Ophiuchus. <br> From the comments: <br> Then it bends towards the south-east by a distance of two Thira to the eleventh star which is a double star of the $4^{\text {th }}$ magnitude. Next to it is a small (faint) star close to it which makes it a double star. |
| 4 | $4$ <br> Triangulum | $\begin{aligned} & \hline \text { HR664 } \\ & (3 \mathrm{~s})=3.25 \\ & (4.01) \\ & 1: 17: 59 \\ & +28: 42: 08 \end{aligned}$ | $\begin{aligned} & 0.57 \\ & \operatorname{deg} \end{aligned}$ | From the table: <br> The rearmost of the three. <br> From the comments: <br> The fourth is the southernmost star of less than the $3^{\text {rd }}$ magnitude. Ptolemy mentioned |


|  |  | HR655 (6) $(5.28)$ $1: 16: 48$ $+28: 11: 58$ |  | it is exactly of the $3^{\text {rd }}$ magnitude. It is a double star because next to it is a star of the $6^{\text {th }}$ magnitude close to it, which was not mentioned by Ptolemy. It resembles the third star on the base in magnitude. |
| :---: | :---: | :---: | :---: | :---: |
| 5 | 31 Virgo | HR5019 <br> (5) <br> (4.74) <br> 12:24:01 <br> $-12: 41: 12$ <br> HR5044 <br> (not <br> mentioned) <br> (5.37) <br> 12:28:33 <br> -12:08:13 | $\begin{aligned} & 1.24 \\ & \text { deg } \end{aligned}$ | From the table: <br> The middle one of these, which is a double star. <br> From the comments: <br> The fifth is to the rear of the two. It is a double star. The distance from the fourth star towards the south-east is one dhira $\bar{a}^{\prime}$. It is of the $5^{\text {th }}$ magnitude. |
| 6 | 8 Sagittarius | HR7116 <br> (nebulous) <br> (4.83) <br> 17:51:27 <br> -23:19:02 <br> HR7120 <br> (not <br> mentioned) <br> (5.00) <br> 17:52:26 <br> -23:16:04 | $\begin{aligned} & 0.23 \\ & \text { deg } \end{aligned}$ | From the table: <br> The star on the eye, which is nebulous and double. <br> From the comments: <br> The eighth is the nebulous star on the eye of Sagittarius. It is towards the north from the sixth star by a distance of two dhira ${ }^{\text {' }}$. |
| 7 | $\begin{array}{\|l\|} \hline 23 \\ \text { Sagittarius } \end{array}$ | HR7343 <br> $(4 \mathrm{~s})=4.25$ <br> (4.29) <br> 18:07:20 <br> -45:55:57 <br> HR7337 <br> (not <br> mentioned) <br> (4.01) <br> 18:07:01 <br> -45:34:50 | $\begin{aligned} & 0.36 \\ & \text { deg } \end{aligned}$ | From the table: <br> The star on the front left hock. <br> From the comments: <br> The twenty third star is on the tip of the left hand. It is south of the constellation Corona Australis by a distance of two and a half dhir $\bar{a}$ '. It is less than the $4^{\text {th }}$ magnitude. Ptolemy mentioned it is of the $2^{\text {nd }}$ magnitude. It is a double star because next to it is a close star which makes it a double star. It is drawn on the southern astrolabes as a star of the $2^{\text {nd }}$ magnitude. It is called 'Urqūb al-Rāmī. |
| 8 | 31Aquarius | HR8968 <br> (5) <br> (5.00) <br> 22:45:23 <br> -19:51:45 <br> HR8987 <br> (6) | 2.83 deg | From the table: <br> The more advanced of the 2 stars close together after the latter. <br> From the comments: <br> Next to the two close stars (the thirtieth and the thirty first) is a star of the $6^{\text {th }}$ magnitude which makes it a double star. It |


|  |  | $\begin{aligned} & \hline(5.28) \\ & 22: 48: 02 \\ & -21: 06: 07 \end{aligned}$ |  | was not mentioned (by Ptolemy). |
| :---: | :---: | :---: | :---: | :---: |
| 9 | 16 Cetus | HR334 $(3 \mathrm{~s})=3.25$ $(3.45)$ $00: 16: 38$ $-15: 50: 49$ HR329 $(6)$ $(5.82)$ $00: 15: 46$ $-15: 27: 15$ | $\begin{aligned} & 0.45 \\ & \text { deg } \end{aligned}$ | From the table: <br> The more advanced of them. <br> From the comments: <br> The sixteenth is the more advanced of them. The distance between them is approximately two $d h i r a \vec{a}$. It is less than the $3^{\text {rd }}$ magnitude. Ptolemy mentioned it is exactly of the $3^{\text {rd }}$ magnitude. Under it is a close star of the $6^{\text {th }}$ magnitude which makes it a double and which was not mentioned by Ptolemy. |
| 10 | 12 Orion | HR2135 <br> $(5 \mathrm{~s})=5.25$ <br> (4.63) <br> 5:02:43 <br> $+19: 28: 01$ <br> HR2130 <br> (not <br> mentioned) <br> (5.14) <br> 5:02:28 <br> +19:00:37 | $\begin{aligned} & 0.46 \\ & \text { deg } \end{aligned}$ | From the table: <br> The rearmost of them. <br> From the comments: <br> The twelfth star is to the rear of the two. It is less than the $5^{\text {th }}$ magnitude. Ptolemy mentioned that it is exactly $5^{\text {th }}$ magnitude. It is a Mud'af (double star) because there is a star next to it. |
| 11 | 15 Eridanus | HR925 $(5)$ $(5.26)$ $2: 13: 53$ $-12: 02: 00$ HR917 $(5)$ $(5.32)$ $2: 12: 19$ $-12: 08: 34$ | 0.40 | From the table: <br> The one in advance of this. <br> From the comments: <br> The fifteenth is in front of the fourteenth star towards the north. It is of the $5^{\text {th }}$ magnitude while Ptolemy mentioned it is of the $4^{\text {th }}$. The distance between them is one dhir $\vec{a}^{\prime}$. It is a double star. |
| 12 | 21 Eridanus | HR 1003 <br> (4) <br> (3.69) <br> 2:33:40 <br> -25:53:47 <br> HR994 <br> (4) <br> (4.88) <br> 2:32:45 <br> -26:40:05 | $\begin{aligned} & 1.25 \\ & \text { deg } \end{aligned}$ | From the table: <br> The middle one of these. <br> From the comments: <br> The twenty-first follows the twentieth. It is of the $4^{\text {th }}$ magnitude. The distance between them is two dhira $\bar{a}$ '. It is a double star because to the south and close to it is a star which makes it a double. |
| 13 | 8\&9 Argo | HR2996 | 0.55 | From the table: |


|  |  | $(4)$ $(3.96)$ $7: 02: 17$ $-26: 54: 33$ HR2993 $(5)$ $(4.59)$ $7: 01: 46$ $-26: 22: 29$ | deg | -The rearmost of them. <br> -The middle one of the three. <br> From the comments: <br> The ninth is close to the eighth, a little inclined towards the north-west. The eighth star is double (with the ninth). |
| :---: | :---: | :---: | :---: | :---: |
| 14 | 12 Argo | HR2773 <br> (3) <br> (2.70) <br> 6:40:37 <br> -35:37:51 <br> HR2787 <br> (not <br> mentioned) <br> (4.66) <br> 6:41:32 <br> -35:14:32 | $\begin{aligned} & 0.43 \\ & \text { deg } \end{aligned}$ | From the table: <br> The southernmost of them <br> From the comments: <br> The twelfth is south of the eleventh star. It is far from it with a distance between them of three dhirara. It is of the $3^{\text {rd }}$ magnitude. It is on the plank where the Kawthal (front sail) is built. It is a double star because next to it is a close star which makes it a double. |
| 15 | 34 Argo | HR3055 <br> (6) <br> (4.11) <br> 7:17:38 <br> -44:05:00 <br> HR3037 <br> (faint) $=5$ or 6 <br> (5.23) <br> 7:16:11 <br> -44:21:19 | $\begin{array}{\|l\|} \hline \begin{array}{l} 0.38 \\ \text { deg } \end{array} \\ \hline \end{array}$ | From the table: <br> The faint star to the rear of this. <br> From the comments: <br> The thirty-fourth is behind the thirty-third star. It is inclined towards the south with a distance between them of one third of a dhir $\bar{a}$ '. It is of the $6^{\text {th }}$ magnitude. It is a double star because next to it is a faint star which makes it a double. |
| 16 | 3 Hydra | HR3482 <br> (4) <br> (3.38) <br> 7:51:07 <br> $+09: 42: 22$ <br> HR3492 <br> ( 5 s ) $=5.25$ <br> (4.36) <br> 7:52:58 <br> +09:09:41 | $\begin{array}{\|l\|} \hline 0.71 \\ \text { deg } \end{array}$ | From the table: <br> The northernmost of the 2 to the rear of these, which is about on the skull. <br> From the comments: <br> Next to the third is a star less than the $5^{\text {th }}$ magnitude. Together with the third they form a double star. It was not mentioned by Ptolemy. |
| 17 | 5\&6 Corvus | HR4757 $(3)$ $(2.95)$ $11: 36: 49$ $-10: 44: 59$ | $\begin{array}{\|l\|} \hline 0.62 \\ \text { deg } \end{array}$ | From the table: <br> -The more advanced of the 2 stars in the rear wing. <br> -The rearmost of them. <br> From the comments: |


|  |  | $\begin{aligned} & \hline \text { HR4775 } \\ & (4) \\ & (4.31) \\ & 11: 38: 58 \\ & -10: 25: 53 \end{aligned}$ |  | The sixth follows the fifth close to it with a distance of less than a Shibr. It is of the $4^{\text {th }}$ magnitude. Together with the fifth they form a double star. |
| :---: | :---: | :---: | :---: | :---: |
| 18 | $22$ <br> Centaurus | HR4940 <br> (5) <br> (4.71) <br> 12:09:26 <br> -42:46:31 <br> HR4933 <br> (not mentioned) (4.85) 12:06:51 -43:49:42 | $\begin{aligned} & 1.06 \\ & \mathrm{deg} \end{aligned}$ | From the table: <br> The star in advance of this on the horse's back. <br> From the comments: <br> The twenty-second is in front of the twenty-first and oriented towards the south. The distance between them is two and half dhir $\bar{a}$ '. It is of the $5^{\text {th }}$ magnitude. It is a double star because next to it is star which makes it a double star. |
| 19 | 8 Ara | HR6897 <br> (4) <br> (3.51) <br> 17:10:17 <br> -45:40:50 <br> HR6934 <br> (6) <br> (4.96) <br> 17:15:02 <br> -45:44:50 | $\begin{aligned} & 0.85 \\ & \text { deg } \end{aligned}$ | From the table: (not in the table) <br> From the comments: <br> Behind the second star is another star also of the $4^{\text {th }}$ magnitude. The distance between them is one third of a dhir $\bar{a}$ '. It was not mentioned by Ptolemy. This star is a double star because next to it is a star of the $6^{\text {th }}$ magnitude which makes it a double. |
| 20 | 5 Piscis Australis | HR8431 <br> (5) <br> (4.17) <br> 21:05:53 $-37: 40: 12$ <br> HR8447 <br> (not mentioned) (4.92) 21:07:55 <br> -37:15:26 | 0.54 | From the table: <br> The star on the belly. <br> From the comments: <br> The fifth star is in front of the first on the belly. It is of the $5^{\text {th }}$ magnitude. The distance between it and the first is close to two dhira $\bar{a}$. It is a double star because next to it is a star which makes it a double. |

From the Table 14 the minimum angular separation for the above Mud'af (double) stars (discounting the reference star) was achieved by 8 Sagittarius (star number according to al-Ṣūfì), which according to Ptolemy and al-Ṣūfĭ is both a nebulous and a double star. The two stars which are in the magnitude range which could be seen in this nebula are: HR7116 and HR7120. The angular separation between these two stars at the epoch of al-Șūfī was 0.23
degrees. It is an interesting point to note here that the star HR7120 is next to the globular cluster NGC6717 (magnitude 9.3). The two stars HR7116 and HR7120 together with the globular cluster might have been the cause of the comments that 8 Sagittarius is double and nebulous even though a globular cluster of magnitude 9.3 would be far below the limit of unaided eye visibility.

I have included in the below Table 15 the star 26 Ursa Major as a reference star, which is the star Mizar. Next to Mizar is the star Alcor. The angular separation between these two stars is 0.20 degrees. However al-Ṣūfī did not refer to these two stars as Muḍ'af or double but he only mentioned that adjacent to al-'Anāq (Mizar) is the star called al-Suhā (the neglected one (Kunitzsch, 2006)). It was well known that the Arabs were able to separate these two stars long before the time of al-Ṣūfi. These stars were used by the Arabs as an eyesight test for the ability to separate and distinguish between the two. The proverb "I showed him al-Suhā and he showed me the Moon" was used as a metaphor indicating the strength of ones eyesight meaning "I can distinguish the very small detail while he can only see large objects such as the Moon". The separation of 8 Sagittarius is quite close to the separation 26 Ursa Major. Even though this shows the ability of al-Ṣūfī as an accomplished observer, however he still did not achieve the level which was reached by the Arabs before him or the minimum visual separation with the unaided eye.

Table 15: Reference Star

| Number | Star <br> Number according to al-Ṣūfī | -HR <br> -al-Ṣūfí <br> Magnitude <br> -Modern <br> Magnitude <br> -Coordinates | Angular Distance | Description according to al-Ṣūfī |
| :---: | :---: | :---: | :---: | :---: |
| Reference <br> star | 26 Ursa <br> Major | HR5054 <br> -al-‘Anāq <br> -Mizar <br> (2) <br> (2.27) <br> 12:40:47 <br> $+60: 28: 44$ <br> HR5062 <br> -al-Suhā <br> -Alcor <br> (small- <br> faint) $=5$ or 6 <br> (4.01) | $\begin{aligned} & 0.20 \\ & \mathrm{deg} \end{aligned}$ | From the table: <br> The middle one. al- 'Anāq. <br> Above al- 'Anāq is a small star adjacent to it which the Arabs call al-Suh $\bar{a}$. In other Arab dialects it is (also) called by the name of: al-Shitā' and al-Saidaq and $N u$ 'aish. This star has not been mentioned by Ptolemy. This star is also used by people to test their eyesight, for they say: "I showed him al-Suhā and he showed me the Moon". |


|  |  | $12: 42: 19$ <br> $+60: 31: 55$ |  |  |
| :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |

### 5.9 The Nebulae in al-Ṣūfī’s Book

The term 'nebula' comes from the Latin word for cloud. A nebula is a cloud of dust and gas in space. In the past the term nebula was also used for distant galaxies, clusters and any other hazy patches of light which resembles a cloud among the stars. After the use of telescopes, the discovery of spectroscopy and the invention of photography, it was possible to distinguish real nebulae from galaxies.

The Arab and Islamic astronomers observed and identified several nebulae very early in their scientific endeavors. The Arabic term used for a nebula was al-Sahābi which also means a cloud. In his major astronomical treatise (al-Qānūn al-Mas'u$d \bar{l}$ ), al-Bīrūnī describes al-Saḥābiāt (plural for nebula) by these words:
> "In the sky there are objects which do not resemble the stars in their round shape and by the bright light which they have. These are the al-Latkhāt al$B \bar{i} \underset{d}{ }$ (the white smears) called al-Sahāabia (nebula). Some believe that these (nebulae) are part of the (the Milky Way) galaxy; however they are both alike and both resemble clouds. These (nebulae) are believed to be an Ishtibāk (a mass) of small stars grouped together"

Al-Bīrūnī clearly distinguished between nebulae and the Milky Way and he described the nature of these nebulae as a concentration or group of stars. As for the Milky Way it was called al-Majarra in Arabic, which is directly translated as just 'the Galaxy'. According to alMarzūqī, in his book Kitāb al-Azminah wa al-Amkina, he said: "...the ancient Arabs called al-Majarra: Um al-Nujūm (the mother of all stars) because there is no area in the sky which has more stars then it." The Arabs also called the Milky Way: Sharj al-Sama' (the dome of the sky) and Nahr al-Majarra (the galaxy river). However the name by which the Milky Way was mostly used was Darb al-Tabbānah (the path of straws). The term Darb al-Tabbānah describes a picture of farmers coming back from planting their fields while dropping straws every once in a while thus producing white patches on the ground. Abū Hanīfa al-Daīnawari also described the location of the galaxy in those words: "al-Majarra (the galaxy) is a connected circle like a ring. Even though it is narrow in some places and wide in others however this is due to its circular nature. It is most wide between (the Asterism) Shawlat al'Aqrab (the sting of Scorpio) and al-Nasrān (the two constellations: Lyra and Aquila)".

From the above descriptions which we find in many historical references we see that the ancient Arabs were well aware of these cloud-like objects. The Arabic and Islamic scholars and astronomers later described in detail the nature and location of these nebulae as well as the Milky Way galaxy which they could clearly see in the sky. Al-Ṣūfī also refers to the nebulae as al-Lattkhā al-Sahābiya (the nebulous smear or smudge) and al-Ishtibāk alSaḥābi (the nebulous mass). As his work was based on Ptolemy's book, al-Ṣūfī again identifies the five nebulae which Ptolemy mentioned before. However al-Ṣūfī goes further to describe several other nebulae which he observed himself or were previously identified by the Arabs.

From al-Ṣūfî's description I tried to identify below all the nebulae found in al-Ṣūfí's Book of the Fixed Stars (Table 16). I have included the modern names or designations which correspond to these nebulae. I also indicated the magnitude and surface brightness of these deep sky extended objects. By definition the magnitude of an extended astronomical objects such as galaxies and nebulae is the measure of the concentration of their light at a point source where as the surface brightness of an object is the measure of brightness or magnitude per square arc minute. Therefore the surface brightness of an object is a more practical way to estimate the degree of visibility of extended deep sky objects than using magnitude methods only. Finally in the last column of the table I have included a brief summary on every one of these nebulae as they were mentioned by al-Ṣūfi. This summary includes all the descriptions taken from both the tables as well as from the comments in the constellation chapters of alṢūfī's book.

Table 16: Nebulae found in al-Ṣūfī's book
$\left.\begin{array}{|l|l|l|l|}\hline \text { Number } & \begin{array}{l}\text { Modern } \\ \text { name \& } \\ \text { designation, } \\ \text { Magnitude } \\ \text { \& Surface } \\ \text { brightness }\end{array} & \begin{array}{l}\text { Star/Nebula \& } \\ \text { magnitude } \\ \text { according to } \\ \text { al-Sūfī }\end{array} & \text { Description according to al-Ṣūfī } \\ \hline 1 & \begin{array}{l}\text { NGC } \\ 869 / 884 \\ \text { Open } \\ \text { clusters } \\ \text { Magnitude } \\ 5.30 / 6.10 \\ \text { Surface } \\ \text { brightness } \\ 12.43 / 13.23\end{array} & 1 \text { Perseus } & \text { Nebula }\end{array} \begin{array}{l}\text { From the table: } \\ \text { The nebulous mass on the right hand. } \\ \text { From the comments: } \\ \text { The first of its stars is al-Laṭkhā al-Sahāabiya (nebulous } \\ \text { smear) on the camel's thigh which we have talked about } \\ \text { when we discussed the constellation Cassiopeia. It is on the } \\ \text { edge of its (Perseus) right hand. }\end{array}\right\}$

|  | (NGC 2632) <br> Open cluster <br> Magnitude <br> 3.10 <br> Surface <br> brightness <br> 13.00 | Nebula | The middle of al-Ishtibāk al-Saḥābi (nebulous mass) in the chest, called al-Mi'laf (Praesepe). <br> From the comments: <br> The first of its stars is a Laṭkh $\bar{a}$ (smear) which resembles a piece of cloud surrounded by four close stars with the patch in the middle. Two stars are in front and two are behind. |
| :---: | :---: | :---: | :---: |
| 3 | M7 <br> (NGC 6575) <br> Open <br> Cluster <br> Magnitude <br> 3.30 <br> Surface brightness 12.00 <br> Or <br> NGC6441 <br> Globular cluster <br> Magnitude 7.40 <br> Surface brightness 11.6 | 22 Scorpio $4(s)=4.25$ | From the table: <br> The nebulous star to the rear of the sting. <br> From the comments: <br> As for the three stars outside of the constellation, the first is a star to the rear of al-Shawla and behind the nineteenth star which is on the seventh joint. It is less than $4^{\text {th }}$ magnitude. Ptolemy mentioned that it is a nebulous object. The distance between it and the nineteenth star which is on the seventh Kharaza (joint) is a little more than one dhira $\bar{a}$ '. And the distance between it and al-Shawla is close to one and a half dhira $\bar{a}$. |
| 4 | HR7116 <br> HR7120 <br> NGC6717 <br> Globular <br> cluster <br> Magnitude <br> 9.30 <br> Surface brightness 12.00 | 8 Sagittarius <br> Nebula | From the table: <br> The star on the eye, which is nebulous and double. <br> From the comments: <br> The eighth is the nebulous star on the eye of Sagittarius. It is towards the north from the sixth star by a distance of two dhirā'. |
| 5 | CR69 <br> Open cluster <br> HR1879 <br> HR1883 <br> HR1876 <br> HR1907 <br> Magnitude <br> 2.80 <br> Surface | 1 Orion Nebula | From the table: <br> The nebulous star in the head of Orion, which consists of three close stars. <br> From the comments: <br> The first of its stars is the Saḥabbi (nebula) on the head. This nebula is made up of three small stars close together forming a small Muthallath (triangle). Ptolemy mentioned it to be one star located in the middle of the triangle and he indicated its longitude and latitude in his book. It is located on the head between the two shoulders and further away towards the north but closer to the left shoulder. |


|  | brightness 11.60 |  |  |
| :---: | :---: | :---: | :---: |
| 6 | CR399 <br> Open cluster <br> Magnitude <br> 3.60 <br> Surface <br> brightness <br> 12.95 | $\qquad$ <br> Magnitude not mentioned | From the table: <br> (Description is only mentioned in the comments on the constellation Aquila). <br> From the comments (Constellation Aquila): <br> There is an image of a bowl (cup) with its stars beginning from the bright star on the tail, continuing towards the north-west then going to the east to the base of the bowl; then towards the south-east until it reaches a nebula located north of two stars in the notch of the constellation Sagitta. The distance between the nebula and the top of the bowl is two dhir $\bar{a}$ '; the nebula is located on the east edge and the bright star on the tail on its western edge. |
| 7 | M31 <br> Andromeda <br> Galaxy <br> Magnitude <br> 3.40 <br> Surface <br> brightness <br> 13.50 | Magnitude not mentioned | From the table: <br> (Description is only mentioned in the comments on the constellation Andromeda) <br> From the comments: <br> The Arabs mentioned two lines of stars surrounding an image resembling a large fish below the throat of the Camel. Some of these stars belong to this constellation (Andromeda) and others belong to the constellation Pisces which Ptolemy mentioned as the twelfth constellation of the Zodiac. These two lines of stars begin from the al-Laṭkh $\bar{a}$ al-Saḥābiya (nebulous smear) located close to the fourteenth star which is found at the right side of the three (stars) which are above the girdle. |
| 8 | IC2391 <br> Omicron <br> Velorum open cluster <br> Magnitude <br> 2.50 <br> Surface <br> brightness <br> 12.00 | Magnitude not mentioned | From the table: <br> (Description is only mentioned in the comments on the constellation Argo Navis) <br> From the comments: <br> Above the thirty-seventh star at a distance of one dhira $\bar{a}$, there is a nebulous star. |
| 9 | Large <br> Magellanic <br> cloud <br> Magnitude <br> 0.40 <br> Surface <br> brightness <br> 14.10 | $\qquad$ <br> Magnitude not mentioned | From the table: <br> (Description is only mentioned in the comments on the constellation Argo Navis) <br> From the comments: <br> Some claim that under the star Suhail (the star Canopus) is a star called Qaḍam Suhail (feet of Suhail) and under Qadam Suhail are many bright white stars which are not seen from Iraq and Najd (area north of Arabia). The people of Tehāma (area south of Arabia) call them al-Baqar (Oxen). Ptolemy does not mention any of this and we do not know if this is right or wrong. |
| 10 | M45 <br> Pleiades | 29 Taurus <br> 30 Taurus <br> 31 Taurus | From the table: <br> -The Pleiades: the northern end of the advanced side. <br> -the southern end of the advanced side. |


|  | Open cluster <br> Magnitude <br> 1.20 <br> Surface <br> brightness <br> 11.00 | 32 Taurus $\begin{aligned} & 5 \\ & 5 \\ & 5 \\ & 4 \end{aligned}$ | -The rearmost and narrowest end of the Pleiades. <br> -The small star outside the Pleiades towards the north. <br> From the comments: <br> The Arabs called the twenty-ninth, the thirtieth, the thirtyfirst and the thirty-second, al-Thurayy $\bar{a}$ (the Pleiades). Inside (the Pleiades) are two stars or three together with the other four looking like a bunch of grapes that are close together. Therefore they considered them as one star and named it al-Najem (The Star) par excellence. They also named it Nujūm al-Thurayyā (the stars of the Pleiades). It was called al-Thurayyā because they were blessed by it and by its rise, and they claimed that the rain which falls when it Naw (sets) brings good luck. <br> (al-Thurayy $\bar{a}$ ) means a small fortune (the diminutive noun for fortune). They (the Arabs) diminutised it because its stars are close and small. They mentioned in their books that it is located on the Aliet (the buttocks or the fat tail of a sheep) of (the constellation) Aries, (however) it is located on the Sinām (hump) of Taurus. <br> The distance between it and the last star on the buttocks of Aries is three dhirā' as is seen by the eye. It is the third of Manāzil al-Qamar (the lunar mansions). |
| :---: | :---: | :---: | :---: |

### 5.9.1 Notes on the Nebulae found in al-Ṣūfí's Book

I have included below some comments on the above nebulae which were identified by alṢūfī. I also included their modern pictures in order to describe and identify these objects much more clearly:

1. The double clusters NGC884 and NGC869 (Figure 42) were observed by many cultures such as the Greeks, Indians and others long before the time of al-Ṣūfī. These clusters were cataloged by Hipparchus as well as Ptolemy. These clusters are bright enough to be clearly seen by the naked eye.


Figure 42 Double clusters NGC884 and NGC869.

In his comments al-Ṣūfī refers to the "camel's thigh" which he mentioned also in his description of the constellation Cassiopeia. Al-Ṣūfi mentioned that the ancient Arabs described a picture of a camel which they identified between the constellation of Cassiopeia and Perseus.
2. The open cluster M44 (Figure 43) is another nebula which was clearly seen by the naked eye and recognized a long time ago by the Greeks and other cultures.


Figure 43 M44 open cluster.
3. Formerly the nebula which was associated with the star 22-Scorpio was considered to be the open cluster M7. It is interesting to note that al-Ṣūfì assigns a magnitude to the star 22 -Scorpio of $4(s)=4.25$. For all other nebulae he only mentions that they are nebulous objects. This procedure was also used in the Almagest therefore al-Ṣūfì again tried to adhere to Ptolemy's method of description in this regard except for the star 22-Scorpio. However for the star 22-Scorpio al-Ṣūfì might have been referring to the star HR6630 (magnitude 3.21) which also has next to it the globular cluster NGC6441 (surface brightness 11.6). Al-Ṣūfī states that Ptolemy mentioned that this star is a nebulous object. He then goes on to determine the distance between this nebulous object and the nineteenth star which is on the seventh Kharaza (joint) as a little more than one dhirā', and the distance between it and al-Shawla (stars 20/21 Scorpio) as close to one and a half dhira $\bar{a}^{\prime}$. From these distance approximations this nebula should be about 2 deg 20 min from the nineteenth star of Scorpio and 3 deg 30 min from the twentieth and the twenty first stars of Scorpio. I have calculated the distance between these nebulae and these stars and the results are indicated in the following table 17:

Table 17: Distance between Nebulae and Stars

| Distance from | Distance from | Distance from | Distance from |
| :--- | :--- | :--- | :--- |
| NGC6441 to | NGC6441 to | M7 to | M7 to |
| 19 Scorpio | $21 / 20$ Scorpio | 19 Scorpio | $21 / 20$ Scorpio |
| $2 \operatorname{deg} 34 \mathrm{~min}$ | $3 \operatorname{deg} 38 \mathrm{~min}$ | $4 \operatorname{deg} 53 \mathrm{~min}$ | 5 deg 07 min |

From these approximate distances and the fact that one dhira' is $2 \operatorname{deg} 20$ minutes according to al-Ṣūfi himself it looks more likely that the nebula which al-Ṣūfī was referring to in this case is the globular cluster NGC6441 and not M7 as was supposedly known. This distinction was first recognized by Manitius (1912) then by Peters and Knobel (1915) and later confirmed by Toomer in his translation of the Almagest (1984).


Figure 44: Map which shows NGC6441


Figure 45: Image of NGC6441

Figure 44 is a map which shows that NGC6441 is much closer to the nineteenth, twentieth and the twenty-first stars of Scorpio than is M7. Figure 45 is an image of the globular cluster NGC6441 to the left of the star HR6630 taken from the Digitized Sky Survey
4. Al-Ṣūfì mentioned the star 8-Sagittarius as a double star together with a nebulous star. The two stars were identified as HR7116 and HR7120. Next to HR7120 is the NGC6717 globular cluster. Al-Ṣūfī might have been referring to these three objects as a nebulous asterism. I have obtained the image from the Digitized Sky Survey (Figure 46) which shows the star HR7116 on the right edge of the image and star HR7120 in the center with NGC6717 just under it.


Figure 46: Stars HR7116, HR7120 and globular cluster NGC6717.
5. The image below is of the open cluster CR69 with the star HR1879 centered in the middle. This image was obtained from the Digitized Sky Survey


Figure 47: CR69 open cluster.
6. The CR399 open cluster (see Figure 48) was first discovered by al-Șūfí and described in his Book of the Fixed Stars. It was later independently rediscovered by Giovanni Hodierna in 1654. It is also sometimes named Brocchi's Cluster after the astronomer D.F. Brocchi, who created a map of it in the 1920s. It was included in Collinder's 1931 catalog of open clusters and given the designation of Collinder 399.


Figure 48: CR399 open cluster.
7. Messier 31 (M31 is the famous Andromeda Galaxy (see Figure 49). It is the nearest large spiral galaxy to us. It was first discovered by al-Ṣūfì and described in his Book of the Fixed Stars. It was later included in early European star catalogs, for example Simon Marius in 1612, Giovanni Hodierna in 1654 and Charles Messier in 1764.


Figure 49: M31 Andromeda Galaxy.
8. The Omicron Velorum open cluster (CR399) was first discovered by al-Ṣūfī and described in his Book of the Fixed Stars (see Figure 50). It was later rediscovered by Abbe Lacaille in 1752 and he cataloged it as 'Lac II.5'.


Figure 50: Omicron Velorum open cluster.
9. The Large Magellanic Cloud (Figure 51), together with its small neighbor the Small Magellanic Cloud, are well known objects in the southern hemisphere. They must have been very well recognized by ancient cultures living in the Southern Hemisphere. However there is very little preserved evidence to document these facts. Some Arab researchers claim that the earliest documented proof of observation of the Magellanic Clouds might be found in al-Ṣūfí's Book of the Fixed Stars (Mujahed, 1997). However, al-Șūfì only mentioned that there are stars under the stars of Suhail (Canopus) and Qadam Suhail (feet of Suhail) which the Arabs call al-Baqar (Oxen) but he does not mention that there is any nebula. This recent claim is probably due to the fact that al-Baqar was mentioned by the $15^{\text {th }}$ century Arab seafarer Ibn-Majed who mentioned the Large Magellanic Cloud as a nebula and named it al-Baqar before it was documented by Magellan in A.D. 1519. However, al-Ṣūfí does not claim that he observed these stars himself. He attributed this to the southern people of Arabia (region of Tehāma). He admits that he does not know if this is right or wrong. This is a tribute to this author's scientific integrity whereby in the same paragraph he admits to making his observations from the city of Shiraz which according to the observation he made with the 'Adud $\bar{\imath}$ Ring is 29 deg and 36 min and at this latitude these stars could not be seen.


Figure 51: Large Magellanic Cloud.
10. Al-Şūfi mentioned that inside the Pleiades (Figure 52) there are two stars or three together with the other four looking like a bunch of grapes. These additional stars are HR 1149, HR 1165 and HR1142. Therefore, together with the other four, al-Ṣūfì managed to observe seven stars of the Pleiades.


Figure 52: M45 Pleiades open cluster.

### 5.10

 Old Arabic Astronomical Traditions in al-Ṣūfî’s WorkWhen ancient civilization were watching the heavens they observed that many groups of stars formed patterns in the sky that resembled people, animals and objects similar to what they experienced in their daily lives. Among those early civilizations were the ancient Arabic cultures that inhabited what we call now the Middle East. They named many of the stars, which they observed according to their own experience, and the environment which they lived in. This endeavor started more than 3000 years even before the emergence of Islam, which transformed the history of the region. At first this scientific movement was connected to the development of the lunar calendar. It then transformed into the unique science of the lunar mansions. From this effort another study emerged which was called 'Ilm al-Anwa'. The $A n w \bar{a}$ ' were a form of astrological-meteorological system of predicting the weather and identifying the beginning of the seasons in order to specify the dates of festivals, holidays, pilgrimage and the best times for traveling and commerce (see Section 2.3). These ancient fields of study are what were to be called 'Arabic folk astronomy'. They were very popular among many Arab and Islamic religious and scientific scholars such as al-Battānī and alDaīnawari, as well as al-Ṣūfī.

In his introductory chapter al-Ṣūfĩ divided those who study the stars into two groups. The first group was the astronomers (Munajjimin). The second group studied the Arabic method of the sciences of $a l-A n w \bar{a}$ ' and the Moon mansions. From this identification we can deduce that al-Ṣūfì considered 'Arabic folk astronomy' to be an important scientific field of study in its own right. He took upon himself to explain the development of this field as well as to identify all the various names of stars, asterisms, mansions and constellations as per the method of the Arabs. He also tried to correct many of the mistakes which were mentioned by previous authors in this subject such as al-Battānī and al-Daīnawari (see my translation of alṢūfí's Introductory chapter Section 4.1).

I have tabulated below the names of stars and asterisms for some of the constellations that have been used in Arabic folk astronomy. This exercise is only to give an idea on the scope of information which is contained in each of the chapters on the constellations according to the explanation of al-Ṣūfi:

Table 18: Names of stars in constellation Ursa Minor as per Arabic folk astronomy.

| Arabic Name | Name in Arabic | Star/s (HR) | Explanation |
| :---: | :---: | :---: | :---: |
| al-Farqadain | الفرقاين | 5563, 5735 | The meaning of this word in Arabic is: "The two calves". |
| Banāt Na'sh alṢughra | بنات نـش الصغرى | The bier <br> 5903, 6116, <br> 5563, 5735 <br> The daughters <br> 424, 6789, 6322 | "The little daughters of the bier (or coffin)". The Arabs likened the image of this constellation to three women "the daughters" who are pulling "a bier (or coffin)". |
| al-Juday | الجي | 424 | "The kid or goat" (This is the polar star "Polaris". It is not to be confused with the constellation Capricorn even thought the Arabic folk name is the same as the constellation Capricorn). |
| Fa's al-Rahā | فاس الرحا |  | "A type of a fish", which is round and looks like a round "grinding axe". |

Table 19: Names of stars in constellation Ursa Major as per Arabic folk astronomy.

| Arabic Name | Name in Arabic | Star/s (HR) | Explanation and comments |
| :---: | :---: | :---: | :---: |
| al-Mirāq | المراق | 4295 | The flank or groin. |
| al-Khatem | الخطم | 3323 | The snout. |
| Banāt Na'sh al-kubra | بنات الكبرى | $\begin{array}{\|l\|} \hline 5191,5054,4905 \\ 4301,4295,4660,4554 \end{array}$ | "The great daughters of the bier (or coffin)". The Arabs likened the image of this constellation to three women "the daughters" (Banat) who are pulling "a bier (or coffin)". <br> al-Naeesh means the bier (or coffin). |
| Bani Na'sh | بني نـش |  | The clan of al-Na'sh (bier). |
| Sarīr Banāt Na'sh | سرير بنات نـش | 4301,4295,4660,4554 | The bed of the daughters of the Bier. The coffin was sometimes referred to as a bed. |
| al-Qä' $\bar{l} d$ | القائد | 5191 | The leader. |
| al-'Anāq | العناق | 5054 | A young female goat. |
| al-Jūn | الجون | 4905 | The bull. |
| al-Suhā | السها | 5062 | The Arabic translation of the word means the neglected one. This is the star "Alcor". As alṢūfi wrote, it is also called by other names which are: alShita $\overline{\text { ' }}$, al-Saidaq and Nu 'aish. |
| Kafazāt alZibā | قفزات الظّ | The first Kafza (al-Kafza al-Ūla) | The Arabic translation means: the leaps of a Gazelle. |


| al-Thu'ailibān <br> al-Qarā’in | الثُيلبان القراين | 4377, 4375 <br> The second Kafza (alKafza al-Thānīa) 4033, 4069 <br> The third Kafza (alKafza al-Thālitha) 3569, 3594 | These six stars represent the footprints or leaps of a Gazelle. (Al Kafazāt) are also called by the Arabs by other names such as: al-Thu'ailibān and alQarā’in. |
| :---: | :---: | :---: | :---: |
| Athar Zulfa alZibā | اثنر ظلفى الظبى |  | The hoof trail or footprints of a gazelle. |
| al-Şarfa | الصرفة | 4534 | This is the bright star called Denebola which is on the tail of (constellation) Leo. |
| al-Dafira, <br> al-Halba | الظفيرة <br> اللالبة | 4357, 4300, 4259,4362 | A group of stars above al-Ṣarfa that are (also) named by the Arabs al-Halba. These are four stars which are also found in the constellation of Leo. |
| al-Hawd | الحوض | $\begin{aligned} & 3624,3757,3888,3894, \\ & 3775,3662,3619 \end{aligned}$ | These stars form a semi-circle which is sometimes called Sarīr Banat $N a$ 'sh. Here al-Șūfī contradicts himself by naming Sarîr twice. |
| al-Zibā | الظّبى | $\begin{aligned} & 3323,3354,3403,3576, \\ & 3616,3771 \end{aligned}$ | It is translated to: Gazelle. These are the six stars on the eyebrow, the eyes, the ears and the snout. |
| Kibd al-Asad | كبد الاسد | 4915 | This is translated in Arabic to: the liver of the lion. This star is now in the modern constellation of Canes Venatici. |

Table 20: Names of stars in constellation Taurus as per Arabic folk astronomy.

| Arabic Name | Name in Arabic | Star/s (HR) | Explanation and comments |
| :---: | :---: | :---: | :---: |
| al-Thurayyā, <br> al-Najm, <br> Nujūm al- <br> Thurayyā | الثريا <br> النجم <br> نجوم الثريا | $1145,1156,1178,1188$ <br> Additional stars: $1149,1165,1142$ | The Arabs call the twentyninth, the thirtieth, the thirty-first and the thirtysecond, al-Thurayyā (the Pleiades). Inside (the Pleiades) are two stars or three together with the other four looking like a bunch of grapes that are close together. Therefore they considered them as one star and named it al-Najm (The Star) par excellence. It is the third of Manāzil alQamar (the lunar |


| al-Dabarān, Ain al-Thawr, Tāb'al-Najm, al-Tāb', al-Mijdah, al-Mujdah, Hadī al-Najm, al-fanīq | الدبران <br> عين الثور <br> تابع النجم <br> التابع <br> المِجدح <br> المُجدح <br> حادي النجم <br> الفنيق | 1457 | The star Aldebaran which is also known by the other name Ain al-Thawr (eye of Taurus). It is (also) called Tāb' al-Najm (star follower) and Tālī al-Najm (rear star) and al-Mijdah where the letter M is accented, as well as al-Mujdah. It is just called al-Tāb' (follower) by itself without adding the word al-Najm (star). It is also called Hadı̄ al-Najm (star follower - follower of the Pleiades) and al-fan $\bar{q} q$ which means the great Camel. It is the fourth of Manāzil al-Qamar (the lunar mansions). |
| :---: | :---: | :---: | :---: |
| al-Qilās, <br> Qilāṣa, <br> Ghunaīma | القلاص <br> القلاصة <br> غنيمة |  | The stars around (Aldebaran) are called alQilās which are the small Camels. (The Arabs) claim that (these stars) are named Qilās and also (named) Ghunaīma. |
| al-Kalbain | الكلبين | 1392, 1387 | The two close stars on the northern ear which are the twenty- first and the twentysecond are called al-Kalbain (the two dogs). They claim they are the dogs of Aldebaran. |
| al-Ḍayīqa | الضيقة |  | This means the small gap in Arabic. As al-Ṣūfī explained, the Arabs found between the setting of alThurayy $\bar{a}$ and Aldebaran a small difference or gap which they called al-Dayūqa (small/narrow gap). |
| al-Dāl | الدال | 1346,1373,1411,1457,1409 | The five (stars) which resemble (the Greek letter D) al-Dāl. <br> These are the stars the Greeks call the 'Hyades'. |

Table 21: Names of stars in constellation Scorpio as per Arabic folk astronomy.

| Arabic Name | Name in Arabic | Star/s (HR) | Explanation and comments |
| :---: | :---: | :---: | :---: |
| al-Iklīl | الاكليل | $\begin{aligned} & \text { 5984, 5953, } \\ & 5944 \end{aligned}$ | Al-Ṣūfī explains that the Arabs call the three stars on the forehead alIkilıl. However, he also refers to his explanation about this when he mentioned the constellation Libra and that the story from the Arabs about this is wrong. |
| al-Qalb (the heart). <br> Qalb al-'Aqrab | القلب | 6134 | This star is the middle of two other stars and is reddish in color as al-Ṣūfī explains. It is called Qalb al- 'Aqrab by the Arabs and (Antares) by the Greeks. |
| al-Nìy ${ }^{\text {a }}$ t | النياط | 6084, 6165 | The seventh star in front of al-Qalb and the ninth star behind it are called al-Nīyāt. |
| al-Fiqarāt <br> (plural) <br> Fiqra <br> (singular) | الفنقرات | 6241 (1t joint) <br> 6247 ( $2^{\text {nd }}$ joint) <br> 6262 ( $3^{\text {rd }}$ joint) <br> 6271 ( $3^{\text {rd }}$ joint) <br> 6380 (4 $4^{\text {th }}$ joint) <br> 6553 ( $5^{\text {th }}$ joint) <br> 6615 ( $6^{\text {th }}$ joint) <br> 6580 ( $7^{\text {th }}$ joint) | Fiqarāt means spinal vertebrae. AlSūfì mentions that the stars on the Kharazāt (joints) are called alFiqarāt or singularly Fiqra. |
| al-Shawla (the sting) <br> Shawlat al'Aqrab, <br> Shawlat al-Sura <br> al-Ibra | الشولة <br> شولة العقرب <br> شولة السرة <br> الابرة | $\begin{array}{\|l\|} \hline 6527 \\ 6508 \\ \hline \end{array}$ | Al-Sūfī mentions that the two stars on the tip of the tail which are the twentieth and the twenty-first are called al-Shawla. These two are also called Shawlat al- 'Aqrab or Shawlat al-Sura and are also called al-Ibra (the needle). They were called alShawla because they always rise up vertically. They are the nineteenth of the lunar mansions. |

Table 22: Names of stars in constellation Orion as per Arabic folk astronomy.

| Arabic Name | Name in Arabic | Star/s (HR) | Explanation and comments |
| :---: | :---: | :---: | :---: |
| al-Haq 'a | الهقعة | 1879, 1880, 1876 | Al-Şüfi mentioned that this nebula |
| Haq 'a al-Jauz ${ }^{\text {' }}$ | هتعة الجوزاء |  | which resembles the points of the letter Tha (ث). (This letter in |
| al-Tahātū | التحاتي |  | Arabic is written with three points on it.) |
| al-Tahiyat | التحيات |  | Al-Sūfi also mentioned that the Arabs call this nebula by many |


| $\begin{aligned} & \text { al-Tahia } \\ & \text { al-Athāfí } \end{aligned}$ | التحية الاثافي |  | names and that it is the fifth of the lunar mansions. |
| :---: | :---: | :---: | :---: |
| Mankib alJauzā ' <br> Yad al-Jauza' <br> Mirzam al$J a u z \bar{a}{ }^{\prime}$ <br> Rā'ı̄al-Jauzā | منقب الجوزاء <br> يد الجوزاء <br> مرزم الجوزاء <br> راعي الجوزاء | 2061 | Ṣūfī Al mentioned that the second star was called Mankib al-Jauzā and also Yad al-Jauzā'. He also explained that some of the Arabs called it Mirzam al-Jauz $\bar{a}$ ' and this was wrong of them, because it was the practice of the Arabs to begin the name of any bright star by the word Mirzam like the two (stars) Mirzam al-Shi'rayan. (These stars are: al-Shi'ra al-Yamāniya which is the star Sirius and al-Shi'ra alShāmīya which is the star Procyon). Al-Ṣūfĭ also mentioned that the second star was also sometimes called Rā'ī al-Jauzā'. |
| al-Nājid <br> al-Mirzam | الناجد <br> المرزم | 1790 | Al-Șūfī also mentioned that the third star was called al-Nājid and it was also called by al-Mirzam. |
| Mintaqat alJauza' <br> Niṭāq al-Jauz $\bar{a}$ ' <br> al-Niẓām <br> al-Naẓm. <br> Nazm al-Jauz $\bar{a}$ ' <br> Faqār al-Jauzā '. | منطقة الجوزاء <br> نطاق الجوزاء <br> النظام <br> النظم <br> نظم الجوزاء <br> فقار الجوزاء | 1852, 1903, 1948 | Al-Ṣūfì mentioned that the three bright stars on the middle of Orion which are the twenty-sixth, the twenty-seventh and the twentyeight were called collectively as Mințaqat al-Jauzā', Niṭāq alJauzā', al-Nizām and also alNazm. They were also mentioned as Nazm al-Jauza' and Faqār al$J a u z \bar{a}$ '. The separation of the names came later on where by the twenty-sixth is now named 'Mintaka'. The twenty-seventh is named 'Alnilam' which was a derivative from the word al-Nizām. And the twenty-eighth is named 'Alnitak'. |
| al-Laqat <br> Saif al-Jabbār. | اللقط <br> سيف الجبار | 1892, 1897, 1899 | Al-Șūfì mentioned here also that the three stars which are the thirtieth, the thirty-first and the thirty-second were called collectively as al-Laqat and also Saif al-Jabbār (sword of Orion). |
| Rijl al-Jauz $\bar{a}$ ' <br> Rā'ı̄al-Jauzā' <br> al-Nājid | رجل الجوزاء <br> راعي الجوزاء <br> الناجد | 1713 | The thirty-fifth which is the great bright star on the left leg was called Rijl al-Jauzä' (leg of Orion) and also Rā' $\bar{\imath}$ al-Jauz $\bar{a}$ ' (Shepherd of Orion). It was also mentioned by some Arabs that the thirty-fifth which is on the left leg was called al-Nājid. |
| Tāj al-Jauz ${ }^{\prime}$ | تاج الجوزاء | 1676,1638, 1580, | Şūfī Al mentioned that the nine |


| Dhawā’īb alJauzā ${ }^{\prime}$ | ذوايب | $\begin{aligned} & 1570,1544,1543, \\ & 1552,1567,1601 \end{aligned}$ | stars forming a curve that are on the pelt and which are from the seventeenth until the twenty-fifth were called Tāj al-Jauz $\bar{a}$ ' (crown of Orion) and also Dhawā $\bar{\imath} b$ al$J a u z \bar{a}{ }^{\prime}$ (this is the skin of the lion which a hunter usually wraps around his hand). |
| :---: | :---: | :---: | :---: |

Table 23: Names of stars in constellation Centaurus as per Arabic folk astronomy.

| Arabic Name | Name in Arabic | Star/s (HR) | Explanation and comments |
| :---: | :---: | :---: | :---: |
| al-Shamārīkh | الثماريخ |  | The Arabs called both the constellations Centaurus and Lepus by the name of: al-Shamārīkh. |
| Hidāar, al-Wazn, Muḥlifain, Muhnithain | حضار <br> الوزن <br> محليفين <br> محنثين | 5659,5267 | The Arabs called these two stars by these 4 names. However al-Ṣūfĩ was not sure which one of these names referred to which star. |

### 5.11 Comments on the Chapter of the Constellation Ursa Minor

### 5.11.1 The Explanation of ' $F a$ 's al Raḥa '

In this chapter of the constellation Ursa Minor, al-Ṣūfī wrote about an image which was used in Arabic folk astronomy called $F a$ 's al-Rah $\bar{a}$. It is an area which had been compared by the Arabs to the likeness of a fish. It is formed by two rows of stars forming two arcs as al-Ṣūfī explains. The first arc is formed by: "... the three stars on the tail, together with the fourth and sixth form a curved lin." The second arc starts with "... this star is connected with the star on the end of the tail, forming a line of dim stars which is curved like the first line." Al-Ṣūfī then explains that: "... these two arcs enclose an area with the shape of a fish, called al-Fa's; this may be compared with Fa's al-Raha $\bar{a}$, where the pole is in the middle. However, the equatorial pole is on the outside of the second arc, close to the nearest star on the line to the star al-Juday."

Al-Ṣūfi stated here that the pole is located in the middle of the image of this fish. However as an accomplished astronomer, al-Ṣūfī must have known that this is clearly not the case. Therefore the explanation for this matter is that he must have been stating what the Arabs have said about this area or this image of the fish with the pole at its centre. For he then explains: "... the equatorial pole is on the outside of the second arc, close to the nearest star on the line to the star al-Juday." (See below the explanation and location of this (nearest) star)

This explanation of the image of the fish is found in many other books on Arabic folk astronomy. The most important was that of Abū Ḥanīfa al-Daīnawri in his book on al-Anwā’, where he clearly states that the Arabs: "... believe that the pole is in the middle of this image." However alDaīnawri goes on to explain that "... it is not the case for the pole is close to a star next to al-Juday on this curve of dim stars. I found that these stars are the closest stars to the pole. I found that the distance between this star and the pole is less then one degree. However the pole is not a star but a point on the sphere."

Al-Ṣūfì must have known this explanation by Abu Hanifa al-Dinawari because in the introductory chapter of his book he mentioned that the book by Abū Hanīfa al-Daīnawri is the best book on Arabic folk astronomy even though he has some misgivings about the accuracy of some of al-Daīnawri's information and his observational skills. (See translation of al-Ṣūfī introductory chapter)

The below picture (Figure 53) shows the image of the constellation with the two curves forming an image of a fish. The middle red point is the estimated area where the Arabs believed the equatorial pole was located. Even though this point is slightly off center however it is a remarkable achievement to those Arab observers who where able to locate this point in the sky without the aid of any instruments, but only relied on their naked eyes. In Figure 54 the star chart for the constellation Ursa Minor has been re-calculated to the year A.D. 960 taking into account of precession. The nearest visible star to the pole at that time was the star HR 4893 with visual magnitude of 5.28. This star was probably the star mentioned by al-Daīnawri and al-Ṣūfi. The distance between the pole and the star is close to 1 degree. This also shows the remarkable accuracy and observation skills of al-Daīnawri and al-Ṣūfī in identifying almost the precise location of the equatorial pole in that period of time.


### 5.11.2 The Directions for Using the Star Maps as per al-Ṣūfī Explanation

At the end of the chapter on Ursa Minor, al-Ṣūfī explains clearly the reasons why he made two different pictures. He also explains the method of using these maps where he wrote:
"For every constellation we have drawn two pictures: one as it is projected on the globe and the other as it is seen in the heavens. Hence we have covered both of the different cases, so there is no confusion for anyone who sees that what is viewed on the globe is different from what is in the heavens. When we want to see the constellation as it is we lift the book over our heads and we look at the second picture. From beneath we are viewing it as it is seen in the heavens."

It is apparent that as an observational astronomer and an instrument-maker al-Ṣūfī was very much concerned with the accuracy of the data he had and the way it should be used correctly when constructing a celestial globe.

### 5.11.3 Star Names and Modern Designations of the Stars

I have included below in Table 24 all the stars that are included in al-Ṣūfís star tables for constellation Ursa Minor. I have also included the HR, numbers so each star can be correctly identified. The stars' identification are according to Toomer's book. I also tabulated below the names of the stars according to the Arabic tradition and according to what was described by al-Ṣūfī, together with the modern star names and any other common name.

Table 24: Star Names and Modern Designations of the Stars for Ursa Minor Constellation

| Star number <br> (as per al- <br> Şūfi) | HR | Star name and <br> description (as per al- <br> Șūfi) | Star name/s <br> in Arabic <br> tradition | Modern <br> star <br> name/s | Other star <br> name/s |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 1 Ursa minor | 424 | The star on the end of <br> the tail which is al- <br> Juday | al-Juday | Polaris | Alruccabah, <br> Cynosura, <br> Phoenice, <br> Lodestar, Pole <br> Star, <br> Tramontana, <br> Angel Stern, <br> Navigatoria, <br> Star of Arcady, <br> Yilduz, Mismar |
| 2 Ursa minor | 6789 | The one next to it on <br> the tail |  | Yildun | Vildiur, Gildun |
| 3 Ursa minor | 6322 | The one next to that <br> before the place where <br> the tail joins the body |  |  |  |
| 4 Ursa minor | 5903 | The southern most of <br> the stars in the <br> advanced side of the <br> rectangle |  |  |  |
| 5 Ursa minor | 6116 | The northern most of <br> those in the same side |  |  |  |
| 6 Ursa minor | 5563 | The southern star in the <br> rear side which is the <br> brightest of al- <br> Farqadain | Brightest <br> of al- <br> Fargadain | Kocab | Kochab, <br> Kochah |
| 7 Ursa minor | 5735 | The northern one in the <br> same side which is the <br> dimmest of al- <br> Farqadain | Dimmest <br> of al- <br> Farqadain | Pherkad | Pherkad Major |


| 8 Ursa minor | 5430 | The southern star <br> parallel to al-Farqadain |  |  |
| :--- | :--- | :--- | :--- | :--- |

### 5.11.4 Modern Star Chart of Ursa Minor Constellation

In Figure 55 below I have included a modern star chart of Ursa Minor constellation showing the star's modern name, al-Ṣūfī designation number and HR number. The software used to generate above chart is: Cartes du Ciel version 2.76.


### 5.12 Comments on the Chapter of the Constellation Ursa Major

5.12.1 Differences in Coordinates and Magnitudes between Manuscripts Marsh144 and MS 5036

The below table shows the differences in coordinates and magnitude values for the constellation Ursa Major which were identified in the manuscripts Marsh144 and MS5036. These differences were identified and compared with al-Ṣūfí's written description of the constellation. In the comments below I have also referred to other manuscripts, which are: The French translation by Schjellerup which was based on the rather late Copenhagen Manuscript MS83 dated A.D. 1601. The other is the London manuscript OR5323 dated $14^{\text {th }}$ century A.D. The last is the Hyderabad copy which was based on several manuscripts but mainly that of MS5036; however I found that the Hyderabad edition contains many errors which do not make it very reliable.

Table 25: Differences in Coordinates and Magnitudes between Manuscripts.

| Star number (as per alṢūfī) | Lat. Marsh1 44 | Lat. MS 5036 | Mag. Marsh1 44 | Mag. MS <br> 5036 | Explanations and Comments |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 7 Ursa major |  |  | 4.25 | 3.75 | The value in al-Șūfís written description is 4 s while the MS5036 chart shows it as 4 k , however the Marsh144 chart shows it correctly as 4s. |
| 17 Ursa major | 4530 | 4430 |  |  | The value for Lat indicated in Schjellerup French translation (based on the Copenhagen Manuscript MS83) is similar to the MS5036 which is 4430 . |
| 34 Ursa major | 2020 | 2305 |  |  | The value for Lat indicated in Schjellerup French translation is 23 00 which is also a different value but closer to the MS5036 value. This proves that the copy of the Copenhagen manuscript is similar to the MS5036. <br> The London manuscript OR5323 shows the Lat 2020 |

### 5.12.2 Star names and modern designations of the stars

I have included below in Table 26 all the stars that are included in al-Ṣūfî's star tables for constellation Ursa Minor. I have also included the HR, numbers so each star can be correctly identified. The stars identifications are according to Toomer's book. I also tabulated below the names
of the stars according to the Arabic tradition and according to what was described by al-Ṣūfī, together with the modern star names and any other common name.

Table 26: Star Names and Modern Designations of the Stars for Ursa Major

| Star number (as per al-Șūfī) | HR | Star name and description (as per alṢūfi) | Star name/s in Arabic tradition | Modern star name/s | Other star name/s |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 Ursa major | 3323 | The star on the end of the snout. | al-Khatem | Muscida |  |
| 2 Ursa major | 3354 | The more advanced of the two stars in the two eyes. |  |  |  |
| 3 Ursa major | 3403 | The other one of the two. |  |  |  |
| 4 Ursa major | 3576 | The more advanced of the two stars in the forehead. |  |  |  |
| 5 Ursa major | 3616 | The other one of the two. |  |  |  |
| 6 Ursa major | 3771 | The star on the tip of the advance ear. |  |  |  |
| 7 Ursa major | 3624 | The more advanced of the two stars in the neck. |  |  |  |
| 8 Ursa major | 3757 | The other one of the two, longitude or latitude are wrong. |  |  |  |
| 9 Ursa major | 3888 | The northern most of the two stars in the chest. |  |  |  |
| 10 Ursa major | 3894 | The southernmost of them. |  |  |  |
| 11 Ursa major | 3775 | The star on the left knee. |  |  |  |
| 12 Ursa major | 3569 | The northern most of the two in the front left paw. al-Kafza |  | Talitha |  |
| 13 Ursa major | 3594 | The southern most of them. al-Kafza |  |  |  |
| 14 Ursa major | 3662 | The star above the right knee. |  |  |  |
| 15 Ursa major | 3619 | The star below the right knee. |  |  |  |
| 16 Ursa major | 4301 | The star on the back which is part of the quadrilateral. |  | Dubhe | Dubb, al-dubb |
| 17 Ursa major | 4295 | The one on the flank. | al-Mirāq | Merak | Mirak |
| 18 Ursa major | 4660 | The one on the place where the tail joins |  | Megrez | Kaffa in Becvar |


|  |  | the body. |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 19 Ursa major | 4554 | The remaining one on the left hind thigh. |  | Phad | Phecda, Phekda, Phegda, Phekha, Phacd |
| 20 Ursa major | 4033 | The more advanced of the two stars in the left hind paw. al-Kafza |  | Tania Borealis | Al-Kafza al-Thānāa |
| 21 Ursa major | 4069 | The next one. al-Kafza |  | Tania Australis |  |
| 22 Ursa major | 4335 | The star on the left knee bends. |  |  |  |
| 23 Ursa major | 4377 | The northern most of the two stars in the right hind paw. al-Kafza |  | Alula Borealis |  |
| 24 Ursa major | 4375 | The southernmost of them. al-Kafza |  | Alula Australis |  |
| 25 Ursa major | 4905 | The first of the three stars on the tail next to the place where it joins the body. alJaoun | al-Jūn | Aliioth | Alioth, Aliath |
| 26 Ursa major | 5054 | The middle one. alInak | al- 'Anāq | Mizar | Mirzar, Mizat |
| 27 Ursa major | 5191 | The third on the end of the tail. al-Kaed | al-Qā $\bar{i} d$ | Alkaid | Benetnash, Benetnasch, Elkeid |
| 28 Ursa major | 4915 | The star under the tail at some distance towards the south. | Kibd al-Asad |  |  |
| 29 Ursa major | 4785 | The rather faint star in advance of it. |  |  |  |
| 30 Ursa major | 3705 | The southernmost of the two stars between the front legs of Ursa Major and the head of Leo. |  |  |  |
| 31 Ursa major | 3690 | The one north of it. |  |  |  |
| 32 Ursa major | 3800 | The next of the remaining three faint stars. |  |  |  |
| 33 Ursa major | 3809 | The one in advance of this. |  |  |  |
| 34 Ursa major | 3612 | The one in advance again of the latter. |  |  |  |
| 35 Ursa major | 3275 | The star between the front legs (of Ursa Major) and Gemini. |  | Alsciaukat | Mabsuthat |

### 5.12.3 Explanation of al-Ṣūfi's Distance Approximation

Throughout al-Ṣūfi's work the author indicated some measurements, which might seem to be a very general approximation to the measurement of distance between the stars. However, upon careful examination of this method, which was made by Schjellerup in his French translation of al-Ṣufi's book, we can see that these measurements can be almost exactly defined in term of numerical distance values. These values are summarized as follows: one dhirā ${ }^{\prime}=2 \operatorname{deg} 20 \mathrm{~min}$; one Shibr $=1 / 3$ Thira; one Qasba $=1 / 32$ Thira and one Rumh $=14 \mathrm{deg}$. In the comments on the constellation Auriga al-Șūfī clearly mentioned that the value of one dhira' is two degrees and one-third of a degree ( 20 minutes). For example in the constellation Ursa Major al-Ṣūfi mentioned that there are two stars close to the star $a l-Q \bar{a} T \bar{d} d$. The distance between these two stars is one Thira and the distance between the closer of these two to al-Qā $\bar{\imath} d$ is also close to one Thira. These two stars have not been mentioned by Ptolemy. Upon examination we can identify these two stars to be HR5023 and HR5112 and the distance between these two stars is almost 2 degrees and 26 min . The distance between al-Qā $\bar{i} d$ and the closer of these two stars is also a little more then 2 degrees.

### 5.12.4 Modern Star Chart of Ursa Major Constellation

Figure 56 below is a modern Star chart of Ursa Major constellation. The stars indicated in red are the stars according to al-Șūfi's star number. The stars indicated in green are the stars mentioned by alSūfî in his comments but not included in the charts nor are included in Ptolemy. There was no place to include the star's modern name or the HR number for every star in this constellation, therefore I only included al-Șūfì star numbers where the details can be found in the above comments. The software used to generate above chart is Cartes du Ciel version 2.76.


### 5.13 Comments on the Chapter of the Constellation Taurus

### 5.13.1 Star names and Modern Designations of the Stars

I have included below in Table 27 all the stars that are included in al-Ṣūfís star tables for constellation Taurus. I have also included the HR, numbers so each star can be correctly identified. The stars identifications are according to Toomer's book. I also tabulated below the names of the stars according to the Arabic tradition and according to what was described by al-Ṣūfí, together with the modern star names and any other common name.

Table 27: Star Names and Modern Designations of the Stars for Taurus

| Star <br> number (as per al-Ṣūfī) | HR | Star name and description (as per al-Ṣūfī) | Star name/s in Arabic tradition | Modern star name/s | Other star name/s |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 Taurus | 1066 | The northernmost of the 4 stars in the cut-off position. |  |  |  |
| 2 Taurus | 1061 | The one after. |  |  |  |
| 3 Taurus | 1038 | The one after this also. |  |  |  |
| 4 Taurus | 1030 | The southernmost of the 4 . |  |  |  |
| 5 Taurus | 1174 | The one on the rear of these, on the right shoulder blade. |  |  |  |
| 6 Taurus | 1239 | The star in the chest. |  |  |  |
| 7 Taurus | 1320 | The star in the right knee. |  |  |  |
| 8 Taurus | 1251 | The star on the right hock. |  |  |  |
| 9 Taurus | 1473 | The star on the left knee. |  |  |  |
| 10 Taurus | 1458 | The star on the left lower leg. |  |  |  |
| 11 Taurus | 1346 | The star on the nostrils in the face looks like the letter ( $\Delta$ ) $D \bar{a} l$ from the books of the Greeks. |  | Hyadum I |  |
| 12 Taurus | 1373 | The one between this and the northern eye. |  | Hyadum II |  |
| 13 Taurus | 1411 | The one between it and the southern eye. |  |  |  |
| 14 Taurus | 1457 | The bright star the reddish one of the letter ( $\Delta$ ) al-Dāl on the southern eye and it is Aldebaran. | al- <br> Dabarān <br> or <br> Ain al- <br> Thawr | Aldebaran | Cor Tauri, Parilicium |
| 15 Taurus | 1409 | The remaining one on the northern eye. |  | Ain |  |
| 16 Taurus | 1547 | The star on the place where the southern horn and the ear join the head. |  |  |  |


| 17 Taurus | 1656 | The southernmost of the 2 stars in the southern horn |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 18 Taurus | 1658 | The northernmost of these |  |  |
| 19 Taurus | 1910 | The star on the tip of the southern horn |  |  |
| 20 Taurus | 1497 | The star on the northern horn triangle. |  |  |
| Ptolemy 21 not included in al-Ṣūfī |  | "The star on the tip of the northern horn is the same star as the one on right leg of the constellation Auriga." |  |  |
| 21 Taurus (=Ptolemy 22) | 1392 | The northernmost of the 2 stars close together in the northern ear. | al-Kalbain |  |
| 22 Taurus | 1387 | The southern of them. The latitude as seen in the sky should be 0000 . | al-Kalbain |  |
| 23 Taurus | 1256 | The more advanced of the 2 small stars in the neck. |  |  |
| 24 Taurus | 1329 | The rearmost of them. Its latitude should be southerly because in the sky it is so. |  |  |
| 25 Taurus | 1287 | The quadrilateral in the neck, the southernmost star on the advanced side. |  |  |
| 26 Taurus | 1269 | The northernmost star on the advanced side. |  |  |
| 27 Taurus | 1369 | The southernmost star on the rear side. |  |  |
| 28 Taurus | 1348 | The northernmost one on the rear side. |  |  |
| 29 Taurus | 1145 | The Pleiades: the northern end of the advanced side. |  | Taygeta |
| 30 Taurus | 1156 | The southern end of the advanced side. |  | Merope |
| 31 Taurus | 1178 | The rearmost and narrowest end of the Pleiades. |  | Atlas |
| 32 Taurus | 1188 | The small star outside the Pleiades towards the north. |  |  |
| 33 Taurus | 1101 | The star under the right foot and the shoulder blade. |  |  |
| 34 Taurus | 1620 | The most advanced of the 3 stars over the southern horn. |  |  |
| 35 Taurus | 1739 | The middle one of the three. |  |  |
| 36 Taurus | 1810 | The rearmost of them |  |  |
| 37 Taurus | 1946 | The northernmost of the 2 stars under the southern tip of the southern horn. |  |  |
| 38 Taurus | 1985 | The southernmost of them. |  |  |
| 39 Taurus | 1875 | The most advanced of the 5 |  |  |


|  |  | stars under the northern <br> horn. |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 40 Taurus | 1928 | The one to the rear of this. |  |  |  |
| 41 Taurus | 2002 | The one to the rear again of <br> the latter. |  |  |  |
| 42 Taurus | 2034 | The northernmost of the <br> remaining rearmost 2. |  |  |  |
| 43 Taurus | 2084 | The southernmost of these <br> two. |  |  |  |

### 5.13.2 The Explanation of 'al-Dayīqa'.

At the end of this chapter on the constellation Taurus, al-Șūfì wrote about a location in the sky that the Arabs called al-Daȳ̄qa which means 'the small gap' in Arabic. He dedicated almost two pages on this topic which might seem from first sight that it is a very important topic in traditional Arabic astronomy. However I believe that there are many astronomical concepts that the author tried to explain using this topic as an example in order confirm his scientific capability. The case below is an exercise in the idea 'Oblique Ascensions' which was a well-known concept in ancient and classical Greek astronomy. Therefore I will try here to analyze al-Ṣūfí's comments in order to identify some of these scientific astronomical ideas.

Al-Ṣūfì started by explaining that there are two close stars on the northern ear, and these stars are the twenty-first (HR1392) and the twenty-second (HR1387) which were called al-Kalbain (the two dogs). He then states that many Arab scholars narrate that these two stars are called al-D.ayīqa because they believed that when the Moon slows down it stays in that location. However, he completely rejects this idea and states that this is wrong. He then explains in detail the reason why by saying that: "... the stars of al-Thurayyā are fifteen degrees of Taurus and these two stars are twentyfour and a half degrees of it. The distance between them and al-Thurayyā is nine degrees and the least amount the Moon travels in one day and one night when its is moving slowest and its most distance (from the Earth), is eleven degrees." Here we have several ideas which need further explanation. The Moon could not travel from al-Thurayyā directly to these two stars in the same or next day even when it is in its slowest and further orbit from the Earth. By this picture al-Ṣūfī explains several facts about the path and orbit of the Moon. First is that path of the Moon can be higher than the ecliptic. In the comments about the constellation Scorpio he explains that it is can reach up to five degrees further then the ecliptic. The other idea is that the orbit of the Moon is variable and the least amount the Moon travels in one day is eleven degrees. As al-Ṣūfí's work was based on Ptolemy's then it is safe to assume that he was well aware of the Ptolemy's epicycle and deferent system and the concept of the variable distance of the Earth and the Moon and the variable apparent speed of the Moon as well as
the concept of the 'Oblique Ascensions'. As we can see in Figure 57, which shows Ptolemy's epicycle and deferent system, it is clear that the Moon-Earth distance varies depending on the time and position of the Moon in epicycle.


Figure 57 Ptolemy's epicycle and deferent system

Next al-Ṣūfī explains that al-Dayīqa is the area or gap between al-Thurayyā and al-dabarān and not the two stars. He further explains that because the Arabs use al-Anw $\bar{a}$ ' folk tradition this is why this area was called al-Daȳ̄qa. Al-Ṣūfī explains that al-Anwā' or Naw' "... is when a star sets in the west at dawn and when its Raqīb [companion star] rises in the east from under the light [of the Sun]. The Raqīb of each one is the fifteenth star [of the lunar mansions]." The Naw' of a star had been an area of controversy between Arab scholars on whether it is the rise or fall of a star. However, alSūūi here confirms that the Naw' of a star is not the rise but the fall of a star in the west at dawn. (Further explanations on $a l-A n w \bar{a}$ ' and lunar mansions are to be in the chapter on Arabic Folk astronomy)

Al-Șūfì then tries to go into detail on why this area or gap was called thus. His explanation is quite clear where he says that: "The middle of al-Thurayy $\bar{a}$ is on the fifteen degrees of Taurus and aldabarān is on the twenty five degree of it. The distance on the degrees of the zodiac between them is ten degrees. However the latitude of al-Thurayyā in the north from its (zodiac) degrees is four degrees and few minutes. And the latitude of al-dabarān in the south is five degrees. And it is in the nature of the northern stars to rise before their (zodiac) degree rise and set after their (zodiac) degrees set, and the southern (stars) rise after their (zodiac) degree rise and set before their (zodiac) degrees set. Therefore al-Thurayy $\bar{a}$ approximately rises at thirteen degrees of Taurus and al-dabarān rises at twenty seven of it. Thereby the degrees between the rise of al-Thurayy $\bar{a}$ and al-dabarān are approximately fourteen degrees of the degrees of the zodiac and eleven degrees and a few minutes from the horizon in this third zone. And al-Thurayy $\bar{a}$ sets at seventeen degrees of Taurus because it sets after its zodiac degree. And al-dabarān sets at twenty three degrees of it because it sets before its zodiac degrees. Thereby the degrees between the setting of al-Thurayy $\bar{a}$ and al-dabarān are six
degrees of the degrees of the zodiac and seven degrees from the horizon in this zone. The degrees of Taurus sets at the same time as the degrees of Scorpio rise. When they found between the setting of al-Thurayyā and al-dabarān this amount they called this gap between them al-Ḍayīqa." I have made below two diagrams in order to help explain the concept of the 'Oblique Ascensions' and what al-Ṣūfī was trying to convey. The first is Figure 58 shows the position and rising of al-Thurayy $\bar{a}$ and aldabarān on May 13 at dawn in the east at the time of al-Ṣūfi. The second is Figure 59 shows the position and setting of al-Thurayyā and al-dabarān on November 13 at dawn in the west at the time of al-Ṣūfi. This is the Naw' of the al-Thurayyā and al-dabarān. We can see from below that because the Arabs considered the Naw' of a star as the setting at dawn and that the distance from the horizon between al-Thurayy $\bar{a}$ and al-dabarān is small (only 7 degrees) then they called this small gap alDayīqa which means 'the small or narrow gap' in Arabic. This is one important examples in which alSufi was trying to combine Greek astronomy with Arabic traditional astronomy.


One last idea which al-Ṣūfì mentioned in this section is the Third Zone. This was the concept of dividing the Earth into climes or zones which were called clima, plural climata or klimata which in Greek means 'inclination'. However there seems to have been some dispute among ancient Greek scholars as to the exact number or arrangement of these zones. According to Strabo the concept of the division of the Earth into zones began as early as the 6 th century B.C. with a Greek scholar named Permenides of Elea. The number of zones accepted by Strabo was five, and he criticizes another scholar Polybius for making the number six. The five zones accepted by Strabo were as follows: the uninhabitable Torrid Zone lying in the region of the equator; a zone on either side of this extending to
the tropic; and then the temperate zones extending in either direction from the tropic to the arctic regions. However Ptolemy in his Geography divided the northern temperate zone into seven zones. This division in seven zones may go back to notions of geography predating the idea of a spherical Earth introduced by Pythagoras in the 6th century BC. Medieval Arabs and Persian scholars such as al-Bīrūnī, al-Idrīsī as well as al-Ṣūfī adopted Ptolemy's system of seven climes and divided the latitudes of the Earth into seven habitable zones starting from the equator. According to al-Bīrūn̄̄ the third zone is from latitude 27 to 33 degrees hence the middle of this zone is at latitude 30 deg. Therefore, according to al-Ṣūfî's comments these observations have been made in the third zone, most probably in the city of Shiraz (Latitude: 29.53. Longitude: 52.58). This confirms the historical record which mentions that al-Ṣūfi has conducted his astronomical observations or maybe constructed an observatory in Shiraz.

### 5.13.3 Modern Star chart of Taurus constellation

Figure 60 below is a modern Star chart of Constellation Taurus. The stars indicated in red are the stars according to al-Ṣūfî's star number. The stars indicated in green are the stars mentioned by al-Ṣūfî in his comments but not included in the charts nor are included in Ptolemy. There was no place to include the star's modern name or the HR number for every star in this constellation, therefore I only included al-Șūfī star numbers where the details can be found in the above comments. The software used to generate above chart is Cartes du Ciel version 2.76.


### 5.14 Comments on the Chapter of the Constellation Scorpio

### 5.14.1 Star Names and Modern Designations of the Stars

I have included below in Table 28 all the stars that are included in al-Ṣūfī's star tables for constellation Scorpio. I have also included the HR, numbers so each star can be correctly identified. The stars identifications are according to Toomer's book. I also tabulated below the names of the stars according to the Arabic tradition and according to what was described by al-Ṣūfī, together with the modern star names and any other common name.

Table 28: Star Names and Modern Designations of the Stars for Scorpio

| Star number (as per alṢūfī) | HR | Star name and description (as per al-Ṣūfī) | Star name/s in Arabic tradition | Modern star name/s | Other star name/s |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 Scorpio | 5984 | The northernmost of the 3 bright stars on the forehead. | al-Iklīl | Graffias | Grafias, Grassias, Acrab, Akrab, Elacrab |
| 2 Scorpio | 5953 | The middle one of these. | al-Iklīl | Dschubba | Iclarkrau |
| 3 Scorpio | 5944 | The southernmost of the three. | al-Iklīl |  |  |
| 4 Scorpio | 5928 | The star south again of this on one of the legs. |  |  |  |
| 5 Scorpio | 6027 | The southernmost of the 2 stars adjacent to the northernmost of the three bright one. |  | Jabbah |  |
| 6 Scorpio | 5993 | The southernmost of these. |  |  |  |
| 7 Scorpio | 6084 | The most advanced of the 3 bright stars in the body. | al-Nīyāt | Alniyat |  |
| 8 Scorpio | 6134 | The middle one of these which is reddish and called Qalb al- 'Aqrab (Antares). | -al-Qalb <br> (the heart) <br> -Qalb al- <br> 'Aqrab | Antares | Cor Scorpii, Qalb al Aqrab, Vespertilio |
| 9 Scorpio | 6165 | The rearmost of the 3 . | al-Nìyāt |  |  |
| 10 Scorpio | 6028 | The advanced star of the 2 under these approximately on the last leg. |  |  |  |
| 11 Scorpio | 6070 | The rearmost of these. |  |  |  |
| 12 Scorpio | 6241 | The star in the first tail joint from the body. | al-Fiqra |  |  |
| 13 Scorpio | 6247 | The one after this in the $2^{\text {nd }}$ joint. | al-Fiqra |  |  |
| 14 Scorpio | 6262 | The northern star of alMud' 'af (the double star) in the $3^{\text {rd }}$ joint. | al-Fiqra |  |  |
| 15 Scorpio | 6271 | The southern star of the double star. | al-Fiqra |  |  |
| 16 Scorpio | 6380 | The one following in the $4^{\text {th }}$ joint. | al-Fiqra |  |  |


| 17 Scorpio | 6553 | The one after that in the $5^{\text {th }}$ joint. | al-Fiqra | Sargas |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 18 Scorpio | 6615 | The next one again in the $6^{\text {th }}$ joint. | al-Fiqra |  |  |
| 19 Scorpio | 6580 | The star in the $7^{\text {th }}$ joint the joint next to the sting. | al-Fiqra |  |  |
| 20 Scorpio | 6527 | The rearmost of the 2 stars in the sting. | -al-Shawla (the sting) -Shawlat al- 'Aqrab -Shawlat al-Sura -al-Ibra | Shaula |  |
| 21 Scorpio | 6508 | The more advanced of these. | -al-Shawla (the sting) -Shawlat al-'Aqrab -Shawlat al-Sura -al-Ibra | Lesath | Lesuth |
| 22 Scorpio | 6475 | The nebulous star to the rear of the sting. |  | M7 |  |
| 23 Scorpio | 6492 | The most advanced of the 2 stars to the north of the sting. |  |  |  |
| 24 Scorpio | 6616 | The rearmost of them. |  |  |  |

### 5.14.2 Modern Star Chart of Constellation Scorpio

Figure 61 below is a modern Star chart of Constellation Scorpio. The stars indicated in red are the stars according to al-Ṣūfi's star number. The stars indicated in green are the stars mentioned by al-Şūfĭ in his comments but not included in the charts nor are included in Ptolemy. There was no place to include the star's modern name or the HR number for every star in this constellation, therefore I only included al-Sūfī star numbers where the details can be found in the above comments. The software used to generate above chart is Cartes du Ciel version 2.76 .


Figure 61: Modern Star Chart of Scorpio Constellation

### 5.15 Comments on the Chapter of the Constellation Orion

### 5.15.1 Star Names and Modern Designations of the Stars

I have included below in Table 29 all the stars that are included in al-Ṣūfî's star tables for constellation Scorpio. I have also included the HR, numbers so each star can be correctly identified. The stars identifications are according to Toomer's book. I also tabulated below the names of the stars according to the Arabic tradition and according to what was described by al-Ṣūfi, together with the modern star names and any other common name.

Table 29: Star Names and Modern Designations of the Stars for Orion

| Star number (as per al-Ṣūfī) | HR | Star name and description (as per alṢūfi) | Star name/s in Arabic tradition | Modern star name/s | Other star name/s |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 Orion | $\begin{aligned} & \hline 1879 \\ & 1880 \\ & 1876 \end{aligned}$ | The nebulous star in the head of Orion, which are the three close stars. | -al-Haq'a <br> -Haq'a al-Jauzā ' <br> - al-Tahātū, <br> -al-Tahiyat <br> - al-Tahia <br> - al-Athāfí | Meissa | Heka |
| 2 Orion | 2061 | The bright reddish star on the right shoulder. | -Mankib al-Jauzä' <br> -Yad al-Jauzä <br> -Mirzam al-Jauzā | Betelgeuse | Betelguex, Beteiguex, Betelgeuze, Al Mankib |
| 3 Orion | 1790 | The star on the left shoulder. | $\begin{aligned} & \text {-al-Nājid } \\ & \text {-al-Mirzam } \end{aligned}$ | Bellatrix | Amazon Star, the |
| 4 Orion | 1839 | The one under this to the rear. |  |  |  |
| 5 Orion | 2124 | The star on the right elbow. |  |  |  |
| 6 Orion | 2241 | The star on the right forearm. |  |  |  |
| 7 Orion | 2199 | The quadrilateral in the right hand: The rear, double star on the southern side. |  |  |  |
| 8 Orion | 2159 | The advanced star on the southern side. |  |  |  |
| 9 Orion | 2223 | The rear one on the northern side. |  |  |  |
| 10 Orion | 2198 | The advanced one on the northern side |  |  |  |
| 11 Orion | 2047 | The more advanced of the 2 stars in the staff. |  |  |  |
| 12 Orion | 2135 | The rearmost of them. |  |  |  |


| 13 Orion | 1934 | The rearmost of the 4 stars almost on a straight line just over the back. |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 14 Orion | 1872 | The one in advanced of this. |  |  |  |
| 15 Orion | 1842 | The one in advanced again of this. |  |  |  |
| 16 Orion | 1811 | The last and most advanced of the 4 |  |  |  |
| 17 Orion | 1676 | The stars in the pelt on the left arm: The northernmost. | -Tāj al-Jauzā -Dhawā îb alJauz $\vec{a}^{\prime}$ |  |  |
| 18 Orion | 1638 | The $2^{\text {nd }}$ from the northernmost. | -Tāj al-Jauzā |  |  |
| 19 Orion | 1580 | The $3^{\text {rd }}$ from the northernmost. | -Dhawā $\bar{i} b$ alJauzā' |  |  |
| 20 Orion | 1570 | The $4^{\text {th }}$ from the northernmost. | -Tāj al-Jauzā |  |  |
| 21 Orion | 1544 | The $5^{\text {th }}$ from the northernmost. | -Dhawā $\bar{\imath} b$ alJauza' |  |  |
| 22 Orion | 1543 | The $6^{\text {th }}$ from the northernmost. | -Tāj al-Jauzā |  |  |
| 23 Orion | 1552 | The $7^{\text {th }}$ from the northernmost. | -Dhawā īb alJauzā |  |  |
| 24 Orion | 1567 | The $8^{\text {th }}$ from the northernmost. | -Tāj al-Jauzā |  |  |
| 25 Orion | 1601 | The last and the southernmost of those in the pelt. | -Dhawā $\overline{\text { Th }}$ b alJauzā' |  |  |
| 26 Orion | 1852 | The most advanced of the 3 stars on the belt. | Mintaqat alJauzā | Mintaka |  |
| 27 Orion | 1903 | The middle one. | al-Nizām <br> al-Nazm. <br> Naztm al-Jauzā ${ }^{\prime}$ | Alnilam | Alnihan, Alnitam |
| 28 Orion | 1948 | The rearmost of the three. | Nitāq al-Jauzä ${ }^{\prime}$ | Alnitak | Alnitah |
| 29 Orion | 1788 | The star near the handle of the sward. |  |  |  |
| 30 Orion | 1892 | The northernmost of the 3 stars joined together at the tip of the dagger. | al-Laqat Saif al-Jabbār |  |  |
| 31 Orion | 1897 | The middle one. | al-Laqat <br> Saif al-Jabbār |  |  |
| 32 Orion | 1899 | The southernmost of the three. | al-Laqat Saif al-Jabbār | Nair al Saif | Hatysa in Becvar |
| 33 Orion | 1937 | The rearmost of the 2 stars under the tip of the sward. |  |  |  |


| 34 Orion | 1855 | The more advanced of them. |  | Thabit | Tabit |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 35 Orion | 1713 | The bright star in the left foot, which is (applied in) common to the water (of Eridanus). | -Rijl al-Jauzä' -Rā’̄̄ al-Jauzā -al-Nājid | Rigel | Algebar, Elgebar |
| 36 Orion | 1735 | The star to the north of it in the lower leg over the ankle-joint. |  |  |  |
| 37 Orion | 1784 | The star under the left heel outside. |  |  |  |
| 38 Orion | 2004 | The star under the right rear knee. |  | Saiph |  |

### 5.15.2 Modern Star Chart of Constellation Orion

Figure 62 below is a modern Star chart of Constellation Scorpio. The stars indicated in red are the stars according to al-Șūfi's star number. The stars indicated in green are the stars mentioned by alSūfī in his comments but not included in the charts nor are included in Ptolemy. There was no place to include the star's modern name or the HR number for every star in this constellation, therefore I only included al-Șūfí star numbers where the details can be found in the above comments. The software used to generate above chart is Cartes du Ciel version 2.76.


### 5.16 Comments on the Chapter of the Constellation Centaurus:

### 5.16.1 Star names and modern designations of the stars:

I have included below in Table 30 all the stars that are included in al-Ṣūfîs star tables for constellation Scorpio. I have also included the HR, numbers so each star can be correctly identified. The stars identifications are according to Toomer's book. I also tabulated below the names of the stars according to the Arabic tradition and according to what was described by al-Ṣūfí, together with the modern star names and any other common name.

Table 30: Star Names and Modern Designations of the Stars for Centaurus

| Star number (as per alṢūfī) | HR | Star name and description (as per alȘūfī) | Star name/s in Arabic tradition | Modern star name/s | Other star name/s |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 Centaurus | 5192 | The southernmost of the 4 stars in the head. |  |  |  |
| 2 Centaurus | 5221 | The northernmost of them. |  |  |  |
| 3 Centaurus | 5168 | The more advanced of the other, middle 2. |  |  |  |
| 4 Centaurus | 5210 | The rearmost of these, the last of the 4. |  |  |  |
| 5 Centaurus | 5028 | The star on the left advanced shoulder. |  |  |  |
| 6 Centaurus | 5288 | The star on the right shoulder. |  | Menkent |  |
| 7 Centaurus | 5089 | The star on the left shoulder-blade. |  |  |  |
| 8 Centaurus | 5367 | The four stare in the thyrsus. <br> The northernmost of the advanced 2. |  |  |  |
| 9 Centaurus | 5378 | The southernmost of these. |  |  |  |
| 10 Centaurus | 5485 | The one of the other two which is at the tip of the thyrsus. |  |  |  |
| 11 <br> Centaurus | 5471 | The last one south of the latter. |  |  |  |
| $12$ <br> Centaurus | 5190 | The most advanced of the 3 stars in the right side. |  |  |  |
| $13$ <br> Centaurus | 5193 | The middle one. |  |  |  |
| 14 Centaurus | 5248 | The rearmost of the three. |  |  |  |
| $15$ <br> Centaurus | 5285 | The star on the right upper arm. |  |  |  |
| 16 | 5440 | The star on the right |  |  |  |


| Centaurus |  | forearm. |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & 17 \\ & \text { Centaurus } \end{aligned}$ | 5576 | The stars on the right hand. |  |  |  |
| $18$ <br> Centaurus | 5231 | The bright star in the place where the human body joins the horse. |  |  |  |
| $\begin{aligned} & \hline 19 \\ & \text { Centaurus } \end{aligned}$ | 5260 | The rearmost of the 2 faint stars to the north of this. |  |  |  |
| $\begin{aligned} & 20 \\ & \text { Centaurus } \end{aligned}$ | 5249 | The more advanced of them. |  |  |  |
| $21$ <br> Centaurus | $\begin{aligned} & \text { NGC } \\ & 5139 \end{aligned}$ | The star on the place where the back joins the horse body. |  |  |  |
| $\begin{aligned} & \hline 22 \\ & \text { Centaurus } \end{aligned}$ | 4940 | The star in advanced of this on the horse back. |  |  |  |
| $\begin{aligned} & 23 \\ & \text { Centaurus } \end{aligned}$ | 4819 | The rearmost of the stars on the rump. |  |  |  |
| $24$ <br> Centaurus | 4802 | The middle one. |  |  |  |
| $25$ <br> Centaurus | 4743 | The most advanced of the three. |  |  |  |
| $\begin{aligned} & 26 \\ & \text { Centaurus } \end{aligned}$ | 4621 | The more advanced of the 2 stars close together on the right thigh. |  |  |  |
| $\begin{aligned} & \hline 27 \\ & \text { Centaurus } \end{aligned}$ | 4638 | The rearmost of them. |  |  |  |
| $\begin{aligned} & 28 \\ & \text { Centaurus } \end{aligned}$ | 5172 | The star in the chest under the horse armpit. |  |  |  |
| $\begin{aligned} & 29 \\ & \text { Centaurus } \end{aligned}$ | 5132 | The more advanced of the 2 stars under the belly. |  |  |  |
| $\begin{aligned} & \hline 30 \\ & \text { Centaurus } \end{aligned}$ | 5141 | The rearmost of them (Ptolemy) mentioned that it is of the $3^{\text {rd }}$ magnitude however there is no star in this are which can be seen. |  |  |  |
| $\begin{aligned} & 31 \\ & \text { Centaurus } \end{aligned}$ | 4763 | The star on the kneebend of the right hind leg. |  | Gacrux |  |
| $32$ <br> Centaurus | 4853 | The star in the hock of the same leg. |  | Becrux |  |
| $\begin{aligned} & 33 \\ & \text { Centaurus } \end{aligned}$ | 4656 | The star under the knee-bend of the left hind leg. |  |  |  |
| $34$ <br> Centaurus | 4730 | The star on the frog of the hoof on the same leg. |  | Acrux |  |
| $\begin{aligned} & 35 \\ & \text { Centaurus } \end{aligned}$ | 5459 | The star on the end of the right front leg. | Rijl Qantūris Hiḍār, Al-Wazn, | Rigil <br> Kentaurus |  |


|  |  |  | Muhlifain, Muhnithain, |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $36$ <br> Centaurus | 5267 | The star on the knee of the left front leg. | Hiḍār, Al-Wazn, Muḥlifain, Muhnithain | Agena |  |
| $37$ <br> Centaurus | 4898 | The star outside under the right hind leg. |  |  |  |

### 5.16.2 Modern Star Chart of Constellation Centaurus

Figure 63 below is a modern Star chart of Constellation Scorpio. The stars indicated in red are the stars according to al-Ṣūfís star number. The stars indicated in green are the stars mentioned by alṢūfĭ in his comments but not included in the charts nor are included in Ptolemy. There was no place to include the star's modern name or the HR number for every star in this constellation, therefore I only included al-Ṣūfī star numbers where the details can be found in the above comments. The software used to generate above chart is Cartes du Ciel version 2.76.


Figure 63: Modern Star Chart of Centaurus Constellation

## 6. Conclusion

Late one evening in the summer of A.D. 960 the 57 year old Persian astronomer 'Abd alRaḥmān al-Ṣūfī was in the presence of the Buwayhid ruler, 'Aḍud al-Dawla in the city of Shiraz. He wrote that "The grand prince "Aḍud al-Dawla, was visited by a renowned scholar while I was in his presence. The prince asked the astronomer about some of the known stars in the sky..." To his surprise the scholar was not able to distinguish between these stars correctly. He continued:
"...when I saw that all these people who were well known and are leaders in this science so that people follow them and use their books without knowing the right from wrong ...I found in their books many errors especially in the books of $a l-A n w \bar{a}^{\prime}$ and the stories which they obtained from the Arabs ...the lunar mansions and the rest of the stars ...I wanted many times to reveal this and expose it but I either felt sluggish or I had many things which occupied me from this task until God honored me with serving the benevolent king 'Aḍud al-Dawla. "

How could 'Abd al-Raḥmān al-Ṣūfī know that his book which was completed four years later in A.D. 964 was to become one of the most important medieval Arabic treatises in astronomy? This book was Șuwar al-Kawākib al-Thamāniyah wa-al-Ārba'een which was later known as The Book of the Fixed Stars. As we have seen in this study, this major work contained an extensive star catalogue, which lists star coordinates and magnitude estimates, as well as detailed star charts. It also included other topics such as the descriptions of stars, nebulae, and a good summary on old Arabic folk astronomy. My journey to discover this book has been as fascinating as the results, which came out of this effort.

I have begun this study by giving a general account on the key elements of Arabic and Islamic astronomy. I started the first chapter of this study with the history of ancient astronomy going on to the development of Babylonian astronomy. Then I made a brief description on the contribution of Greek astronomers leading up to Arabic and Islamic Astronomy. I also gave a general description on the Greek cosmological concept of the geocentric universe and the development of the Ptolemaic system with Deferent and Epicycle. Then I gave a brief history of the Arabic and Islamic empire from its early start to its golden age, as well as the main events, which shaped the development of science and astronomy during that time.

However in order to understand al-Șūfís work it was important to understand some of the general characteristics of Arabic and Islamic astronomy. I started chapter 2.2 by giving a brief background on the religion of Islam and its contribution to the development of science and Astronomy. The effect of this religion was evident in al-Șūfi's work as well as in many other works during that period. The Greek cosmological geocentric model, where by the Earth is a sphere which lies at the center of a spherical heaven, was accepted as correct for over a thousand years by almost all Arabic and Islamic astronomers. The culmination of the Arab and Islamic science of astronomy was in the development of the astronomical tradition called $a l-Z \bar{i} j$. These were astronomical tables based on trigonometric and mathematical techniques. In this chapter I included a general account on observatories and astronomical instruments, which were used by al-Ṣūfī as well as by many other Arab astronomers of his time.

The third chapter of this section deals with old Arabic astronomical tradition. The lunar astronomical tradition was an important tool used by these old Arabs. This was merged with a form of astrological-meteorological experience that came to be known as the $A n w \bar{a}$. This system was used to predict the weather and to identify the beginning of the seasons in order to specify the dates of festivals, holidays, pilgrimage and the best times for traveling and commerce. In order to systemize this lunar motion, the Arabs divided the apparent path of the Moon in the sky into 28 divisions. These 28 divisions are called "Manāzil al-Qamar" or the Lunar Mansions.

The final chapter in part 2 of this thesis is a brief study on Ptolemy and his book called the Almagest which is a mathematical as well as an astronomical treatise, detailing the motions of the Stars, the Sun, the Moon and the five known planets at that time. The Almagest includes a catalog with descriptions, positions and magnitudes for 1022 stars grouped into 48 constellations for the epoch of A.D. 137. This work became the standard star catalogue used in the Western, Arab and Islamic worlds for over a thousand years.

In Part 3 of this thesis I started the first chapter with a brief biography on 'Abd al-Raḥmān al-Șūfi. However I was surprised that very little was known about al-Ṣūfi's life and career. From several important Arabic historical references I found that al-Şūfi's full name was: Abd al-Raḥmān, Ibn 'Umar, Ibn Muḥammad, Ibn Sahl, al-Rāz̄̄, known as Abū alHeusaīn al-Ṣūfì. I also found that al-Șūfì was born on Saturday the $14^{\text {th }}$ of Muharram in the year A.H. 291 which corresponds to the $6^{\text {th }}$ of December in 903 . He died on Tuesday the $13^{\text {th }}$ of Muharram in the year A.H. 376 which corresponds to $25^{\text {th }}$ of May 986. I have also deduced several facts on al-Șūfi's life such as: The title of "al-Rāzz$\vec{\imath}$ " which meant that he is from the
city of Rayy, south east of the modern city of Tehran. Al-Ṣūfī was also a Persian not an Arab even though he wrote all his works in Arabic. The location of his death in not known, but most probably it was in Shiraz. From the introductory chapter of his work we know that he lived most of his life between the provinces of Rayy and Fars and in the cities of Rayy, Isfahan and Shiraz. In his work al-Șūfì wrote that he made his observations in Shiraz where he established his observatory. He also wrote that he visited Daīnawar, which is the home of the famous scholar and astronomer Abu Hanīfa al-Daīnawari. He also visited Isfahan to research a celestial globe constructed by another important astronomer of that period.

In this chapter I made a brief study on the political and social background of this period in order to understand the impact of the events which helped mould the life of our author. Al-Ṣūfì was born in the beginning of the $10^{\text {th }}$ century. From the time line of al-Ṣūfís life we saw that he lived throughout most of the rule of the Buwayhid rulers. However the most significant scientific contributions of al-Ṣūfī were made during the reign of 'Aḍud alDawla who was one of the strongest of these rulers. The Book of the fixed stars was dedicated to 'Aḍud al-Dawla. However al-Sūūī also dedicated other books to other members of the Buwayhid dynasty. The title of $S \bar{u} \bar{f} i \bar{i}$ signifies that this person was part of an Islamic religious order. Since al-Ṣūfī was given this religious honorary title then we assume that he must have been influenced by such $S$ ūfì movements during his time.

In his book al-Ṣūfì mentioned several important individuals. He also mentioned some of their works, which he commented upon and sometimes criticized in the introductory chapter of his work. The main person who was mentioned by al-Ṣūfī was of course Ptolemy. Al-Ṣūfĩ refers to Ptolemy 119 times in his Book. The other two main characters, which were frequently mentioned in al-Ṣūfîs work, were al-Battānī and Abu Hanīfa al-Daīnawari. AlṢūfī criticized al-Battānī by stating that his star catalog is but a copy of Ptolemy's Almagest only with the correction for Precession. As for Abu Hanīfa al-Daīnawari he was another famous Persian scholar of the $10^{\text {th }}$ century. Al-Ṣūfì considered al-Daīnawari's work on Arabic Astronomical Tradition, called (Kitab al-Anw $\bar{a}$ ') or the Book on Anw $\bar{a}$ ' to be the best written book on this subject. However al-Ṣūfī again criticized al-Daīnawari for his knowledge of the stars and their movements. In the second chapter 3.2 of this thesis I made a brief biographical study on all those individuals who were mentioned in al-Ṣūfís book.

In chapter 3.3 I made a brief survey on all the works which were known to have been written by al-Ṣūfì. The first is, the Book of the Fixed Stars, which was al-Ṣūfî's most famous work and the topic of this study. The second is Kitāb al-Urjūza fi al-Kawākib al-Thābitah Muṣawaran. This is a Poem on the fixed stars. Some historians attributed this poem to al-Ṣūfì
however this poem was probably written by al-Șūfi's son and not by al-Ṣūfĩ himself. Then we have Kitāb al-Tathkira wa Matāreh al-Shu'a' or The Book of Information and Projection of the Rays. Unfortunately it is no longer extant today. Al-Ṣūfī also wrote Kitāb al-Madkhal Fi 'Ilm al-Āḥkām (Introductory Book to the Science of Astrology), Fi Sharh al- 'Amal bi al-Kura (On the Explanation of the Use of the Celestial Globe) and Kitāb al-'Amal bi al-Isterlāb (Book on using the Astrolabe). Finally there is al-Zīj al-Şūfi. This $Z \bar{j} j$ was mentioned by several important Arabic astronomers such as Ibn Yūnus in Cairo and Ibn-Ezra. Unfortunately it is also no longer extant.

Al-Șūfi mentioned in his Book that the observations he made were from the city of Shiraz, which is located south of Iran (Latitude: 29:53 and Longitude: 52:58). Al-Ṣūfī mentioned that the instrument, which was utilized for his observations, was an equatorial ring with a diameter of 250 cm , having a 5 min subdivision on its scale. This instrument was considerable in size and was thus called the Aḍudi Ring after the ruler Aḍud al-Dawla. He mentioned that it was used to determine the latitude of the city of Shiraz to be: 29 deg and 36 min. One of the Arabic historical references mentions that in 1043 there used to be in the Cairo library a celestial globe made of silver that was constructed by al-Ṣūfì for Aḍud alDawla. The weight of this globe was three hundred dirhams and it was purchased for three thousand dinars. Unfortunately this instrument is no longer available today. From the few available treaties written by al-Șūfī on the Astrolabe and the celestial Globe and from the available historical records, we know that al-Șūfì measured the obliquity of the ecliptic from the year A.D. 965 until A.D. 970 and located the vernal and the autumnal equinoxes and used several observational instruments such as a Sundial, a Quadrant, an Astrolabe, a Celestial Globe, and most probably different sizes of Rings such as the Adudi Ring. In chapter 3.4 of I tried to collect all references found in many Arabic historical references that were related to these instruments and the observatory in Shiraz

Many scientists and astronomers have based their astronomical observations on alṢūfi's work. Through out history al-Ṣūfi's name was sometimes miss-spelled or miss-written. He has been named Esophi by Leo Africanus and Azophi by the Spanish Jewish astronomer Ibn Ezra. He was again mentioned by the name Azophi by the $16^{\text {th }}$ century European map makers Albrecht Durer and by Peter Apian. In chapter 3.5 of this thesis, I tried to list some of the most important scholars and astronomers who have made use of al-Ṣūfi's work starting from al-Bīrūnī in the $11^{\text {th }}$ centaury up to the beginning of the $20^{\text {th }}$ century. Finally in the last chapter of this section I included a brief description on the crater on the Moon named Azophi and the main belt asteroid designated as "12621 al-Ṣūfi". I have identified this crater and included its picture as well as its coordinate and location on the Moon.

The main effort to revive the treasures hidden in al-Șūfís book was in the translation of this work from Arabic to English. In part 4 of this thesis I started the translation with alṢūfî's introductory chapter. This chapter is a very important part of his work. Al-Ṣūfī starts his introduction with the usual praise to God and prophet Muḥammad. He then divides those who are interested in learning of the stars into two groups. The first group includes the actual astronomers, which he called al-Munajjimin. The other groups are those who study the Arabic $A n w \bar{a}$ ' tradition. In this introductory chapter al-Ṣūfī criticizes the work of al-Battānī. He begins by praising al-Daīnawari's book on $A n w \bar{a}$ ' then ends up with criticizing his knowledge on the stars. He writes about the reason he wrote his book and dedicates it to Aḍud al-Dawla. He explains the methods he used in calculating precession. Finally he explains why he made dual charts for the constellation and the method of using these charts. In this forth part of this thesis I tried to translate the main introductory chapter, the whole star catalog for the entire 48 constellations, as well as six complete constellation chapters of al-Ṣūfís work. These constellations chapters are: Ursa Minor and Ursa Major of the Northern Constellations, Taurus and Scorpio of the Zodiac Constellations and Orion and Centaurus of the Southern Constellations. As I mentioned before that I did not translate all the constellation chapters of al-Ṣūfí's work because that would be beyond the scope of this thesis.

Before I started with the detailed study of al-Ṣūfi's work, and the complete English translation I had to identify the extant manuscripts of the Book of the Fixed Stars. There are many manuscripts that are still preserved in libraries throughout the world. Tracking of these manuscripts involved extensive travel worldwide and much library research. However, I managed to locate as many as 35 manuscripts and acquired copies of the major ones, which I needed for this study. I started the first chapter in part 5 of this thesis by listing all the existing manuscripts of al-Ṣūfí's work that I could find. I grouped these manuscripts by country or location of library they are being kept. Unfortunately not many manuscripts could be used for this study. I put several criteria that I used to choose the most suitable manuscript for the translation. The two main manuscripts which I identified to be the bases of the translation and discussion were the manuscript Marsh144 and MS5036. The Marsh144 manuscript is the earliest manuscript of the Book of the Fixed Stars. It is dated to 1009 only 23 years after alṢūfi's death. This manuscript was actually copied by the authors' son himself. It is now located at the Bodleian library in Oxford. I managed to acquire a copy of this manuscript for this study and I used this as the bases of the English translation. The other manuscript is MS5036 which is found at the national library in Paris. It is dated to 1430 . Even though this manuscript was written much later, however it is a much better written copy. Therefore in the
translation I have relied on this manuscript whenever anything was not clear in manuscript Marsh144.

The study and analysis of al-Ṣūfi's book begins in the chapter 5.2 of this section of this thesis. It begins with the description of the structure of the book and the layout of the constellation chapters. Following that chapter 5.3 describes another important aspects of this study, which are the charts or the maps. One of al-Ṣūfi's innovations in charting the stars was the production of dual illustrations of each of Ptolemy's constellations: One illustration was as portrayed on a celestial globe, the other illustration as viewed directly in the night sky. These were considered a unique feature of al-Ṣūfî's work. Since al-Ṣūfís work was based on Ptolemy's Almagest therefore most of the rendering of the constellation figures resemble classical style figures. However some of the figures have undergone a process of Orientalization as a result of misunderstanding of some of the Greek mythology figures as well as copyist errors in some versions of the Almagest. The other diversion from classical style constellation was also due to influence of the $A n w \bar{a}$ ' tradition which al-Ṣūfī was very much interested in. An example of such addition is to be found in the constellations Andromeda. Al-Ṣūfì makes two additional illustrations for this constellation. The first is the figure of Andromeda with a fish covering her legs. The second is with two fishes covering her body. Some of the constellations in the Marsh144 manuscript were also influenced by another period in history which is found in the Art of the Sassanid era. An example of such Sassanid influence can be found in the illustration of the flying wings of Pegasus which resembles Simurgh the Sassanian mythical flying creature. Another interesting constellation to note is the constellation Lyra meaning the "Harp". Al-Șūfī gave several other names for this constellation which were based on the $A n w \bar{a}$ ' tradition. Among these names was al-Wazza meaning the "Goose" and al-Sulahfāt, which is a "tortoise". The Marsh144 manuscript depicts this constellation as a kind of harp. However al-Ṣūfī mentioned that in many eastern works Lyra was illustrated as a Sulahfāt or a tortoise. In later western illustration this constellation was rendered as a harp superimposed on the image of the goose. Such an illustration can be found in Andreas Cellarius' stellar catalogue published in 1660 and in Johann Hevelius' Uranographia printed in 1690.

For the epoch of his catalog al-Ṣūfì adopted the beginning of the year 1276 of the era of Alexander the great (or Thu al-Qarnain) which corresponds to the year A.D. 964. However al-Șūfi mentioned that "Ptolemy used the observations of Menelaus' who made his observations in the year 845 of the year of Naboukhat Nassar. Al-Ṣūfī also mentioned that: "The time difference between the observations of Menelaus and the date of Ptolemy is 41 years". He concluded that Ptolemy added 25 minutes on Menelaus longitude values to
account for precession. However it is still unknown why al-Ṣūfĩ refers to this fact because at this time there is no evidence or available text that mentions that Ptolemy used Menelaus observations other than al-Ṣūfî's claim. At the end of al-Ṣūfí's introductory chapter he described in detail the method he used in constructing his catalog especially in calculating precession. For his epoch of A.D. 964 he applied the most accurate Arabic precession constant at that time of 1 deg in 66 years rather than the correct value of 1 deg in 71.2 years, thereby adding 12 degrees 42 minutes on Ptolemy's longitude value to allow for precession. Over the 839 years between the tables of Ptolemy and al-Ṣūfi, precession would actually amount to 11 deg 47 min . Hence by using 12 deg 42 min , al-Ṣūfī over-corrected Ptolemy's stellar longitudes by 55 min . I started chapter 5.4 of this section with a brief analysis on the star coordinates in al-Ṣūfī's book before starting the magnitude analysis. Al-Ṣūfì and Ptolemy both added intermediate values to the magnitude class system for some stars. Ptolemy mentioned the words "more-bright" and "less-bright" for certain stars. However al-Ṣūfì expressed these intermediate magnitude values by the words "Aṣghareh" which means "less" or "Akbareh" which means "greater" and "A'zameh" which means "much-greater". Most scholars who studied al-Ṣūfî's work did not differentiate between the two words Akbareh and $A^{\prime}$ zameh. However when I looked at al-Ṣūfî's text in detail it was evident to me that he made a clear distinction between three intermediate magnitudes. I believe that al-Ṣūfī used what I have termed a 3-step intermediate magnitude system, which was more accurate than Ptolemy 2-step intermediate system. I think that with this system al-Ṣūfí managed to express all magnitude values by a constant difference of 0.25 . One of the main topics of this study was to research this 3-step intermediate magnitude system, which would shed new light on the accuracy and independence of al-Ṣūfî's work. I have made a complete analysis on al-Ṣūfî's magnitude values whereby the magnitude values were numerically interpreted by a constant difference of 0.25 magnitudes: that is " +0.25 " for "less", " -0.25 " for "greater" and " -0.5 " for "much-greater". Ptolemy's 2-step intermediate magnitude difference was interpreted by a constant of (0.3) magnitude. After the data collection I conducted an accuracy analysis for the magnitudes of al-Ṣūfī and Ptolemy by calculating the difference between these values and the modern visual magnitudes in order to see if al-Ṣūfī had in mind a two-step or three-step magnitude systems. The statistical results showed that the Mean for the 3-step system is slightly better. The standard deviation is the same whether we apply the 3 or 2 step system whereas it is higher with Ptolemy. The dispersion in al-Ṣūfî's data is thus significantly less than in Ptolemy. Even though the statistical results for al-Ṣūfī values might not be entirely conclusive to some, however I still believe that al-Ṣūfĭ intended to use the 3 -step system. The main reason for this assumption is in the way al-Șūfi expressed or described the values of the stellar magnitudes in his book. From the many descriptions of the magnitude values which are found in constellation commentaries we see that al-Ṣūfī made clear distinction between the
words Akbareh and A'zameh. In many instances we see that he expressed the terms Aspgareh or Akbareh consecutively. As for the term Asghareh, al-Ṣūfì only used this word to indicate the meaning of less. He mentioned Asghareh in many cases through out the work. Therefore from the literary analysis of al-Ṣūfī's work I had the impression that he was not really concerned with word repetition or correct sentence structure. If al-Ṣūfī was concerned with the correct grammatical structure or with word repetition then he would not have used the term Asghareh in all his work even though there are many other words in Arabic vocabulary, which could have been used instead. Whereas he deliberately switched between the other two terms Akbareh and A'zameh.

In his written comments on the constellations al-Ṣūfī mentioned many additional stars that were not included in Ptolemy's star catalog. However it is surprising that al-Ṣūfī did not include these stars in his tables even though he identified many of them in detail and described their magnitudes and he even estimated their locations. In many instances al-Ṣūfì mentions that in several areas of the sky there are many stars but he fails to mention a definite number because of their large numbers. In chapter 5.5 of this thesis I have identified to a total number of 134 of these additional stars; 65 were located in the Northern constellations, 41 in the Zodiac constellations and 28 in the Southern constellations.

There are very few records on the color of stars in ancient star catalogs. "Red" was the color that attracted the most attention while the other colors such as "white" or "blue" were rarely mentioned. Ptolemy gave the color "red" to six stars in his catalog. These stars were Aldebaran, Arcturus, Betelgeuse, Pollux, Antares and strangely enough Sirius. In the Book of the Fixed Stars al-Ṣūfì described seven stars with red color. These stars were Aldebaran, Arcturus, Betelgeuse, Pollux, Alpha Hydrae, Algol and Antares. However al-Ṣūfī stays silent about the color of Sirius. He only describes it as a bright star on the mouth called al-Kalb (Dog). In chapter 5.6 of this study I tried to give a brief summary on each of these eight stars along with what al-Ṣūfī mentioned about them. The colors of these stars were sometimes mentioned in the tables and other times in his comments on the constellations.

The Astrolabe is an ancient analog calculator. It was used for solving problems relating to the time and position of the Sun and stars in the sky. The Astrolabe is thought to be a Greek invention. The first person credited with constructing an Astrolabe in the Islamic world was the eighth century astronomer Muhammad al-Fazari. By the $9^{\text {th }}$ century the Astrolabe was very much in use in the Arab and Islamic world. Al-Ṣūfī wrote extensively on the construction and use of the Astrolabe. In one of his treatises al-Ṣūfī described more than 1000 different uses for an Astrolabe in fields such as astronomy, astrology, timekeeping,
navigation, construction and surveying. Al-Ṣūfî's Book of the Fixed Stars included 44 of these astrolabe stars. It was the best and most accurate of al-Ṣūfī's works. However al-Ṣūfì did not make a list of the Astrolabe stars but rather the information on these stars were scattered throughout the various sections of the book. In chapter 5.7 I identified all the Astrolabe stars found in al-Ṣūfî's book. I also included a brief summary on every one of these stars as they were mentioned by al-Ṣūfi. This summary included all the descriptions both from the tables as well as from the comments in the constellation chapters that mentioned these stars.

In his book al-Ṣūfì mentioned the presence of 'double stars' which he referred to as Muḍ'af stars. In many case he describes their location and magnitude. From al-Ṣūfí's description I managed to identify as many as 20 of these Mud'af stars. I also calculated the angular distance between these stars in order to identify the minimum angular distance which al-Ṣūfì managed to achieve. From the results of this survey the minimum angular separation for these Mud'af stars was achieved by the star HR7116 and star HR7120 with a separation of 0.23 degrees. In this part of the study I have also included the star Mizar. Next to Mizar is the star Alcor. The angular separation between these two stars is 0.20 degrees. However al-Ṣūfì did not refer to these two stars as Mud 'af but he only mentioned that adjacent to Mizar is the star called al-Suh $\bar{a}$ (the neglected one). It was well known that the Arabs were able to separate these two stars long before the time of al-Ṣūfi.

The next chapter in this study describes the Nebulea in al-Ṣūfî’s book. Al-Ṣūfī refers to these nebulae as al-Laṭkhāt al-Sahābiya (the nebulous smear or smudge) and al-Ishtibāk al-Saḥābi (the nebulous mass). Al-Ṣūfi again identified the five nebulae, which Ptolemy mentioned before. However he goes further to describe 10 nebulae, which he himself observed or were previously identified by the Arabs. From al-Ṣūfís description I tried to identify all 10 of these nebulae or galaxies found in the Book of the Fixed Stars. It is now a well-known fact that al-Ṣūfì mentioned for the first time in recorded history the location of the Andromeda galaxy or M31.

Al-Ṣūfī considered Arabic folk astronomy to be an important scientific field of study in its own right. He took upon himself to identify all the various names of stars, asterisms, mansions and constellations as per the method of the Arabs. He also tried to correct many of the mistakes, which were mentioned by previous authors on this subject such as al-Battānī and al-Daīnawari. In chapter 5.10 of this thesis I tabulated the names of stars and asterisms that have been used in Arabic folk astronomy according to al-Ṣūfî. This table included the star name, the Arabic name, the HR number as well as the explanation and comments for every
one of these stars. However for length purposes I made this study for only 6 of the constellations, which are: Ursa Minor, Ursa Major, Taurus, Scorpio, Orion and Centaurus. This exercise was only to give an idea on the importance of this subject in al-Ṣūfî's book and the scope of information that is contained in each of the constellation chapters.

The last six chapters of the study of al-Ṣūfís book are the comments on the Constellations: Ursa Minor, Ursa Major, Taurus, Scorpio, Orion, and Centaurus. In these 6 chapters I made a detailed list of all the stars mentioned by al-Ṣūfĩ. This included the stars descriptions, which were included in al-Ṣūfi's star tables as well as the commentaries. I also included the HR number so each star can be correctly identified. I have again included the star names according to the old Arabic tradition as mentioned in al-Ṣūfí's book as well as some of the names, which have been given to these stars through out history. In these chapters I have also included a modern Star map in order to identify all the stars that were mentioned by al-Ṣūfî in these chapters.

As we have seen in this study al-Ṣūfí's work has been translated and used by many astronomers throughout history starting from al-Bīrūn̄̄ in A.D. 1030, the authors of the Alfonsine tables in 1252, and the famous prince and astronomer Ulugh Bēg in 1437. Modern astronomers such as Ideler ( 1809) and Knobel (1917) also referred to his work. The last modern translation of al-Ṣūfís work was done in French by Schjellerup in 1874. In his introduction to this translation Schjellerup mentioned that:
> "These facts give to the work of al-Șūfī an importance which cannot be denied. Now the time has come when it shall be the duty of the future generations to study the work of the learned astronomers of the Levant and to reveal their importance and to draw conclusions there from."

Following the instructions of important scholars such as Schjellerup and Kunitzsch, I began my own voyage of discovery, which started, with the translation of al-Ṣūfí's work from Arabic to English. To my knowledge, this was the first time that a major English translation of this book was attempted. In this study I tried to translate as accurately as possible the first introductory chapter, six of the major constellation chapters as well as all the star catalogue which is found in this book. Al-Ṣūfî's star catalog was mainly based on Ptolemy's classical work 'the Mathmatike Syntaxis' which was later called the Almagest by the Arabs. As we have seen earlier, al-Ṣūfi updated Ptolemy's stellar longitudes by adding 12 degrees 42 minutes on Ptolemy's longitude value to allow for precession, as he explained in the introductory chapter of his book. He applied the precession constant of 1 deg in 66 years
rather than the correct value of 1 deg in 71.2 years. However, it is in the star magnitudes where al-Ṣūfĩ distinguished himself. He corrected many of the values, which were mentioned in previous catalogues. My analysis in this regard showed that al-Ṣūfī was very accurate in his description of these stellar magnitudes. From the description of the stars which are to be found in each of the constellation chapters, al-Ṣūfī adopted a unique system in expressing these magnitudes which I termed 'the 3-step magnitude system'. The analysis of this system revealed that it was slightly more accurate then the older ' 2 -step system' used by Ptolemy and others. From the various discussions on al-Ṣūfi’s Book of the Fixed Stars, this work had a very important place in the history of Arabic and Islamic observational astronomy. As Winter (1955) said: "al-Ṣūfī not only corrected observational errors in the works of his predecessors, like the famous Arab astronomer al-Battān̄̄, but he also exposed many of the faulty observations found in the various versions of the Almagest. He carefully defined the boundaries of each constellation, and recorded magnitudes and positions of stars using new and independent observations he made himself."

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### 8.1 Table of Coordinates, Magnitudes and Magnitude Analysis.

The first three columns of this table 31 show the number and the number sequence of the stars and constellations. The $4^{\text {th }}$ to the $9^{\text {th }}$ columns are the coordinated values according to al-Ṣūfi's tables. The $10^{\text {th }}$ column (SM) shows the magnitudes of the stars according to al-Ṣūfí. The $11^{\text {th }}$ (SM1) column shows the magnitudes after adjustment for the 3 -step system and the $12^{\text {th }}$ column (SM2) for the 2 -step system. The $13^{\text {th }}$ column (PM) shows the magnitude according to Ptolemy. The $14^{\text {th }}$ column (PMA) shows Ptolemy's magnitudes after adjustment for the 2step system. The $15^{\text {th }}$ (VIS) and $16^{\text {th }}$ (HR) columns show the modern visual magnitude and the HR number for each star.

Table 31: Table of Coordinates, Magnitudes and Magnitude Analysis

| Seq | R.\# | Constellation | Zodiac | Deg | min | D. | Lat | min | SM | SM1 | SM2 | PM | PMA | VIS | HR |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 1 | UMi | 2(60) | 12 | 52 | N | 66 | 0 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.02 | 424 |
| 2 | 2 | UMi | 2(60) | 15 | 12 | N | 70 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.36 | 6789 |
| 3 | 3 | UMi | 2(60) | 28 | 42 | N | 74 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.23 | 6322 |
| 4 | 4 | UMi | 3(90) | 12 | 22 | N | 75 | 40 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.32 | 5903 |
| 5 | 5 | UMi | 3(90) | 16 | 22 | N | 77 | 40 | 5(k) | 4.75 | 4.70 | 4 | 4.00 | 4.95 | 6116 |
| 6 | 6 | UMi | 3(90) | 29 | 52 | N | 72 | 50 | 2 | 2.00 | 2.00 | 2 | 2.00 | 2.08 | 5563 |
| 7 | 7 | UMi | 4(120) | 8 | 52 | N | 74 | 50 | 3 | 3.00 | 3.00 | 2 | 2.00 | 3.05 | 5735 |
| 8 | 8 | UMi | 4(90) | 25 | 42 | N | 71 | 10 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.25 | 5430 |
| 1 | 9 | UMa | 3(90) | 8 | 2 | N | 39 | 50 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.36 | 3323 |
| 2 | 10 | UMa | 3(90) | 8 | 32 | N | 43 | 5 | 5 | 5.00 | 5.00 | 5 | 5.00 | 5.47 | 3354 |
| 3 | 11 | UMa | 3(90) | 9 | 12 | N | 43 | 5 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.60 | 3403 |
| 4 | 12 | UMa | 3(90) | 8 | 52 | N | 47 | 10 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.76 | 3576 |
| 5 | 13 | UMa | 3(90) | 9 | 22 | N | 47 | 5 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.80 | 3616 |
| 6 | 14 | UMa | 3(90) | 10 | 52 | N | 50 | 30 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.56 | 3771 |
| 7 | 15 | UMa | 3(90) | 13 | 12 | N | 43 | 50 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.67 | 3624 |
| 8 | 16 | UMa | 3(90) | 15 | 12 | N | 44 | 20 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.67 | 3757 |
| 9 | 17 | UMa | 3(90) | 21 | 42 | N | 42 | 5 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.80 | 3888 |
| 10 | 18 | UMa | 3(90) | 23 | 42 | N | 44 | 5 | 4(s) | 4.25 | 4.30 | 4(s) | 4.30 | 4.59 | 3894 |
| 11 | 19 | UMa | 3(90) | 23 | 22 | N | 35 | 5 | 3 | 3.00 | 3.00 | 3 | 3.00 | 3.17 | 3775 |
| 12 | 20 | UMa | 3(90) | 18 | 12 | N | 29 | 20 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.14 | 3569 |
| 13 | 21 | UMa | 3(90) | 19 | 2 | N | 28 | 20 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.60 | 3594 |
| 14 | 22 | UMa | 3(90) | 13 | 22 | N | 36 | 5 | 5(m) | 4.50 | 4.70 | 4 | 4.00 | 4.83 | 3662 |
| 15 | 23 | UMa | 3(90) | 13 | 32 | N | 33 | 20 | 5(m) | 4.50 | 4.70 | 4 | 4.00 | 4.48 | 3619 |
| 16 | 24 | UMa | 4(120) | 5 | 22 | N | 49 | 5 | 2 | 2.00 | 2.00 | 2 | 2.00 | 1.79 | 4301 |
| 17 | 25 | UMa | 4(120) | 4 | 52 | N | 44 | 30 | 3(m) | 2.50 | 2.70 | 2 | 2.00 | 2.37 | 4295 |
| 18 | 26 | UMa | 4(120) | 15 | 52 | N | 51 | 5 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.31 | 4660 |
| 19 | 27 | UMa | 4(120) | 15 | 42 | N | 46 | 30 | 3(m) | 2.50 | 2.70 | 2 | 2.00 | 2.44 | 4554 |
| 20 | 28 | UMa | 4(120) | 5 | 22 | N | 29 | 20 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.45 | 4033 |
| 21 | 29 | UMa | 4(120) | 6 | 52 | N | 28 | 15 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.05 | 4069 |
| 22 | 30 | UMa | 4(120) | 14 | 22 | N | 35 | 15 | 3(s) | 3.25 | 3.30 | 4(m) | 3.70 | 3.01 | 4335 |
| 23 | 31 | UMa | 4(120) | 22 | 35 | N | 25 | 50 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.48 | 4377 |
| 24 | 32 | UMa | 4(120) | 23 | 2 | N | 25 | 0 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.66 | 4375 |
| 25 | 33 | UMa | 4(120) | 24 | 52 | N | 53 | 30 | 2 | 2.00 | 2.00 | 2 | 2.00 | 1.77 | 4905 |
| 26 | 34 | UMa | $5(150)$ | 0 | 42 | N | 55 | 40 | 2 | 2.00 | 2.00 | 2 | 2.00 | 2.27 | 5054 |
| 27 | 35 | UMa | $5(150)$ | 12 | 32 | N | 54 | 0 | 2 | 2.00 | 2.00 | 2 | 2.00 | 1.86 | 5191 |


| 28 | 36 | UMa | 5(150) | 10 | 32 | N | 39 | 45 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.90 | 4915 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 29 | 37 | UMa | 5(150) | 2 | 52 | N | 41 | 20 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.26 | 4785 |
| 30 | 38 | UMa | 4(120) | 27 | 42 | N | 17 | 15 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.13 | 3705 |
| 31 | 39 | UMa | 4(120) | 26 | 2 | N | 19 | 10 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.82 | 3690 |
| 32 | 40 | UMa | 4(120) | 25 | 52 | N | 20 | 0 | 6 | 6.00 | 6.00 | F | 6.00 | 4.55 | 3800 |
| 33 | 41 | UMa | 4(120) | 24 | 52 | N | 22 | 45 | 4 | 4.00 | 4.00 | F | 6.00 | 4.81 | 3809 |
| 34 | 42 | UMa | 4(120) | 23 | 52 | N | 20 | 20 | 6 | 6.00 | 6.00 | F | 6.00 | 4.56 | 3612 |
| 35 | 43 | UMa | 4(120) | 12 | 42 | N | 22 | 15 | 6 | 6.00 | 6.00 | F | 6.00 | 4.25 | 3275 |
| 1 | 44 | Dra | 7(210) | 9 | 22 | N | 76 | 30 | 5 | 5.00 | 5.00 | 4 | 4.00 | 5.80 | 6370 |
| 2 | 45 | Dra | 7(210) | 24 | 32 | N | 73 | 30 | 4 | 4.00 | 4.00 | 4(s) | 4.30 | 4.88 | 6554 |
| 3 | 46 | Dra | 7(210) | 25 | 52 | N | 75 | 40 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 2.79 | 6536 |
| 4 | 47 | Dra | 8(240) | 10 | 2 | N | 80 | 20 | 4(m) | 3.50 | 3.70 | 4 | 4.00 | 3.75 | 6688 |
| 5 | 48 | Dra | 8(240) | 12 | 22 | N | 75 | 30 | $\begin{aligned} & \begin{array}{l} 3(\mathrm{~m}) \text { or } \\ 2(\mathrm{~s}) \\ \hline \end{array} . \begin{array}{l}  \\ \hline \end{array}{ }^{2} \\ & \hline \end{aligned}$ | 2.25 | 2.30 | 3 | 3.00 | 2.23 | 6705 |
| 6 | 49 | Dra | 9(270) | 50 | 22 | N | 82 | 20 | 5 | 5.00 | 5.00 | 4 | 4.00 | 4.98 | 6923 |
| 7 | 50 | Dra | $9(270)$ | 15 | 2 | N | 78 | 15 | 5 | 5.00 | 5.00 | 4 | 4.00 | 5.04 | 7049 |
| 8 | 51 | Dra | $9(270)$ | 11 | 32 | N | 80 | 20 | 5 | 5.00 | 5.00 | 4 | 4.00 | 4.77 | 6978 |
| 9 | 52 | Dra | 10(300) | 2 | 12 | N | 81 | 10 | 5 | 5.00 | 5.00 | 4 | 4.00 | 4.66 | 7125 |
| 10 | 53 | Dra | 11(330) | 20 | 42 | N | 81 | 40 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.59 | 7371 |
| 11 | 54 | Dra | 0 | 3 | 12 | N | 83 | 0 | 3(s) | 3.25 | 3.30 | 4 | 4.00 | 3.07 | 7310 |
| 12 | 55 | Dra | 0 | 20 | 22 | N | 78 | 50 | 4(m) | 3.50 | 3.70 | 4 | 4.00 | 3.83 | 7582 |
| 13 | 56 | Dra | 0 | 5 | 32 | N | 77 | 50 | 5(m) | 4.50 | 4.70 | 4 | 4.00 | 4.51 | 7685 |
| 14 | 57 | Dra | 0 | 23 | 22 | N | 80 | 30 | 5(m) | 4.50 | 4.70 | 5 | 5.00 | 4.66 | 7462 |
| 15 | 58 | Dra | 1(30) | 4 | 22 | N | 81 | 40 | 5(m) | 4.50 | 4.70 | 5 | 5.00 | 4.82 | 7180 |
| 16 | 59 | Dra | 1(30) | 8 | 52 | N | 80 | 15 | 5(m) | 4.50 | 4.70 | 5 | 5.00 | 4.45 | 7352 |
| 17 | 60 | Dra | 2(60) | 26 | 2 | N | 84 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.58 | 6636 |
| 18 | 61 | Dra | 2(60) | 3 | 2 | N | 83 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.55 | 6927 |
| 19 | 62 | Dra | 1(30) | 24 | 32 | N | 84 | 50 | 4(m) | 3.50 | 3.70 | 4 | 4.00 | 4.22 | 6920 |
| 20 | 63 | Dra | 4(120) | 11 | 22 | N | 87 | 30 | 6 | 6.00 | 6.00 | 6 | 6.00 | 5.05 | 6566 |
| 21 | 64 | Dra | 4(120) | 4 | 22 | N | 86 | 50 | 6 | 6.00 | 6.00 | 6 | 6.00 | 4.80 | 6596 |
| 22 | 65 | Dra | 5(150) | 21 | 42 | N | 81 | 15 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.83 | 6223 |
| 23 | 66 | Dra | 5(150) | 22 | 2 | N | 83 | 0 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.90 | 6315 |
| 24 | 67 | Dra | 5(150) | 21 | 2 | N | 84 | 50 | 3 | 3.00 | 3.00 | 3 | 3.00 | 3.17 | 6396 |
| 25 | 68 | Dra | 5(150) | 22 | 42 | N | 78 | 0 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.74 | 6132 |
| 26 | 69 | Dra | 5(150) | 25 | 42 | N | 74 | 40 | 4 | 4.00 | 4.00 | 4(m) | 3.70 | 4.01 | 5986 |
| 27 | 70 | Dra | 5(150) | 25 | 22 | N | 70 | 0 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.29 | 5744 |
| 28 | 71 | Dra | 4(120) | 20 | 2 | N | 64 | 30 | 5(m) | 4.50 | 4.70 | 4 | 4.00 | 4.65 | 5226 |
| 29 | 72 | Dra | 4(120) | 23 | 52 | N | 65 | 30 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.65 | 5291 |
| 30 | 73 | Dra | 4(120) | 1 | 52 | N | 61 | 15 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.87 | 4787 |
| 31 | 74 | Dra | 3(90) | 25 | 52 | N | 56 | 15 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.84 | 4434 |
| 1 | 75 | Cep | 1(30) | 17 | 42 | N | 75 | 90 | 5(m) | 4.50 | 4.70 | 4 | 4.00 | 4.39 | 7750 |
| 2 | 76 | Cep | 1(30) | 15 | 42 | N | 64 | 15 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.22 | 8974 |
| 3 | 77 | Cep | 0 | 20 | 42 | N | 71 | 10 | $\begin{array}{\|l} \hline 4(\mathrm{~m}) \text { or } \\ 3(\mathrm{~s}) \\ \hline \end{array}$ | 3.25 | 3.30 | 4 | 4.00 | 3.23 | 8238 |
| 4 | 78 | Cep | 11(330) | 29 | 22 | N | 69 | 0 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.44 | 8162 |
| 5 | 79 | Cep | 11(330) | 22 | 2 | N | 72 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.46 | 7957 |
| 6 | 80 | Cep | 11(330) | 22 | 42 | N | 74 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.22 | 7850 |
| 7 | 81 | Cep | 0 | 11 | 12 | N | 65 | 30 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.29 | 8417 |
| 8 | 82 | Cep | 0 | 20 | 12 | N | 62 | 30 | 4(m) | 3.50 | 3.70 | 4(m) | 3.70 | 3.52 | 8694 |
| 9 | 83 | Cep | 11(330) | 29 | 2 | N | 60 | 15 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.19 | 8494 |
| 10 | 84 | Cep | 0 | 0 | 2 | N | 61 | 15 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.35 | 8465 |
| 11 | 85 | Cep | 0 | 1 | 42 | N | 61 | 20 | 6 | 6.00 | 6.00 | 5 | 5.00 | 5.04 | 8469 |


| 12 | 86 | Cep | 11(330) | 26 | 22 | N | 64 | 0 | 5(k) | 4.75 | 4.70 | 5 | 5.00 | 4.08 | 8316 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 13 | 87 | Cep | 0 | 4 | 2 | N | 59 | 30 | 4(m) | 3.50 | 3.70 | 4 | 4.00 | 3.75 | 8571 |
| 1 | 88 | Boo | $5(150)$ | 15 | 2 | N | 58 | 40 | 5(m) | 4.50 | 4.70 | 5 | 5.00 | 4.54 | 5328 |
| 2 | 89 | Boo | $5(150)$ | 16 | 52 | N | 58 | 20 | 5(m) | 4.50 | 4.70 | 5 | 5.00 | 4.75 | 5340 |
| 3 | 90 | Boo | $5(150)$ | 18 | 22 | N | 60 | 10 | 5(m) | 4.50 | 4.70 | 5 | 5.00 | 4.05 | 5404 |
| 4 | 91 | Boo | $5(150)$ | 22 | 22 | N | 54 | 40 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.18 | 5351 |
| 5 | 92 | Boo | 6(180) | 2 | 22 | N | 49 | 0 | 3 | 3.00 | 3.00 | 3 | 3.00 | 3.03 | 5435 |
| 6 | 93 | Boo | 6(180) | 9 | 22 | N | 53 | 50 | 4(m) | 3.50 | 3.70 | 4(m) | 3.70 | 3.50 | 5602 |
| 7 | 94 | Boo | 6(180) | 18 | 22 | N | 48 | 40 | 4(m) | 3.50 | 3.70 | 4(m) | 3.70 | 3.47 | 5681 |
| 8 | 95 | Boo | 6(180) | 18 | 22 | N | 53 | 15 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.31 | 5733 |
| 9 | 96 | Boo | 6(180) | 17 | 42 | N | 57 | 30 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 5.02 | 5763 |
| 10 | 97 | Boo | 6(180) | 20 | 22 | N | 46 | 10 | 5(m) | 4.50 | 4.70 | 4(m) | 3.70 | 5.58 | 5727 |
| 11 | 98 | Boo | 6(180) | 21 | 12 | N | 45 | 30 | 5 | 5.00 | 5.00 | 5 | 5.00 | 5.51 | 5709 |
| 12 | 99 | Boo | 6(180) | 21 | 17 | N | 41 | 20 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.93 | 5634 |
| 13 | 100 | Boo | 6(180) | 19 | 22 | N | 41 | 50 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.54 | 5616 |
| 14 | 101 | Boo | 6(180) | 19 | 42 | N | 42 | 30 | 5 | 5.00 | 5.00 | 5 | 5.00 | 5.67 | 5638 |
| 15 | 102 | Boo | 6(180) | 20 | 22 | N | 40 | 20 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.81 | 5600 |
| 16 | 103 | Boo | 6(180) | 12 | 42 | N | 40 | 15 | 3 | 3.00 | 3.00 | 3 | 3.00 | 1.95 | 5506 |
| 17 | 104 | Boo | 6(180) | 8 | 22 | N | 41 | 40 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.46 | 5447 |
| 18 | 105 | Boo | 6(180) | 7 | 42 | N | 42 | 10 | 4 | 4.00 | 4.00 | 4(m) | 3.70 | 3.58 | 5429 |
| 19 | 106 | Boo | 6(180) | 18 | 2 | N | 28 | 0 | 4(k) or 4 | 3.75 | 3.70 | 3 | 3.00 | 3.68 | 5478 |
| 20 | 107 | Boo | 6(180) | 4 | 2 | N | 28 | 0 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.68 | 5235 |
| 21 | 108 | Boo | 6(180) | 3 | 12 | N | 26 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.50 | 5185 |
| 22 | 109 | Boo | 6(180) | 4 | 2 | N | 25 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.07 | 5200 |
| 23 | 110 | Boo | 6(180) | 9 | 42 | N | 31 | 30 | 1 | 1.00 | 1.00 | 1 | 1.00 | 0.04 | 5340 |
| 1 | 111 | CrB | 6(180) | 27 | 22 | N | 44 | 30 | 2 | 2.00 | 2.00 | 2 | 2.00 | 2.23 | 5793 |
| 2 | 112 | CrB | 6(180) | 24 | 22 | N | 46 | 10 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.68 | 5747 |
| 3 | 113 | CrB | 6(180) | 24 | 32 | N | 48 | 0 | 4(s) | 4.25 | 4.30 | 5 | 5.00 | 4.14 | 5778 |
| 4 | 114 | CrB | 6(180) | 26 | 22 | N | 50 | 30 | 6 | 6.00 | 6.00 | 6 | 6.00 | 5.56 | 5855 |
| 5 | 115 | CrB | 6(180) | 29 | 52 | N | 44 | 45 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.84 | 5849 |
| 6 | 116 | CrB | 7(210) | 1 | 52 | N | 44 | 50 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.63 | 5889 |
| 7 | 117 | CrB | 7(210) | 4 | 2 | N | 46 | 10 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.15 | 5947 |
| 8 | 118 | CrB | 7(210) | 4 | 22 | N | 49 | 20 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.99 | 5971 |
| 1 | 119 | Her | $8(240)$ | 0 | 22 | N | 37 | 30 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 2.73 | 6406 |
| 2 | 120 | Her | $7(210)$ | 16 | 22 | N | 43 | 0 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.77 | 6148 |
| 3 | 121 | Her | $7(210)$ | 54 | 22 | N | 40 | 10 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.75 | 6095 |
| 4 | 122 | Her | $7(210)$ | 10 | 42 | N | 37 | 10 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 5.00 | 6008 |
| 5 | 123 | Her | $7(210)$ | 29 | 22 | N | 48 | 0 | 3 | 3.00 | 3.00 | 3 | 3.00 | 3.14 | 6410 |
| 6 | 124 | Her | $8(240)$ | 4 | 42 | N | 49 | 30 | 5 | 5.00 | 5.00 | 4(k) | 3.70 | 4.41 | 6526 |
| 7 | 125 | Her | $8(240)$ | 10 | 22 | N | 52 | 0 | 4 | 4.00 | 4.00 | 4(m) | 3.70 | 3.42 | 6623 |
| 8 | 126 | Her | $8(240)$ | 18 | 12 | N | 52 | 50 | 4 | 4.00 | 4.00 | 4(m) | 3.70 | 3.83 | 6779 |
| 9 | 127 | Her | 8(240) | 54 | 22 | N | 54 | 0 | 4 | 4.00 | 4.00 | 4(m) | 3.70 | 4.41 | 6707 |
| 10 | 128 | Her | $8(240)$ | 54 | 12 | N | 53 | 0 | 4 | 4.00 | 4.00 | 4(m) | 3.70 | 3.70 | 6703 |
| 11 | 129 | Her | 7(210) | 16 | 32 | N | 53 | 10 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.81 | 6212 |


| 12 | 130 | Her | 7(210) | 22 | 52 | N | 53 | 30 | 4 | 4.00 | 4.00 | 4(m) | 3.70 | 3.92 | 6324 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 13 | 131 | Her | 7(210) | 22 | 42 | N | 56 | 10 | $\begin{aligned} & 5(\mathrm{~s}) \text { or } \\ & 6(\mathrm{~m}) \end{aligned}$ | 5.50 | 5.70 | 5 | 5.00 | 5.25 | 6332 |
| 14 | 132 | Her | 7(210) | 28 | 52 | N | 38 | 30 | $\begin{aligned} & 5(\mathrm{~s}) \text { or } \\ & 6(\mathrm{~m}) \\ & \hline \end{aligned}$ | 5.50 | 5.70 | 5 | 5.00 | 5.39 | 6377 |
| 15 | 133 | Her | 7(210) | 26 | 42 | N | 59 | 50 | 4(k) | 3.75 | 3.70 | 3 | 3.00 | 3.16 | 6418 |
| 16 | 134 | Her | 7(210) | 28 | 2 | N | 60 | 20 | 5 | 5.00 | 5.00 | 4 | 4.00 | 4.65 | 6436 |
| 17 | 135 | Her | 7(210) | 29 | 2 | N | 61 | 15 | 4 | 4.00 | 4.00 | 4(m) | 3.70 | 4.72 | 6484 |
| 18 | 136 | Her | 8(240) | 53 | 32 | N | 61 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.86 | 6695 |
| 19 | 137 | Her | 8(240) | 4 | 52 | N | 69 | 20 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.80 | 6588 |
| 20 | 138 | Her | 7(210) | 28 | 2 | N | 70 | 15 | 6 | 6.00 | 6.00 | 6 | 6.00 | 5.59 | 6464 |
| 21 | 139 | Her | 7(210) | 29 | 32 | N | 71 | 15 | 6 | 6.00 | 6.00 | 6 | 6.00 | 5.80 | 6509 |
| 22 | 140 | Her | 8(240) | 2 | 22 | N | 72 | 0 | 6 | 6.00 | 6.00 | 6 | 6.00 | 5.37 | 6574 |
| 23 | 141 | Her | 7(210) | 53 | 22 | N | 60 | 15 | 4 | 4.00 | 4.00 | 4(m) | 3.70 | 3.53 | 6220 |
| 24 | 142 | Her | 7(210) | 8 | 2 | N | 63 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.20 | 6168 |
| 25 | 143 | Her | 6(180) | 28 | 22 | N | 65 | 30 | 4 or 4(m) | 4.00 | 4.00 | 4(m) | 3.70 | 3.89 | 6092 |
| 26 | 144 | Her | 6(210) | 26 | 2 | N | 63 | 40 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.26 | 6023 |
| 27 | 145 | Her | 6(180) | 22 | 52 | N | 64 | 15 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.76 | 5982 |
| 28 | 146 | Her | 6(180) | 23 | 52 | N | 60 | 0 | 5 | 5.00 | 5.00 | 4 | 4.00 | 4.62 | 5914 |
| 29 | 147 | Her | 7(210) | 15 | 22 | N | 38 | 10 | 4 | 4.00 | 4.00 | 5 | 5.00 | 4.57 | 6117 |
| 1 | 148 | Lyr | 9(270) | 0 | 2 | N | 62 | 0 | 1 | 1.00 | 1.00 | 1 | 1.00 | 0.04 | 7001 |
| 2 | 149 | Lyr | 9(270) | 3 | 2 | N | 62 | 40 | 4(k) | 3.75 | 3.70 | 4(k) | 3.70 | 5.06 | 7051 |
| 3 | 150 | Lyr | $9(270)$ | 3 | 2 | N | 61 | 0 | 4(k) | 3.75 | 3.70 | 4(k) | 3.70 | 4.36 | 7056 |
| 4 | 151 | Lyr | 9(270) | 6 | 22 | N | 60 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.30 | 7139 |
| 5 | 152 | Lyr | 9(270) | 52 | 42 | N | 61 | 20 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.39 | 7298 |
| 6 | 153 | Lyr | 9(270) | 52 | 22 | N | 60 | 20 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.36 | 7314 |
| 7 | 154 | Lyr | 9(270) | 3 | 42 | N | 56 | 10 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.45 | 7106 |
| 8 | 155 | Lyr | 9(270) | 3 | 32 | N | 55 | 0 | 4(s) | 4.25 | 4.30 | 4(s) | 4.30 | 5.25 | 7102 |
| 9 | 156 | Lyr | 9(270) | 6 | 52 | N | 55 | 20 | 3 | 3.00 | 3.00 | 3 | 3.00 | 3.24 | 7178 |
| 10 | 157 | Lyr | 9(270) | 6 | 42 | N | 54 | 45 | 5 or 5(s) | 5.25 | 5.30 | 4(s) | 4.30 | 4.93 | 7192 |
| 1 | 158 | Cyg | 9(270) | 19 | 12 | N | 49 | 20 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.08 | 7417 |
| 2 | 159 | Cyg | 9(270) | 21 | 42 | N | 50 | 20 | 6(m) | 5.50 | 5.70 | 5 | 5.00 | 4.69 | 7478 |
| 3 | 160 | Cyg | 9(270) | 29 | 2 | N | 54 | 30 | 5 | 5.00 | 5.00 | 4(k) | 3.70 | 3.89 | 7615 |
| 4 | 161 | Cyg | 10(300) | 11 | 12 | N | 57 | 20 | 3(m) | 2.50 | 2.70 | 3 | 3.00 | 2.20 | 7796 |
| 5 | 162 | Cyg | 10(300) | 21 | 52 | N | 60 | 0 | 2 | 2.00 | 2.00 | 2 | 2.00 | 1.25 | 7924 |
| 6 | 163 | Cyg | 10(300) | 2 | 2 | N | 64 | 40 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.87 | 7528 |
| 7 | 164 | Cyg | 10(300) | 5 | 12 | N | 69 | 40 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.49 | 7469 |
| 8 | 165 | Cyg | 10(300) | 3 | 52 | N | 71 | 30 | 4 | 4.00 | 4.00 | 4(m) | 3.70 | 3.79 | 7420 |
| 9 | 166 | Cyg | 9(270) | 29 | 22 | N | 74 | 0 | 4 | 4.00 | 4.00 | 4(m) | 3.70 | 3.77 | 7328 |
| 10 | 167 | Cyg | 10(300) | 13 | 32 | N | 49 | 30 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.46 | 7949 |
| 11 | 168 | Cyg | 10(300) | 16 | 32 | N | 52 | 10 | 4(s) | 4.25 | 4.30 | 4(m) | 3.70 | 4.53 | 7963 |
| 12 | 169 | Cyg | 10(300) | 19 | 22 | N | 44 | 0 | 3 | 3.00 | 3.00 | 3 | 3.00 | 3.20 | 8115 |
| 13 | 170 | Cyg | 10(300) | 22 | 42 | N | 55 | 10 | 4 | 4.00 | 4.00 | 4(m) | 3.70 | 3.94 | 8028 |
| 14 | 171 | Cyg | 10(300) | 27 | 12 | N | 57 | 0 | 4 | 4.00 | 4.00 | 4(m) | 3.70 | 3.72 | 8079 |
| 15 | 172 | Cyg | 10(300) | 33 | 52 | N | 64 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.79 | 7735 |


| 16 | 173 | Cyg | 10(300) | 15 | 22 | N | 64 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.98 | 7751 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 17 | 174 | Cyg | 10(300) | 24 | 52 | N | 63 | 45 | 5 | 5.00 | 5.00 | 5 | 5.00 | 5.44 | 7851 |
| 18 | 175 | Cyg | 10(300) | 23 | 22 | N | 49 | 40 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.72 | 8130 |
| 19 | 176 | Cyg | 10(300) | 26 | 32 | N | 51 | 40 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.23 | 8143 |
| 1 | 177 | Cas | 0 | 20 | 32 | N | 45 | 20 | 4(k) | 3.75 | 3.70 | 4(m) | 3.70 | 3.66 | 153 |
| 2 | 178 | Cas | 0 | 23 | 32 | N | 46 | 45 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.23 | 168 |
| 3 | 179 | Cas | 0 | 25 | 42 | N | 47 | 50 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.43 | 219 |
| 4 | 180 | Cas | 0 | 29 | 22 | N | 49 | 0 | 3(k) | 2.75 | 2.70 | 3(m) | 2.70 | 2.47 | 264 |
| 5 | 181 | Cas | 1(30) | 3 | 22 | N | 45 | 30 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.68 | 403 |
| 6 | 182 | Cas | 1(30) | 9 | 42 | N | 47 | 20 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.38 | 542 |
| 7 | 183 | Cas | 1(30) | 14 | 22 | N | 47 | 20 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.52 | 707 |
| 8 | 184 | Cas | 0 | 27 | 22 | N | 44 | 20 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.33 | 343 |
| 9 | 185 | Cas | 1(30) | 0 | 22 | N | 45 | 0 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.98 | 382 |
| 10 | 186 | Cas | 0 | 15 | 2 | N | 50 | 0 | 6 | 6.00 | 6.00 | 6 | 6.00 | 4.88 | 9071 |
| 11 | 187 | Cas | 0 | 27 | 42 | N | 52 | 40 | 4 or 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.16 | 130 |
| 12 | 188 | Cas | 0 | 20 | 32 | N | 51 | 40 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.27 | 21 |
| 13 | 189 | Cas | 0 | 16 | 2 | N | 51 | 40 | 6 | 6.00 | 6.00 | 6 | 6.00 | 4.54 | 9045 |
| 1 | 190 | Per | 1(30) | 9 | 22 | N | 40 | 30 | - | - | - | - | - | - | $\begin{aligned} & \mathrm{ngc} \\ & 869 \\ & \hline \end{aligned}$ |
| 2 | 191 | Per | 1(30) | 13 | 52 | N | 37 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.76 | 834 |
| 3 | 192 | Per | 1(30) | 15 | 22 | N | 34 | 30 | 3(s) | 3.25 | 3.30 | 3(s) | 3.30 | 2.93 | 915 |
| 4 | 193 | Per | 1(30) | 10 | 12 | N | 32 | 20 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.12 | 799 |
| 5 | 194 | Per | 1(30) | 13 | 22 | N | 34 | 30 | 5 | 5.00 | 5.00 | 4 | 4.00 | 3.95 | 854 |
| 6 | 195 | Per | 1(30) | 14 | 12 | N | 31 | 10 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.05 | 937 |
| 7 | 196 | Per | 1(30) | 17 | 32 | N | 30 | 0 | 2 | 2.00 | 2.00 | 2 | 2.00 | 1.79 | 1017 |
| 8 | 197 | Per | 1(30) | 18 | 2 | N | 27 | 50 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.36 | 1052 |
| 9 | 198 | Per | 1(30) | 19 | 42 | N | 27 | 40 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.23 | 1087 |
| 10 | 199 | Per | $1(30)$ | 20 | 22 | N | 27 | 20 | 3 | 3.00 | 3.00 | 3 | 3.00 | 3.01 | 1122 |
| 11 | 200 | Per | 1(30) | 13 | 12 | N | 27 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.80 | 941 |
| 12 | 201 | Per | 1(30) | 12 | 22 | N | 23 | 0 | 2(s) | 2.25 | 2.30 | 2 | 2.00 | 2.12 | 936 |
| 13 | 202 | Per | 1(30) | 11 | 52 | N | 21 | 0 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.63 | 947 |
| 14 | 203 | Per | 1(30) | 10 | 22 | N | 21 | 0 | 4(m) | 3.50 | 3.70 | 4 | 4.00 | 3.39 | 921 |
| 15 | 204 | Per | 1(30) | 9 | 32 | N | 22 | 15 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.70 | 879 |
| 16 | 205 | Per | 1(30) | 27 | 32 | N | 28 | 15 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.61 | 1324 |
| 17 | 206 | Per | 1(30) | 25 | 42 | N | 28 | 10 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.29 | 1261 |
| 18 | 207 | Per | 1(30) | 25 | 2 | N | 25 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.04 | 1273 |
| 19 | 208 | Per | 1(30) | 26 | 42 | N | 26 | 15 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.14 | 1303 |
| 20 | 209 | Per | 1(30) | 24 | 52 | N | 24 | 30 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.85 | 1350 |
| 21 | 210 | Per | 1(30) | 29 | 2 | N | 18 | 45 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.25 | 1454 |
| 22 | 211 | Per | 1(30) | 19 | 32 | N | 21 | 50 | 4 | 4.00 | 4.00 | 4(m) | 3.70 | 3.77 | 1135 |
| 23 | 212 | Per | 1(30) | 21 | 22 | N | 19 | 15 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.89 | 1220 |
| 24 | 213 | Per | 1(30) | 21 | 2 | N | 14 | 45 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.04 | 1228 |
| 25 | 214 | Per | 1(30) | 16 | 52 | N | 12 | 0 | 3(s) | 3.25 | 3.30 | 3(s) | 3.30 | 3.83 | 1131 |
| 26 | 215 | Per | 1(30) | 19 | 2 | N | 11 | 0 | 3(s) | 3.25 | 3.30 | 3(m) | 2.70 | 2.85 | 1203 |
| 27 | 216 | Per | 1(30) | 24 | 32 | N | 18 | 0 | 5(s) | 5.25 | 5.30 | 5 | 5.00 | 4.71 | 1306 |
| 28 | 217 | Per | 1(30) | 27 | 42 | N | 31 | 0 | 5(s) | 5.25 | 5.30 | 5 | 5.00 | 5.19 | 1314 |


| 29 | 218 | Per | $1(30)$ | 7 | 22 | N | 20 | 40 | 5 | 5.00 | 5.00 | 6 | 6.00 | 4.23 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 219 | Aur | $2(60)$ | 15 | 12 | N | 30 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.72 |


| 29 | 261 | Oph | 8(240) | 17 | 22 | N | 33 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.73 | 6771 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 262 | Ser | 7(210) | 1 | 32 | N | 38 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.52 | 5842 |
| 2 | 263 | Ser | 7(210) | 4 | 22 | N | 40 | 0 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.76 | 5899 |
| 3 | 264 | Ser | 7(210) | 7 | 2 | N | 36 | 0 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.85 | 5933 |
| 4 | 265 | Ser | $7(210)$ | 4 | 42 | N | 34 | 15 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.67 | 5867 |
| 5 | 266 | Ser | 7(210) | 4 | 2 | N | 37 | 15 | 5 | 5.00 | 5.00 | 4 | 4.00 | 4.09 | 5879 |
| 6 | 267 | Ser | 7(210) | 5 | 52 | N | 42 | 30 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.83 | 5972 |
| 7 | 268 | Ser | 7(210) | 4 | 22 | N | 29 | 15 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.05 | 5788 |
| 8 | 269 | Ser | $7(210)$ | 7 | 32 | N | 26 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.43 | 5868 |
| 9 | 270 | Ser | 7(210) | 7 | 2 | N | 25 | 20 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.65 | 5854 |
| 10 | 271 | Ser | 7(210) | 9 | 2 | N | 24 | 0 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.71 | 5892 |
| 11 | 272 | Ser | 7 (210) | 11 | 22 | N | 16 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.53 | 5881 |
| 12 | 273 | Ser | $7(210)$ | 20 | 52 | N | 16 | 15 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.63 | 6129 |
| 13 | 274 | Ser | $8(240)$ | 6 | 22 | N | 10 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.33 | 5446 |
| 14 | 275 | Ser | 8(240) | 9 | 42 | N | 8 | 30 | 4(m) | 3.50 | 3.70 | 4(m) | 3.70 | 3.54 | 6561 |
| 15 | 276 | Ser | 8(240) | 10 | 32 | N | 10 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.26 | 6581 |
| 16 | 277 | Ser | 8(240) | 16 | 22 | N | 20 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.62 | 6710 |
| 17 | 278 | Ser | 8(240) | 21 | 22 | N | 21 | 15 | 4(m) | 3.50 | 3.70 | 4(m) | 3.70 | 3.26 | 6869 |
| 18 | 279 | Ser | 9(270) | 1 | 2 | N | 27 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.87 | 7141 |
| 1 | 280 | Sge | $9(270)$ | 22 | 52 | N | 39 | 20 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.47 | 7635 |
| 2 | 281 | Sge | $9(270)$ | 19 | 22 | N | 39 | 10 | 6 | 6.00 | 6.00 | 6 | 6.00 | 5.00 | 7546 |
| 3 | 282 | Sge | $9(270)$ | 18 | 32 | N | 39 | 50 | 5 | 5.00 | 5.00 | 5 | 5.00 | 3.82 | 7536 |
| 4 | 283 | Sge | $9(270)$ | 16 | 22 | N | 39 | 0 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.37 | 7479 |
| 5 | 284 | Sge | $9(270)$ | 16 | 2 | N | 38 | 40 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.37 | 7488 |
| 1 | 285 | Aql | $9(270)$ | 19 | 52 | N | 26 | 50 | 6 | 6.00 | 6.00 | 4 | 4.00 | 5.52 | 7669 |
| 2 | 286 | Aql | $9(270)$ | 17 | 32 | N | 27 | 10 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.72 | 7602 |
| 3 | 287 | Aql | $9(270)$ | 16 | 32 | N | 29 | 10 | 2(m) | 1.50 | 1.70 | 2(m) | 1.70 | 0.79 | 7557 |
| 4 | 288 | Aql | 9(270) | 17 | 22 | N | 30 | 0 | 5 | 5.00 | 5.00 | 3(s) | 3.30 | 5.11 | 7560 |
| 5 | 289 | Aql | $9(270)$ | 15 | 52 | N | 31 | 30 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.72 | 7525 |
| 6 | 290 | Aql | 9(270) | 18 | 42 | N | 31 | 30 | 6 | 6.00 | 6.00 | 5 | 5.00 | 5.28 | 7610 |
| 7 | 291 | Aql | $9(270)$ | 12 | 22 | N | 28 | 40 | 6 | 6.00 | 6.00 | 5 | 5.00 | 4.45 | 7429 |
| 8 | 292 | Aql | 9(270) | 13 | 52 | N | 26 | 40 | 6 | 6.00 | 6.00 | 5 | 5.00 | 5.17 | 7474 |
| 9 | 293 | Aql | $9(270)$ | 4 | 52 | N | 36 | 20 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.99 | 7235 |
| 10 | 294 | Aql | 9(270) | 16 | 52 | N | 21 | 40 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.90 | 7570 |
| 11 | 295 | Aql | $9(270)$ | 21 | 22 | N | 19 | 10 | 3 | 3.00 | 3.00 | 3 | 3.00 | 3.23 | 7710 |
| 12 | 296 | Aql | $9(270)$ | 8 | 42 | N | 25 | 0 | 3(s) | 3.25 | 3.30 | 4(m) | 3.70 | 3.37 | 7377 |
| 13 | 297 | Aql | 9(270) | 10 | 52 | N | 20 | 0 | 4(s) | 4.25 | 4.30 | 3 | 3.00 | 4.36 | 7447 |
| 14 | 298 | Aql | $9(270)$ | 12 | 22 | N | 15 | 30 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.95 | 7446 |
| 15 | 299 | Aql | $9(270)$ | 3 | 52 | N | 18 | 10 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.44 | 7236 |
| 1 | 300 | Del | 10(300) | 0 | 22 | N | 29 | 10 | 4(m) | 3.50 | 3.70 | 3(s) | 3.30 | 4.03 | 7852 |
| 2 | 301 | Del | 10(300) | 1 | 22 | N | 29 | 0 | 6 | 6.00 | 6.00 | 4(s) | 4.30 | 5.43 | 7883 |
| 3 | 302 | Del | 10(300) | 1 | 22 | N | 27 | 45 | 6 | 6.00 | 6.00 | 4 | 4.00 | 5.06 | 7896 |
| 4 | 303 | Del | 10(300) | 1 | 12 | N | 32 | 0 | 3(s) | 3.25 | 3.30 | 3(s) | 3.30 | 3.63 | 7882 |
| 5 | 304 | Del | 10(300) | 2 | 52 | N | 33 | 50 | 3(s) | 3.25 | 3.30 | 3(s) | 3.30 | 3.77 | 7906 |
| 6 | 305 | Del | 10(300) | 4 | 2 | N | 32 | 0 | 3(s) | 3.25 | 3.30 | 3(s) | 3.30 | 4.43 | 7928 |
| 7 | 306 | Del | 10(300) | 6 | 12 | N | 33 | 10 | 3(s) | 3.25 | 3.30 | 3(s) | 3.30 | 4.27 | 7948 |
| 8 | 307 | Del | 10(300) | 0 | 12 | N | 34 | 0 | 6 | 6.00 | 6.00 | 6 | 6.00 | 5.38 | 7858 |
| 9 | 308 | Del | 10(300) | 0 | 12 | N | 31 | 50 | 6 | 6.00 | 6.00 | 6 | 6.00 | 4.68 | 7871 |
| 10 | 309 | Del | 10(300) | 1 | 42 | N | 31 | 30 | 6 | 6.00 | 6.00 | 6 | 6.00 | 5.72 | 7892 |
| 1 | 310 | Equ | 10(300) | 9 | 2 | N | 20 | 30 | 4 | 4.00 | 4.00 | 7 | 7.00 | 3.92 | 8131 |


| 2 | 311 | Equ | 10(300) | 10 | 42 | N | 20 | 40 | 6 | 6.00 | 6.00 | 7 | 7.00 | 5.16 | 8178 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3 | 312 | Equ | 10(300) | 9 | 2 | N | 25 | 20 | 5(s) | 5.25 | 5.30 | 7 | 7.00 | 4.69 | 8097 |
| 4 | 313 | Equ | 10(300) | 10 | 22 | N | 25 | 0 | 5(s) | 5.25 | 5.30 | 7 | 7.00 | 4.49 | 8123 |
| 1 | 314 | Peg | 0 | 0 | 32 | N | 26 | 0 | 2(s) | 2.25 | 2.30 | 2(s) | 2.30 | 2.06 | 15 |
| 2 | 315 | Peg | 11(330) | 24 | 52 | N | 12 | 30 | 2(s) | 2.25 | 2.30 | 2(s) | 2.30 | 2.83 | 8739 |
| 3 | 316 | Peg | 11(330) | 14 | 52 | N | 31 | 0 | 2(s) | 2.25 | 2.30 | 2(s) | 2.30 | 2.42 | 8775 |
| 4 | 317 | Peg | 11(330) | 9 | 22 | N | 19 | 40 | 2(s) | 2.25 | 2.30 | 2(s) | 2.30 | 2.49 | 8781 |
| 5 | 318 | Peg | 11(330) | 17 | 12 | N | 25 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.60 | 8880 |
| 6 | 319 | Peg | 11(330) | 17 | 42 | N | 25 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.40 | 8905 |
| 7 | 320 | Peg | 11(330) | 11 | 42 | N | 35 | 0 | 5 or 3 | 3.00 | 3.00 | 3 | 3.00 | 2.94 | 8650 |
| 8 | 321 | Peg | 11(330) | 11 | 12 | N | 34 | 30 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.79 | 8641 |
| 9 | 322 | Peg | 11(330) | 8 | 52 | N | 29 | 0 | 4(k) | 3.75 | 3.70 | 4 | 4.00 | 3.95 | 8667 |
| 10 | 323 | Peg | 11(330) | 9 | 42 | N | 29 | 30 | 4(k) | 3.75 | 3.70 | 4 | 4.00 | 3.48 | 8684 |
| 11 | 324 | Peg | 11(330) | 1 | 32 | N | 18 | 0 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.40 | 8634 |
| 12 | 325 | Peg | 11(330) | 3 | 12 | N | 19 | 0 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.19 | 8665 |
| 13 | 326 | Peg | 11(330) | 4 | 2 | N | 15 | 0 | 6 or 5(s) | 6.00 | 6.00 | 5 | 5.00 | 4.90 | 8717 |
| 14 | 327 | Peg | 11(330) | 3 | 12 | N | 16 | 0 | 6 or 5(s) | 6.00 | 6.00 | 5 | 5.00 | 5.16 | 8697 |
| 15 | 328 | Peg | 10(300) | 22 | 2 | N | 16 | 50 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.53 | 8450 |
| 16 | 329 | Peg | 10(300) | 20 | 42 | N | 16 | 0 | 5(s) | 5.25 | 5.30 | 4 | 4.00 | 4.84 | 8413 |
| 17 | 330 | Peg | 10(300) | 18 | 2 | N | 22 | 30 | 3 | 3.00 | 3.00 | 3(m) | 2.70 | 2.39 | 8308 |
| 18 | 331 | Peg | 11(330) | 6 | 22 | N | 41 | 10 | 4 | 4.00 | 4.00 | 4(m) | 3.70 | 4.29 | 8454 |
| 19 | 332 | Peg | 11(330) | 5 | 22 | N | 34 | 15 | 4 | 4.00 | 4.00 | 4(m) | 3.70 | 3.76 | 8430 |
| 20 | 333 | Peg | 10(300) | 25 | 2 | N | 36 | 50 | 4 | 4.00 | 4.00 | 4(m | 3.70 | 4.13 | 8315 |
| 1 | 334 | And | 0 | 8 | 2 | N | 24 | 30 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.27 | 165 |
| 2 | 335 | And | 0 | 9 | 2 | N | 27 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.36 | 154 |
| 3 | 336 | And | 0 | 7 | 2 | N | 23 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.38 | 163 |
| 4 | 337 | And | 0 | 6 | 22 | N | 32 | 0 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.52 | 68 |
| 5 | 338 | And | 0 | 7 | 22 | N | 33 | 30 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.61 | 63 |
| 6 | 339 | And | 0 | 7 | 42 | N | 32 | 20 | $\begin{aligned} & 5(\mathrm{~m}) \text { or } \\ & 5(\mathrm{~s}) \\ & \hline \end{aligned}$ | 5.25 | 5.30 | 5 | 5.00 | 5.18 | 82 |
| 7 | 340 | And | 0 | 2 | 22 | N | 41 | 0 | 4(m) | 3.50 | 3.70 | 4 | 4.00 | 4.29 | 8965 |
| 8 | 341 | And | 0 | 3 | 22 | N | 42 | 0 | 4(m) | 3.50 | 3.70 | 4 | 4.00 | 4.14 | 8976 |
| 9 | 342 | And | 0 | 4 | 52 | N | 44 | 0 | 4(m) | 3.50 | 3.70 | 4 | 4.00 | 3.82 | 8961 |
| 10 | 343 | And | 0 | 6 | 52 | N | 17 | 30 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.06 | 215 |
| 11 | 344 | And | 0 | 8 | 22 | N | 15 | 50 | 5(m) | 4.50 | 4.70 | 4 | 4.00 | 4.42 | 271 |
| 12 | 345 | And | 0 | 16 | 32 | N | 26 | 20 | 2(s) | 2.25 | 2.30 | 3 | 3.00 | 2.06 | 337 |
| 13 | 346 | And | 0 | 14 | 32 | N | 30 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.87 | 269 |
| 14 | 347 | And | 0 | 14 | 42 | N | 32 | 30 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.53 | 226 |
| 15 | 348 | And | 0 | 29 | 32 | N | 28 | 0 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.26 | 603 |
| 16 | 349 | And | 0 | 29 | 52 | N | 37 | 20 | 4 | 4.00 | 4.00 | 4(m) | 3.70 | 4.07 | 496 |
| 17 | 350 | And | 0 | 27 | 52 | N | 35 | 20 | 4(m) | 3.50 | 3.70 | 4 | 4.00 | 3.57 | 464 |
| 18 | 351 | And | 0 | 25 | 2 | N | 29 | 0 | 4(m) | 3.50 | 3.70 | 4 | 4.00 | 4.10 | 458 |


| 19 | 352 | And | 0 | 24 | 42 | N | 28 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.94 | 477 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 20 | 353 | And | 0 | 22 | 52 | N | 35 | 30 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.25 | 335 |
| 21 | 354 | And | 0 | 25 | 22 | N | 34 | 30 | $5(\mathrm{~s})$ or 6 | 6.00 | 6.00 | 5 | 5.00 | 5.27 | 390 |
| 22 | 355 | And | 0 | 26 | 52 | N | 32 | 30 | 5(s) or 6 | 6.00 | 6.00 | 5 | 5.00 | 4.98 | 469 |
| 23 | 356 | And | 11(330) | 24 | 22 | N | 44 | 0 | 4(m) or 4 | 3.50 | 3.70 | 3 | 3.00 | 3.62 | 8762 |
| 1 | 357 | Tri | 0 | 23 | 42 | N | 16 | 30 | 3 | 3.00 | 3.00 | 3 | 3.00 | 3.41 | 544 |
| 2 | 358 | Tri | 0 | 28 | 42 | N | 20 | 40 | 3 | 3.00 | 3.00 | 3 | 3.00 | 3.00 | 622 |
| 3 | 359 | Tri | 0 | 29 | 2 | N | 19 | 40 | 5(s) | 5.25 | 5.30 | 4 | 4.00 | 4.87 | 660 |
| 4 | 360 | Tri | 0 | 29 | 32 | N | 19 | 0 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 4.01 | 664 |
| 1 | 1 | Ari | 0 | 19 | 22 | N | 7 | 20 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 4.75 | 546 |
| 2 | 2 | Ari | 0 | 20 | 22 | N | 8 | 20 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.64 | 553 |
| 3 | 3 | Ari | 0 | 23 | 42 | N | 7 | 40 | 5(s) | 5.25 | 5.30 | 5 | 5.00 | 5.27 | 646 |
| 4 | 4 | Ari | 0 | 24 | 12 | N | 6 | 0 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 5.62 | 669 |
| 5 | 5 | Ari | 0 | 19 | 12 | N | 5 | 30 | 5 | 5.00 | 5.00 | 5 | 5.00 | 5.10 | 563 |
| 6 | 6 | Ari | 1(30) | 0 | 22 | N | 6 | 0 | 6 | 6.00 | 6.00 | 6 | 6.00 | 5.43 | 773 |
| 7 | 7 | Ari | 1(30) | 4 | 2 | N | 4 | 50 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.63 | 887 |
| 8 | 8 | Ari | 1(30) | 6 | 32 | N | 1 | 40 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.35 | 951 |
| 9 | 9 | Ari | 1(30) | 8 | 2 | N | 2 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.89 | 972 |
| 10 | 10 | Ari | 1(30) | 9 | 42 | N | 1 | 50 | 4 | 4.00 | 4.00 | 4 | 4.00 | 5.09 | 1015 |
| 11 | 11 | Ari | 1(30) | 2 | 22 | N | 1 | 10 | 5 | 5.00 | 5.00 | 5 | 5.00 | 5.63 | 869 |
| 12 | 12 | Ari | 1(30) | 0 | 42 | N | 1 | 30 | 5 | 5.00 | 5.00 | 5 | 5.00 | 5.49 | 847 |
| 13 | 13 | Ari | 0 | 27 | 42 | N | 5 | 15 | 4 | 4.00 | 4.00 | 4(m) | 3.70 | 4.27 | 813 |
| 14 | 14 | Ari | 0 | 23 | 22 | N | 10 | 0 | 3(k) | 2.50 | 2.70 | 3(m) | 2.70 | 2.00 | 617 |
| 15 | 15 | Ari | 1(30) | 4 | 22 | N | 10 | 10 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.63 | 838 |
| 16 | 16 | Ari | $1(30)$ | 4 | 2 | N | 12 | 40 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.51 | 824 |
| 17 | 17 | Ari | 1(30) | 2 | 22 | N | 11 | 10 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.66 | 801 |
| 18 | 18 | Ari | 1(30) | 1 | 52 | N | 10 | 40 | 5(s) | 5.25 | 5.30 | 5 | 5.00 | 5.30 | 782 |
| 1 | 19 | Tau | 1(30) | 9 | 2 | S | 6 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.11 | 1066 |
| 2 | 20 | Tau | $1(30)$ | 8 | 42 | S | 7 | 15 | 4 | 4.00 | 4.00 | 4 | 4.00 | 5.14 | 1061 |
| 3 | 21 | Tau | 1(30) | 7 | 22 | S | 8 | 30 | 4(m) | 3.50 | 3.70 | 4 | 4.00 | 3.74 | 1038 |
| 4 | 22 | Tau | $1(30)$ | 7 | 2 | S | 9 | 15 | 4(m) | 3.50 | 3.70 | 4 | 4.00 | 3.60 | 1030 |
| 5 | 23 | Tau | 1(30) | 12 | 22 | S | 9 | 30 | 6 | 6.00 | 5.00 | 5 | 5.00 | 5.07 | 1174 |
| 6 | 24 | Tau | 1(30) | 16 | 22 | S | 3 | 0 | 3 | 3.00 | 3.00 | 3 | 3.00 | 3.47 | 1239 |
| 7 | 25 | Tau | 1(30) | 59 | 22 | S | 12 | 40 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.29 | 1320 |
| 8 | 26 | Tau | 1(30) | 15 | 42 | S | 14 | 50 | 4(m) | 3.50 | 3.70 | 4 | 4.00 | 3.91 | 1251 |
| 9 | 27 | Tau | 1(30) | 24 | 52 | S | 10 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.27 | 1473 |
| 10 | 28 | Tau | $1(30)$ | 15 | 42 | S | 13 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.25 | 1458 |
| 11 | 29 | Tau | 1(30) | 21 | 42 | S | 5 | 45 | 3(s) | 3.25 | 3.30 | 3(s) | 3.30 | 3.65 | 1346 |
| 12 | 30 | Tau | 1(30) | 23 | 2 | S | 4 | 15 | 3(s) | 3.25 | 3.30 | 3(s) | 3.30 | 3.76 | 1373 |
| 13 | 31 | Tau | 1(30) | 23 | 32 | S | 5 | 50 | 3(s) | 3.25 | 3.30 | 3(s) | 3.30 | 3.84 | 1411 |


| 14 | 32 | Tau | 1(30) | 25 | 22 | S | 5 | 10 | 1 | 1.00 | 1.00 | 1 | 1.00 | 0.85 | 1457 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 15 | 33 | Tau | 1(30) | 24 | 32 | S | 3 | 0 | 3(s) | 3.25 | 3.30 | 3(s) | 3.30 | 3.53 | 1409 |
| 16 | 34 | Tau | 1(30) | 29 | 52 | S | 4 | 0 | 5 | 5.00 | 4.00 | 4 | 4.00 | 5.10 | 1547 |
| 17 | 35 | Tau | 2(60) | 3 | 2 | S | 5 | 0 | 5 | 5.00 | 5.00 | 5 | 5.00 | 5.00 | 1656 |
| 18 | 36 | Tau | 2(60) | 2 | 42 | S | 3 | 30 | 5 | 5.00 | 5.00 | 5 | 5.00 | 5.29 | 1658 |
| 19 | 37 | Tau | 2(60) | 10 | 22 | S | 4 | 30 | 3 | 3.00 | 3.00 | 3 | 3.00 | 3.00 | 1910 |
| 20 | 38 | Tau | 1(30) | 28 | 22 | S | 4 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.28 | 1497 |
| 0 | 0 | Tau |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 21 | 39 | Tau | 1(30) | 24 | 42 | N | 0 | 30 | 4 | 4.00 | 4.00 | 5 | 5.00 | 4.28 | 1392 |
| 22 | 40 | Tau | 1(30) | 24 | 22 | N | 4 | 0 | 4 | 4.00 | 4.00 | 5 | 5.00 | 4.22 | 1387 |
| 23 | 41 | Tau | 1(30) | 19 | 42 | N | 0 | 40 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.36 | 1256 |
| 24 | 42 | Tau | 1(30) | 21 | 42 | N | 1 | 0 | 6 | 6.00 | 6.00 | 6 | 6.00 | 4.94 | 1329 |
| 25 | 43 | Tau | 1(30) | 20 | 42 | N | 5 | 0 | 5 | 5.00 | 5.00 | 5 | 5.00 | 5.41 | 1287 |
| 26 | 44 | Tau | 1(30) | 21 | 12 | N | 50 | 10 | 5 | 5.00 | 5.00 | 5 | 5.00 | 5.23 | 1269 |
| 27 | 45 | Tau | 1(30) | 24 | 42 | N | 3 | 0 | 5 | 5.00 | 5.00 | 5 | 5.00 | 5.37 | 1369 |
| 28 | 46 | Tau | 1(30) | 24 | 24 | N | 5 | 0 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.95 | 1348 |
| 29 | 47 | Tau | 1(30) | 14 | 52 | N | 4 | 30 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.30 | 1140 |
| 30 | 48 | Tau | 1(30) | 15 | 12 | N | 3 | 40 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.18 | 1142 |
| 31 | 49 | Tau | 1(30) | 16 | 22 | N | 3 | 20 | 5 | 5.00 | 5.00 | 5 | 5.00 | 3.63 | 1165 |
| 32 | 50 | Tau | 1(30) | 16 | 22 | N | 5 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 5.26 | 1188 |
| 33 | 51 | Tau | 1(30) | 50 | 42 | S | 14 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.28 | 1101 |
| 34 | 52 | Tau | 2(60) | 2 | 42 | S | 2 | 0 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.64 | 1620 |
| 35 | 53 | Tau | 2(60) | 6 | 42 | S | 1 | 45 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.94 | 1739 |
| 36 | 54 | Tau | 2(60) | 8 | 42 | S | 2 | 0 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.88 | 1030 |
| 37 | 55 | Tau | 2(60) | 11 | 42 | S | 6 | 20 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.86 | 1990 |
| 38 | 56 | Tau | 2(60) | 11 | 42 | S | 50 | 40 | 6(s) | 6.25 | 6.30 | 5 | 5.00 | 6.00 | 1985 |
| 39 | 57 | Tau | 2(60) | 9 | 42 | N | 2 | 40 | 5 | 5.00 | 5.00 | 5 | 5.00 | 5.38 | 1821 |
| 40 | 58 | Tau | 2(60) | 11 | 42 | N | 1 | 0 | 5 | 5.00 | 5.00 | 5 | 5.00 | 5.18 | 1928 |
| 41 | 59 | Tau | 2(60) | 13 | 42 | N | 1 | 20 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.86 | 2002 |
| 42 | 60 | Tau | 2(60) | 15 | 2 | N | 3 | 20 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.58 | 2034 |
| 43 | 61 | Tau | 2(60) | 16 | 2 | N | 1 | 15 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.82 | 2084 |
| 1 | 62 | Gem | 3(90) | 6 | 2 | N | 9 | 40 | 2 | 2.00 | 2.00 | 2 | 2.00 | 1.98 | 2891 |
| 2 | 63 | Gem | 3(90) | 9 | 22 | N | 6 | 15 | 2 | 2.00 | 2.00 | 2 | 2.00 | 1.14 | 2990 |
| 3 | 64 | Gem | 2(60) | 29 | 22 | N | 10 | 0 | 4(m) | 3.50 | 3.70 | 4 | 4.00 | 3.60 | 2540 |
| 4 | 65 | Gem | 3(90) | 1 | 22 | N | 50 | 20 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.41 | 2697 |
| 5 | 66 | Gem | $3(90)$ | 4 | 42 | N | 5 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.79 | 2821 |
| 6 | 67 | Gem | 3(90) | 6 | 42 | N | 4 | 50 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.06 | 2905 |
| 7 <br> 8 | 68 | Gem | $3(90)$ | 9 | 22 | N | 2 | 40 | 4(k) | 3.75 | 3.70 | 4 | 4.00 | 3.57 | 2985 |
| 8 | 69 | Gem | 3(90) | 4 | 22 | N | 2 | 40 | 5(s) | 5.25 | 5.30 | 5 | 5.00 | 5.03 | 2808 |
| 9 | 70 | Gem | 3(90) | 5 | 52 | N | 3 | 0 | 5 | 5.00 | 5.00 | 5 | 5.00 | 5.22 | 2846 |
| 10 | 71 | Gem | 2(60) | 25 | 42 | N | 1 | 30 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 2.98 | 2473 |
| 11 | 72 | Gem | 3(90) | 4 | 22 | S | 0 | 30 | 3 | 3.00 | 3.00 | 3 | 3.00 | 3.79 | 2650 |
| 12 | 73 | Gem | $3(90)$ | 0 | 57 | S | 2 | 30 | 4(m) | 3.50 | 3.70 | 3 | 3.00 | 3.53 | 2777 |
| 13 | 74 | Gem | 3(90) | 4 | 2 | S | 6 | 0 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.58 | 2763 |
| 14 | 75 | Gem | 2(60) | 19 | 12 | S | 1 | 30 | 4(k) | 3.75 | 3.70 | 4(m) | 3.70 | 3.28 | 2216 |
| 15 | 76 | Gem | 2(60) | 20 | 52 | S | 1 | 15 | 4(k) | 3.75 | 3.70 | 4(m) | 3.70 | 2.88 | 2286 |
| 16 | 77 | Gem | 2(60) | 22 | 52 | S | 3 | 30 | 3(s) | 3.25 | 3.30 | 4(m) | 3.70 | 4.15 | 2343 |
| 17 | 78 | Gem | 2(60) | 24 | 42 | S | 50 | 30 | 3 | 3.00 | 3.00 | 3 | 3.00 | 1.93 | 2421 |
| 18 | 79 | Gem | 2(60) | 27 | 22 | S | 10 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.35 | 2484 |


| 19 | 80 | Gem | 2(60) | 16 | 52 | S | 0 | 40 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.16 | 2134 |
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| 20 | 81 | Gem | 2(60) | 19 | 12 | N | 5 | 50 | 4(s) | 4.25 | 4.30 | 4(m) | 3.70 | 4.35 | 2219 |
| 21 | 82 | Gem | 2(60) | 17 | 52 | S | 2 | 15 | 5(s) | 5.25 | 5.30 | 5 | 5.00 | 5.27 | 2529 |
| 22 | 83 | Gem | 3(90) | 11 | 2 | S | 1 | 20 | 5(s) | 5.25 | 5.30 | 5 | 5.00 | 5.35 | 3086 |
| 23 | 84 | Gem | 3(90) | 9 | 2 | S | 3 | 20 | 5(s) | 5.25 | 5.30 | 5 | 5.00 | 4.88 | 3003 |
| 24 | 85 | Gem | 3(90) | 8 | 42 | S | 4 | 30 | 5(s) | 5.25 | 5.30 | 5 | 5.00 | 5.05 | 2938 |
| 25 | 86 | Gem | 3(90) | 13 | 22 | S | 2 | 40 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 5.63 | 3208 |
| 1 | 87 | Cnc | 3(90) | 23 | 12 | N | 0 | 40 | - | - | - | - | - | - | M44 |
| 2 | 88 | Cnc | 3(90) | 20 | 22 | N | 1 | 15 | 4(s) | 4.25 | 4.30 | 4(s) | 4.30 | 5.33 | 3366 |
| 3 | 89 | Cnc | 3(90) | 20 | 42 | S | 1 | 10 | 4(s) | 4.25 | 4.30 | 4(s) | 4.30 | 5.35 | 3357 |
| 4 | 90 | Cnc | 3(90) | 23 | 2 | N | 2 | 40 | 4 | 4.00 | 4.00 | 4(m) | 3.70 | 4.66 | 3449 |
| 5 | 91 | Cnc | 3(90) | 24 | 2 | S | 0 | 10 | 4 | 4.00 | 4.00 | 4(m) | 3.70 | 3.94 | 3461 |
| 6 | 92 | Cnc | 3(90) | 29 | 12 | S | 5 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.24 | 3572 |
| 7 | 93 | Cnc | 3(90) | 21 | 2 | N | 11 | 50 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.02 | 3475 |
| 8 | 94 | Cnc | 3(90) | 14 | 22 | N | 1 | 0 | 5(s) | 5.25 | 5.30 | 5 | 5.00 | 5.31 | 3176 |
| 9 | 95 | Cnc | 3(90) | 20 | 12 | S | 7 | 30 | 4 | 4.00 | 4.00 | 3.7 | 3.70 | 3.52 | 3249 |
| 10 | 96 | Cnc | 4(120) | 2 | 22 | S | 2 | 20 | 4(s) | 4.25 | 4.30 | 4(s) | 4.30 | 5.34 | 3669 |
| 11 | 97 | Cnc | 4(120) | 4 | 22 | S | 5 | 40 | 4(s) | 4.25 | 4.30 | 4(s) | 4.30 | 5.24 | 3623 |
| 12 | 98 | Cnc | 3(90) | 26 | 42 | N | 7 | 50 | 5 | 5.00 | 5.00 | 5 | 5.00 | 5.45 | 3595 |
| 13 | 99 | Cnc | 3(90) | 29 | 42 | N | 5 | 15 | 5 | 5.00 | 5.00 | 5 | 5.00 | 5.14 | 3627 |
| 1 | 100 | Leo | 4(120) | 1 | 2 | N | 10 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.46 | 3731 |
| 2 | 101 | Leo | 4(120) | 3 | 52 | N | 7 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.31 | 3773 |
| 3 | 102 | Leo | 4(120) | 7 | 2 | N | 12 | 0 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.88 | 3905 |
| 4 | 103 | Leo | 4(120) | 6 | 52 | N | 9 | 30 | 3(k) | 2.75 | 2.70 | 3(k) | 2.70 | 2.98 | 3873 |
| 5 | 104 | Leo | 4(120) | 12 | 52 | N | 11 | 0 | 3 | 3.00 | 3.00 | 3 | 3.00 | 3.44 | 4031 |
| 6 | 105 | Leo | 4(120) | 14 | 52 | N | 8 | 30 | 2 | 2.00 | 2.00 | 2 | 2.00 | 2.61 | 4057 |
| 7 | 106 | Leo | 4(120) | 13 | 22 | N | 4 | 30 | 3 | 3.00 | 3.00 | 3 | 3.00 | 3.52 | 3975 |
| 8 | 107 | Leo | 4(120) | 15 | 12 | N | 0 | 10 | 1 | 1.00 | 1.00 | 1 | 1.00 | 1.35 | 3982 |
| 9 | 108 | Leo | 4(120) | 16 | 12 | S | 1 | 50 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.37 | 3980 |
| 10 | 109 | Leo | 4(120) | 12 | 42 | S | 0 | 15 | 5 | 5.00 | 5.00 | 5 | 5.00 | 5.26 | 3937 |
| 11 | 110 | Leo | 4(120) | 10 | 2 | 0 | 0 | 0 | 6 | 6.00 | 6.00 | 5 | 5.00 | 5.35 | 3866 |
| 12 | 111 | Leo | 4(120) | 6 | 52 | S | 3 | 40 | 6 | 6.00 | 6.00 | 5 | 5.00 | 4.97 | 3782 |
| 13 | 112 | Leo | 4(120) | 10 | 2 | S | 4 | 10 | 4(k) | 3.75 | 3.70 | 4 | 4.00 | 3.52 | 3852 |
| 14 | 113 | Leo | 4(120) | 15 | 12 | S | 4 | 15 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.70 | 3950 |
| 15 | 114 | Leo | 4(120) | 21 | 52 | S | 0 | 10 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.85 | 4133 |
| 16 | 115 | Leo | 4(120) | 19 | 42 | N | 4 | 0 | 6 | 6.00 | 6.00 | 6 | 6.00 | 5.46 | 4127 |
| 17 | 116 | Leo | 4(120) | 25 | 42 | N | 5 | 20 | 6 | 6.00 | 6.00 | 6 | 6.00 | 5.48 | 4209 |
| 18 | 117 | Leo | 4(120) | 25 | 2 | N | 2 | 20 | 6 | 6.00 | 6.00 | 6 | 6.00 | 5.34 | 4227 |
| 19 | 118 | Leo | 4(120) | 24 | 2 | N | 12 | 15 | 5(m) | 4.50 | 4.70 | 5 | 5.00 | 4.42 | 4300 |
| 20 | 119 | Leo | 4(120) | 26 | 52 | N | 13 | 40 | 2 | 2.00 | 2.00 | 2(s) | 2.30 | 2.56 | 4357 |
| 21 | 120 | Leo | 4(120) | 27 | 2 | N | 11 | 20 | 5 | 5.00 | 5.00 | 5 | 5.00 | 5.57 | 4408 |
| 22 | 121 | Leo | 4(120) | 29 | 2 | N | 9 | 40 | 3 | 3.00 | 3.00 | 3 | 3.00 | 3.34 | 4359 |
| 23 | 122 | Leo | $5(150)$ | 3 | 2 | N | 5 | 50 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.94 | 4399 |
| 24 | 123 | Leo | 5(150) | 4 | 22 | N | 1 | 15 | 4(k) | 3.75 | 3.70 | 4 | 4.00 | 4.05 | 4386 |
| 25 | 124 | Leo | 5(150) | 4 | 22 | S | 5 | 50 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.95 | 4418 |
| 26 | 125 | Leo | 5(150) | 10 | 12 | S | 3 | 0 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.30 | 4471 |


| 27 | 126 | Leo | 5(150) | 7 | 12 | N | 11 | 50 | 1 | 1.00 | 1.00 | 1(s) | 1.30 | 2.14 | 4534 |
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| 28 | 127 | Leo | 4(120) | 18 | 42 | N | 13 | 20 | 5 | 5.00 | 5.00 | 5 | 5.00 | 5.08 | 4192 |
| 29 | 128 | Leo | 4(120) | 20 | 52 | N | 15 | 30 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.50 | 4259 |
| 30 | 129 | Leo | 5(150) | 0 | 12 | N | 1 | 10 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.63 | 4310 |
| 31 | 130 | Leo | 4(120) | 29 | 52 | S | 0 | 30 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.99 | 4294 |
| 32 | 131 | Leo | 5(150) | 0 | 42 | S | 2 | 40 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.84 | 4291 |
| 33 | 132 | Leo | 5(150) | 7 | 32 | N | 30 | 0 | 5 | 5.00 | 5.00 | 7 | 7.00 | 4.36 | 4737 |
| 34 | 133 | Leo | 5(150) | 7 | 2 | N | 25 | 0 | 5 | 5.00 | 5.00 | 7 | 7.00 | 4.95 | 4667 |
| 35 | 134 | Leo | 5(150) | 11 | 12 | N | 25 | 30 | 5 | 5.00 | 5.00 | 7 | 7.00 | 4.81 | 4789 |
| 1 | 135 | Vir | 5(150) | 9 | 2 | N | 4 | 15 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.03 | 4517 |
| 2 | 136 | Vir | 5(150) | 9 | 42 | N | 5 | 40 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.85 | 4515 |
| 3 | 137 | Vir | 5(150) | 13 | 22 | N | 8 | 0 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.12 | 4608 |
| 4 | 138 | Vir | 5(150) | 12 | 52 | N | 5 | 30 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.66 | 4589 |
| 5 | 139 | Vir | 5(150) | 11 | 42 | N | 0 | 10 | 3 | 3.00 | 3.00 | 3 | 3.00 | 3.61 | 4540 |
| 6 | 140 | Vir | 5(150) | 20 | 57 | N | 1 | 10 | 3 | 3.00 | 3.00 | 3 | 3.00 | 3.89 | 4689 |
| 7 | 141 | Vir | 5(150) | 25 | 52 | N | 2 | 50 | 3 | 3.00 | 3.00 | 3 | 3.00 | 3.66 | 4825 |
| 8 | 142 | Vir | 5(150) | 29 | 52 | N | 2 | 50 | 6 | 6.00 | 6.00 | 5 | 5.00 | 5.99 | 4925 |
| 9 | 143 | Vir | 6(180) | 3 | 42 | N | 1 | 40 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.38 | 4963 |
| 10 | 144 | Vir | 5(150) | 27 | 2 | N | 8 | 30 | 3 | 3.00 | 3.00 | 3 | 3.00 | 3.38 | 4910 |
| 11 | 145 | Vir | 5(150) | 20 | 52 | N | 13 | 50 | 5(s) | 5.25 | 5.30 | 5 | 5.00 | 4.88 | 4828 |
| 12 | 146 | Vir | 5(150) | 22 | 52 | N | 11 | 40 | 6 | 6.00 | 6.00 | 6 | 6.00 | 5.22 | 4847 |
| 13 | 147 | Vir | 5(150) | 24 | 52 | N | 15 | 10 | 3 | 3.00 | 3.00 | 3(s) | 3.30 | 2.83 | 4932 |
| 14 | 148 | Vir | 6(180) | 9 | 22 | S | 2 | 0 | 1(s) | 1.25 | 1.30 | 1 | 1.00 | 0.98 | 5056 |
| 15 | 149 | Vir | 6(180) | 7 | 32 | N | 8 | 40 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.37 | 5107 |
| 16 | 150 | Vir | 6(180) | 9 | 2 | N | 3 | 20 | 5(s) | 5.25 | 5.30 | 5 | 5.00 | 4.69 | 5095 |
| 17 <br> 18 | 151 | Vir | 6(180) | 9 | 42 | N | 0 | 10 | 6 | 6.00 | 6.00 | 6 | 6.00 | 5.21 | 5100 |
| 18 | 152 | Vir | 6(180) | 12 | 42 | N | 1 | 30 | 5(s) | 5.25 | 5.30 | 4(s) | 4.30 | 5.01 | 5150 |
| 19 | 153 | Vir | 6(180) | 10 | 42 | S | 0 | 20 | 5(s) | 5.25 | 5.30 | 5 | 5.00 | 5.25 | 5064 |
| 20 | 154 | Vir | 6(180) | 14 | 22 | N | 1 | 30 | 5(s) | 5.25 | 5.30 | 5 | 5.00 | 5.51 | 5173 |
| 21 | 155 | Vir | 6(180) | 10 | 42 | N | 8 | 30 | 5 | 5.00 | 5.00 | 5 | 5.00 | 5.15 | 5232 |
| 22 | 156 | Vir | 6(180) | 19 | 22 | N | 7 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.08 | 5338 |
| 23 | 157 | Vir | 6(180) | 20 | 2 | N | 2 | 40 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.19 | 5315 |
| 24 | 158 | Vir | 6(180) | 21 | 2 | N | 11 | 40 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.81 | 5409 |
| 25 | 159 | Vir | 6(180) | 22 | 42 | N | 0 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.52 | 5359 |
| 26 | 160 | Vir | 6(180) | 25 | 22 | N | 9 | 50 | 4(m) | 3.50 | 3.70 | 4 | 4.00 | 3.88 | 5487 |
| 27 | 161 | Vir | 5(150) | 27 | 22 | S | 3 | 30 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.66 | 4813 |
| 28 | 162 | Vir | 6(180) | 1 | 42 | S | 3 | 30 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.79 | 4902 |
| 29 | 163 | Vir | 6(180) | 4 | 57 | S | 3 | 20 | 5 | 5.00 | 5.00 | 5 | 5.00 | 5.19 | 4955 |
| 30 | 164 | Vir | 6(180) | 9 | 52 | S | 7 | 20 | 6 | 6.00 | 6.00 | 6 | 6.00 | 5.04 | 4981 |
| 31 | 165 | Vir | 6(180) | 10 | 52 | S | 8 | 20 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.74 | 5019 |
| 32 | 166 | Vir | 6(180) | 17 | 52 | S | 7 | 50 | 6 | 6.00 | 6.00 | 6 | 6.00 | 4.97 | 5196 |
| 1 | 167 | Lib | 7(210) | 0 | 42 | N | 0 | 40 | 3(k) | 2.75 | 2.70 | 2 | 2.00 | 2.75 | 5531 |
| 2 | 168 | Lib | 6(180) | 29 | 42 | N | 2 | 30 | 5(s) | 5.25 | 5.30 | 5 | 5.00 | 5.31 | 5523 |
| 3 | 169 | Lib | 7(210) | 4 | 52 | N | 8 | 50 | 3(m) | 2.50 | 2.70 | 2 | 2.00 | 2.61 | 5685 |
| 4 | 170 | Lib | 7(210) | 0 | 22 | N | 8 | 30 | 5(s) | 5.25 | 5.30 | 5 | 5.00 | 4.92 | 5586 |
| 5 | 171 | Lib | 7(210) | 6 | 42 | S | 1 | 40 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.54 | 5652 |
| 6 | 172 | Lib | 7(210) | 4 | 2 | N | 1 | 15 | 5(s) | 5.25 | 5.30 | 4 | 4.00 | 5.20 | 5622 |
| 7 | 173 | Lib | 7(210) | 10 | 32 | N | 4 | 45 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.91 | 5787 |
| 8 | 174 | Lib | 7(210) | 15 | 42 | N | 3 | 30 | 4 | 4.00 | 4.00 | 4(s) | 4.30 | 4.15 | 5908 |


| 9 | 175 | Lib | 7(210) | 8 | 52 | N | 9 | 0 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.61 | 5777 |
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| 10 | 176 | Lib | $7(210)$ | 16 | 22 | N | 6 | 40 | 4(s) | 4.25 | 4.30 | 4(s) | 4.30 | 4.88 | 5941 |
| 11 | 177 | Lib | 7(210) | 17 | 2 | N | 9 | 15 | 4(s) | 4.25 | 4.30 | 4(s) | 4.30 | 4.78 | 5978 |
| 12 | 178 | Lib | 7(210) | 16 | 12 | N | 0 | 30 | 6 | 6.00 | 6.00 | 6 | 6.00 | 5.03 | 5902 |
| 13 | 179 | Lib | 7(210) | 13 | 2 | N | 3 | 0 | 6 | 6.00 | 6.00 | 5 | 5.00 | 5.38 | 5814 |
| 14 | 180 | Lib | 7(210) | 13 | 52 | S | 1 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.74 | 5838 |
| 15 | 181 | Lib | $7(210)$ | 5 | 42 | S | 7 | 30 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.29 | 5603 |
| 16 | 182 | Lib | 7(210) | 13 | 52 | S | 8 | 10 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.58 | 5794 |
| 17 | 183 | Lib | 7(210) | 14 | 42 | S | 9 | 40 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.66 | 5812 |
| 1 | 184 | Sco | 7(210) | 19 | 2 | N | 1 | 20 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.62 | 5984 |
| 2 | 185 | Sco | 7(210) | 18 | 22 | S | 1 | 40 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.32 | 5953 |
| 3 | 186 | Sco | 7(210) | 18 | 22 | S | 5 | 0 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.89 | 5944 |
| 4 | 187 | Sco | 7(210) | 18 | 42 | S | 50 | 50 | 4(m) | 3.50 | 3.70 | 3 | 3.00 | 3.88 | 5928 |
| 5 | 188 | Sco | 7(210) | 19 | 42 | N | 1 | 40 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.01 | 6027 |
| 6 | 189 | Sco | 7(210) | 19 | 2 | N | 0 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.96 | 5993 |
| 7 | 190 | Sco | 7(210) | 23 | 22 | S | 3 | 45 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 2.89 | 6084 |
| 8 | 191 | Sco | 7(210) | 25 | 22 | S | 4 | 0 | 2 | 2.00 | 2.00 | 2 | 2.00 | 0.96 | 6134 |
| 9 | 192 | Sco | 7(210) | 17 | 12 | S | 5 | 30 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.82 | 6165 |
| 10 | 193 | Sco | 7(210) | 22 | 10 | S | 6 | 10 | 5(s) | 5.25 | 5.30 | 5 | 5.00 | 4.59 | 6028 |
| 11 | 194 | Sco | $7(210)$ | 23 | 22 | S | 6 | 40 | 5(s) | 5.25 | 5.30 | 5 | 5.00 | 4.78 | 6070 |
| 12 | 195 | Sco | 8(240) | 1 | 12 | S | 11 | 0 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.29 | 6241 |
| 13 | 196 | Sco | $8(240)$ | 1 | 32 | S | 15 | 0 | 3 | 3.00 | 3.00 | 3 | 3.00 | 3.08 | 6247 |
| 14 | 197 | Sco | 8(240) | 2 | 42 | S | 18 | 40 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.73 | 6262 |
| 15 | 198 | Sco | $8(240)$ | 2 | 52 | S | 19 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.62 | 6271 |
| 16 | 199 | Sco | 8(240) | 5 | 52 | S | 19 | 30 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.33 | 6380 |
| 17 | 200 | Sco | $8(240)$ | 10 | 52 | S | 18 | 50 | 3 | 3.00 | 3.00 | 3 | 3.00 | 1.87 | 6553 |
| 18 | 201 | Sco | 8(240) | 12 | 12 | S | 16 | 40 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.03 | 6615 |
| 19 | 202 | Sco | $8(240)$ | 11 | 42 | S | 15 | 20 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.41 | 6580 |
| 20 | 203 | Sco | $8(240)$ | 10 | 12 | S | 13 | 20 | 3 | 3.00 | 3.00 | 3 | 3.00 | 1.63 | 6527 |
| 21 | 204 | Sco | 8(240) | 9 | 42 | S | 13 | 30 | 3(s) | 3.25 | 3.30 | 4 | 4.00 | 2.69 | 6508 |
| 22 | 205 | Sco | 8(240) | 13 | 52 | S | 13 | 15 | - | - | - | - | - | - | M7 |
| 23 | 206 | Sco | 8(240) | 8 | 12 | S | 6 | 10 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.29 | 6492 |
| 24 | 207 | Sco | 8(240) | 12 | 12 | S | 4 | 10 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.54 | 6616 |
| 1 | 208 | Sgr | 8(240) | 17 | 12 | S | 6 | 20 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 2.99 | 6746 |
| 2 | 209 | Sgr | 8(240) | 20 | 22 | S | 6 | 30 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.70 | 6859 |
| 3 | 210 | Sgr | 8(240) | 20 | 42 | S | 10 | 50 | 3(m) | 2.50 | 2.70 | 3 | 3.00 | 1.85 | 6879 |
| 4 | 211 | Sgr | 8(240) | 21 | 42 | N | 1 | 30 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.83 | 6913 |
| 5 | 212 | Sgr | 8(240) | 19 | 2 | S | 2 | 50 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.86 | 6812 |
| 6 | 213 | Sgr | 8(240) | 28 | 2 | S | 3 | 10 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.02 | 7121 |
| 7 | 214 | Sgr | 8(240) | 25 | 42 | N | 3 | 50 | 4(k) | 3.75 | 3.70 | 4 | 4.00 | 3.17 | 7039 |
| 8 | 215 | Sgr | 8(240) | 27 | 52 | N | 0 | 45 | - | - | - | - | - | - | 7116 |
| 9 | 216 | Sgr | 8(240) | 28 | 22 | N | 2 | 10 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.51 | 7150 |
| 10 | 217 | Sgr | 9(270) | 0 | 22 | N | 1 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.77 | 7217 |


| 11 | 218 | Sgr | 9(270) | 1 | 52 | N | 2 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 2.89 | 7264 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 12 | 219 | Sgr | 9(270) | 4 | 2 | N | 2 | 50 | 5(s) | 5.25 | 5.30 | 5 | 5.00 | 4.96 | 7304 |
| 13 | 220 | Sgr | 9(270) | 5 | 2 | N | 4 | 30 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 3.93 | 7340 |
| 14 | 221 | Sgr | 9(270) | 5 | 32 | N | 6 | 30 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.61 | 7342 |
| 15 | 222 | Sgr | 9(270) | 8 | 22 | N | 5 | 30 | 6 | 6.00 | 6.00 | 6 | 6.00 | 5.06 | 7489 |
| 16 | 223 | Sgr | 9(270) | 12 | 12 | N | 5 | 50 | 5(s) | 5.25 | 5.30 | 5 | 5.00 | 5.02 | 7614 |
| 17 | 224 | Sgr | 9(270) | 10 | 22 | N | 2 | 0 | 6 | 6.00 | 6.00 | 6 | 6.00 | 5.92 | 7561 |
| 18 | 225 | Sgr | 9(270) | 5 | 2 | S | 1 | 50 | 5(s) | 5.25 | 5.30 | 5 | 5.00 | 5.03 | 7362 |
| 19 | 226 | Sgr | 9(270) | 7 | 32 | S | 2 | 50 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.60 | 7440 |
| 20 | 227 | Sgr | 9(270) | 2 | 42 | S | 2 | 30 | 5(s) | 5.25 | 5.30 | 5 | 5.00 | 4.85 | 7292 |
| 21 | 228 | Sgr | 9(270) | 0 | 22 | S | 4 | 30 | 4(k) | 3.75 | 3.70 | 4(k) | 3.70 | 3.31 | 7234 |
| 22 | 229 | Sgr | 8(240) | 29 | 2 | S | 6 | 45 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.60 | 7194 |
| 23 | 230 | Sgr | 9(270) | 0 | 22 | S | 23 | 0 | 4(s) | 4.25 | 4.30 | 2 | 2.00 | 4.29 | 7343 |
| 24 | 231 | Sgr | 8(240) | 29 | 42 | S | 18 | 0 | 4(s) | 4.25 | 4.30 | 2(s) | 2.30 | 3.97 | 7348 |
| 25 | 232 | Sgr | 8(240) | 19 | 22 | S | 13 | 0 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.11 | 6832 |
| 26 | 233 | Sgr | 9(270) | 10 | 2 | S | 13 | 30 | 4(s) | 4.25 | 4.30 | 3 | 3.00 | 4.37 | 7623 |
| 27 | 234 | Sgr | 9(270) | 9 | 32 | S | 20 | 10 | 4(s) | 4.25 | 4.30 | 3 | 3.00 | 4.13 | 7581 |
| 28 | 235 | Sgr | 9(270) | 10 | 22 | S | 4 | 50 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.70 | 7597 |
| 29 | 236 | Sgr | 9(270) | 11 | 32 | S | 4 | 50 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.83 | 7618 |
| 30 | 237 | Sgr | 9(270) | 11 | 32 | S | 5 | 50 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.52 | 7604 |
| 31 | 238 | Sgr | 9(270) | 12 | 22 | S | 6 | 30 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.58 | 7650 |
| 1 | 239 | Cap | 9(270) | 20 | 2 | N | 7 | 20 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.57 | 7754 |
| 2 | 240 | Cap | 9(270) | 20 | 22 | N | 6 | 40 | 5(s) | 5.25 | 5.30 | 6 | 6.00 | 4.76 | 7773 |
| 3 | 241 | Cap | 9(270) | 20 | 2 | N | 5 | 0 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.08 | 7776 |
| 4 | 242 | Cap | 9(270) | 17 | 42 | N | 8 | 0 | 6(s) | 6.25 | 6.30 | 6 | 6.00 | 6.34 | 7712 |
| 5 | 243 | Cap | 9(270) | 21 | 42 | N | 0 | 45 | 6 | 6.00 | 6.00 | 6 | 6.00 | 5.94 | 7830 |
| 6 | 244 | Cap | 9(270) | 21 | 22 | N | 1 | 45 | 6 | 6.00 | 6.00 | 6 | 6.00 | 5.25 | 7814 |
| 7 | 245 | Cap | 9(270) | 21 | 32 | N | 1 | 30 | 6 | 6.00 | 6.00 | 6 | 6.00 | 4.78 | 7822 |
| 8 | 246 | Cap | 9(270) | 18 | 52 | N | 0 | 40 | 6 | 6.00 | 6.00 | 5 | 5.00 | 5.28 | 7761 |
| 9 | 247 | Cap | 9(270) | 24 | 22 | N | 3 | 50 | 6 | 6.00 | 6.00 | 6 | 6.00 | 5.22 | 7889 |
| 10 | 248 | Cap | 9(270) | 24 | 32 | N | 0 | 50 | 6 | 6.00 | 6.00 | 5 | 5.00 | 5.10 | 7900 |


| 11 | 249 | Cap | 9(270) | 23 | 32 | S | 6 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.11 | 7980 |
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| 12 | 250 | Cap | 9(270) | 24 | 22 | S | 8 | 40 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.13 | 7936 |
| 13 | 251 | Cap | 9(270) | 29 | 22 | S | 7 | 40 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.50 | 8080 |
| 14 | 252 | Cap | 10(300) | 2 | 52 | S | 6 | 50 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 3.74 | 8204 |
| 15 | 253 | Cap | 10(300) | 3 | 2 | S | 6 | 0 | 5(m) | 5.25 | 4.70 | 5 | 5.00 | 4.51 | 8213 |
| 16 | 254 | Cap | 10(300) | 1 | 22 | S | 4 | 15 | 6 | 6.00 | 6.00 | 5 | 5.00 | 5.24 | 8127 |
| 17 | 255 | Cap | 9(270) | 29 | 22 | S | 4 | 0 | 6 | 6.00 | 6.00 | 5 | 5.00 | 5.30 | 8087 |
| 18 | 256 | Cap | 9(270) | 29 | 22 | S | 2 | 50 | 5(s) | 5.25 | 5.30 | 5 | 5.00 | 4.84 | 8060 |
| 19 | 257 | Cap | 9(270) | 29 | 22 | 0 | 0 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.07 | 8075 |
| 20 | 258 | Cap | 10(300) | 3 | 42 | S | 0 | 50 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.28 | 8167 |
| 21 | 259 | Cap | 10(300) | 6 | 2 | S | 4 | 45 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.68 | 8260 |
| 22 | 260 | Cap | 10(300) | 7 | 42 | S | 4 | 30 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.73 | 8288 |
| 23 | 261 | Cap | 10(300) | 7 | 32 | S | 2 | 10 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.68 | 8278 |
| 24 | 262 | Cap | 10(300) | 9 | 2 | S | 2 | 0 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.87 | 8322 |
| 25 | 263 | Cap | 10(300) | 9 | 32 | N | 0 | 20 | 5(s) | 5.25 | 5.30 | 5 | 5.00 | 5.18 | 8283 |
| 26 | 264 | Cap | 10(300) | 11 | 22 | 0 | 0 | 0 | 5 | 5.00 | 5.00 | 5 | 5.00 | 5.08 | 8351 |
| 27 | 265 | Cap | 10(300) | 10 | 22 | N | 2 | 50 | 5 | 5.00 | 5.00 | 5 | 5.00 | 5.58 | 8319 |
| 28 | 266 | Cap | 10(300) | 11 | 22 | N | 4 | 20 | 5 | 5.00 | 5.00 | 5 | 5.00 | 5.09 | 8311 |
| 1 | 267 | Aqr | 10(300) | 13 | 2 | N | 15 | 45 | 6(s) | 6.25 | 6.30 | 5 | 5.00 | 5.10 | 8277 |
| 2 | 268 | Aqr | 10(300) | 19 | 2 | N | 11 | 0 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 2.96 | 8414 |
| 3 | 269 | Aqr | 10(300) | 17 | 52 | N | 9 | 40 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.69 | 8402 |
| 4 | 270 | Aqr | 10(300) | 9 | 12 | N | 8 | 50 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 2.91 | 8232 |
| 5 | 271 | Aqr | 10(300) | 10 | 2 | N | 6 | 15 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.69 | 8264 |
| 6 | 272 | Aqr | 10(300) | 0 | 22 | N | 5 | 30 | 6 | 6.00 | 6.00 | 3 | 3.00 | 4.51 | 8093 |
| 7 | 273 | Aqr | 9(270) | 28 | 52 | N | 8 | 0 | 5(s) | 5.25 | 5.30 | 4 | 4.00 | 4.73 | 7990 |
| 8 | 274 | Aqr | $9(270)$ | 27 | 22 | N | 8 | 40 | 4(m) | 3.50 | 3.70 | 3 | 3.00 | 3.77 | 7950 |
| 9 | 275 | Aqr | 10(300) | 22 | 12 | N | 8 | 45 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.84 | 8518 |
| 10 | 276 | Aqr | 10(300) | 24 | 22 | N | 10 | 45 | 4(k) | 3.75 | 3.70 | 3 | 3.00 | 4.66 | 8539 |
| 11 | 277 | Aqr | 10(300) | 24 | 42 | N | 9 | 0 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 4.42 | 8558 |
| 12 | 278 | Aqr | 10(300) | 26 | 42 | N | 8 | 30 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 4.02 | 8597 |
| 13 | 279 | Aqr | 10(300) | 18 | 52 | N | 3 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.16 | 8499 |
| 14 | 280 | Aqr | 10(300) | 19 | 42 | N | 3 | 10 | 5(s) | 5.25 | 5.30 | 5 | 5.00 | 5.37 | 8512 |
| 15 | 281 | Aqr | 10(300) | 21 | 22 | S | 0 | 50 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.82 | 8573 |
| 16 | 282 | Aqr | 10(300) | 14 | 22 | S | 1 | 40 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.27 | 8418 |
| 17 | 283 | Aqr | 10(300) | 15 | 52 | N | 4 | 0 | 6 | 6.00 | 6.00 | 6 | 6.00 | 5.46 | 8452 |
| 18 | 284 | Aqr | 10(300) | 24 | 22 | S | 7 | 30 | 3 | 3.00 | 3.00 | 3 | 3.00 | 3.27 | 8709 |
| 19 | 285 | Aqr | 10(300) | 24 | 2 | S | 5 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.01 | 8679 |
| 20 | 286 | Aqr | 10(300) | 17 | 22 | S | 5 | 40 | 6 | 6.00 | 6.00 | 5 | 5.00 | 6.35 | 8544 |
| 21 | 287 | Aqr | 10(300) | 21 | 2 | S | 10 | 0 | 5(s) | 5.25 | 5.30 | 5 | 5.00 | 5.26 | 8670 |


| 22 | 288 | Aqr | 10(300) | 20 | 32 | S | 9 | 0 | 5(s) | 5.25 | 5.30 | 5 | 5.00 | 4.69 | 8649 |
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| 23 | 289 | Aqr | 10(300) | 27 | 42 | N | 2 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 5.03 | 8610 |
| 24 | 290 | Aqr | 10(300) | 27 | 32 | N | 0 | 10 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 3.74 | 8698 |
| 25 | 291 | Aqr | 11(330) | 0 | 22 | S | 1 | 10 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 5.43 | 8782 |
| 26 | 292 | Aqr | 11(330) | 2 | 42 | S | 0 | 30 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.22 | 8834 |
| 27 | 293 | Aqr | 11(330) | 3 | 12 | S | 1 | 40 | 4 | 4.00 | 4.00 | 4 | 4.00 | 5.06 | 8850 |
| 28 | 294 | Aqr | 11(330) | 1 | 42 | S | 3 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.21 | 8841 |
| 29 | 295 | Aqr | 11(330) | 2 | 32 | S | 4 | 10 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.39 | 8858 |
| 30 | 296 | Aqr | 11(330) | 3 | 32 | S | 8 | 15 | 5(s) | 5.25 | 5.30 | 5 | 5.00 | 5.08 | 8866 |
| 31 | 297 | Aqr | 11(330) | 5 | 22 | S | 12 | 0 | 5 | 5.00 | 5.00 | 5 | 5.00 | 5.00 | 8968 |
| 32 | 298 | Aqr | 11(330) | 5 | 52 | S | 10 | 50 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.49 | 8988 |
| 33 | 299 | Aqr | 11(330) | 4 | 22 | S | 14 | 0 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.82 | 8982 |
| 34 | 300 | Aqr | 11(330) | 4 | 52 | S | 14 | 45 | 5 | 5.00 | 5.00 | 5 | 5.00 | 5.29 | 8998 |
| 35 | 301 | Aqr | 11(330) | 5 | 52 | S | 15 | 40 | 5 | 5.00 | 5.00 | 5 | 5.00 | 5.18 | 9031 |
| 36 | 302 | Aqr | 10(300) | 29 | 42 | S | 14 | 10 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.97 | 8892 |
| 37 | 303 | Aqr | 11(330) | 0 | 12 | S | 15 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.71 | 8939 |
| 38 | 304 | Aqr | 11(330) | 1 | 2 | S | 15 | 45 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.39 | 8906 |
| 39 | 305 | Aqr | 10(300) | 24 | 32 | S | 14 | 50 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.47 | 8789 |
| 40 | 306 | Aqr | 10(300) | 25 | 22 | S | 14 | 20 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.69 | 8817 |
| 41 | 307 | Aqr | 10(300) | 25 | 52 | S | 14 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.66 | 8812 |
| 42 | 308 | Aqr | 10(300) | 19 | 42 | S | 23 | 0 | 1 | 1.00 | 1.00 | 1 | 1.00 | 1.16 | 8728 |
| 43 | 309 | Aqr | 11(330) | 9 | 22 | S | 15 | 30 | 4(m) | 3.50 | 3.70 | 4(m) | 3.70 | 4.55 | 9098 |
| 44 | 310 | Aqr | 11(330) | 12 | 22 | S | 14 | 20 | 4(m) | 3.50 | 3.70 | 4(m) | 3.70 | 4.89 | 33 |
| 45 | 311 | Aqr | 11(330) | 11 | 42 | S | 18 | 15 | 4(m) | 3.50 | 3.70 | 4(m) | 3.70 | 4.44 | 48 |
| 1 | 312 | Psc | 11(330) | 4 | 22 | N | 9 | 15 | 4 | 4.00 | 4.00 | 4(m) | 3.70 | 4.53 | 8773 |
| 2 | 313 | Psc | 11(330) | 6 | 52 | N | 7 | 30 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 3.69 | 8852 |
| 3 | 314 | Psc | 11(330) | 8 | 42 | N | 9 | 20 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 5.05 | 8878 |
| 4 | 315 | Psc | 11(330) | 10 | 52 | N | 9 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.28 | 8916 |
| 5 | 316 | Psc | 11(330) | 13 | 22 | N | 7 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.13 | 8969 |
| 6 | 317 | Psc | 11(330) | 8 | 42 | N | 4 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.94 | 8911 |
| 7 | 318 | Psc | 11(330) | 12 | 22 | N | 3 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.50 | 8984 |
| 8 | 319 | Psc | 11(330) | 18 | 42 | N | 6 | 20 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.01 | 9072 |
| 9 | 320 | Psc | 11(330) | 23 | 42 | N | 5 | 45 | 6 | 6.00 | 6.00 | 6 | 6.00 | 5.37 | 80 |
| 10 | 321 | Psc | 11(330) | 25 | 42 | N | 3 | 45 | 6 | 6.00 | 6.00 | 6 | 6.00 | 5.67 | 132 |
| 11 | 322 | Psc | 11(330) | 29 | 52 | N | 2 | 15 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.43 | 224 |
| 12 | 323 | Psc | 0 | 3 | 12 | N | 1 | 10 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.28 | 294 |
| 13 | 324 | Psc | 0 | 5 | 42 | S | 6 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 5.24 | 361 |
| 14 | 325 | Psc | 0 | 9 | 12 | S | 2 | 0 | 6 | 6.00 | 6.00 | 6 | 6.00 | 5.52 | 330 |
| 15 | 326 | Psc | 0 | 5 | 42 | S | 5 | 0 | 5 | 5.00 | 5.00 | 6 | 6.00 | 5.16 | 378 |
| 16 | 327 | Psc | 0 | 9 | 12 | S | 2 | 20 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.84 | 434 |
| 17 | 328 | Psc | 0 | 11 | 22 | S | 4 | 40 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.44 | 489 |
| 18 | 329 | Psc | 0 | 13 | 22 | S | 7 | 45 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.62 | 549 |
| 19 | 330 | Psc | 0 | 15 | 12 | S | 8 | 30 | 4(m) | 3.50 | 3.70 | 3 | 3.00 | 4.33 | 596 |
| 20 | 331 | Psc | 0 | 13 | 12 | N | 1 | 20 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.26 | 510 |
| 21 | 332 | Psc | 0 | 12 | 52 | N | 1 | 50 | 5(s) | 5.25 | 5.30 | 5 | 5.00 | 5.57 | 463 |
| 22 | 333 | Psc | 0 | 13 | 2 | N | 5 | 20 | 4(m) | 3.50 | 3.70 | 3 | 3.00 | 3.62 | 437 |
| 23 | 334 | Psc | 0 | 13 | 12 | N | 9 | 0 | 5 | 5.00 | 5.00 | 4 | 4.00 | 5.38 | 413 |
| 24 | 335 | Psc | 0 | 13 | 42 | N | 21 | 45 | 5 | 5.00 | 5.00 | 5 | 5.00 | 5.16 | 349 |
| 25 | 336 | Psc | 0 | 13 | 22 | N | 21 | 40 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.51 | 352 |


| 26 | 337 | Psc | 0 | 11 | 22 | N | 20 | 0 | 6(s) | 6.25 | 6.30 | 6 | 6.00 | 5.42 | 274 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 27 | 338 | Psc | 0 | 10 | 22 | N | 19 | 50 | 6(s) | 6.25 | 6.30 | 6 | 6.00 | 6.09 | 262 |
| 28 | 339 | Psc | 0 | 9 | 42 | N | 20 | 20 | 6(s) | 6.25 | 6.30 | 6 | 6.00 | 7.00 | 230 |
| 29 | 340 | Psc | 0 | 8 | 22 | N | 14 | 20 | 4 | 4.00 | 4.00 | 4 | 4.00 | 5.34 | 310 |
| 30 | 341 | Psc | 0 | 9 | 2 | N | 13 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 5.55 | 328 |
| 31 | 342 | Psc | 0 | 10 | 22 | N | 12 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.66 | 351 |
| 32 | 343 | Psc | 0 | 14 | 52 | N | 17 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.76 | 383 |
| 33 | 344 | Psc | 0 | 12 | 32 | N | 15 | 20 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.65 | 360 |
| 34 | 345 | Psc | 0 | 12 | 42 | N | 11 | 45 | 4 | 4.00 | 4.00 | 4 | 4.00 | 5.97 | 397 |
| 35 | 346 | Psc | 11(330) | 13 | 52 | S | 2 | 40 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.86 | 9067 |
| 36 | 347 | Psc | 11(330) | 14 | 57 | S | 2 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 5.10 | 9087 |
| 37 | 348 | Psc | 11(330) | 13 | 22 | S | 5 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.41 | 9089 |
| 38 | 349 | Psc | 11(330) | 15 | 2 | S | 5 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.61 | 3 |
| 1 | 1 | Cet | 1(30) | 0 | 22 | S | 7 | 45 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.70 | 896 |
| 2 | 2 | Cet | 1(30) | 0 | 22 | S | 12 | 20 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.53 | 911 |
| 3 | 3 | Cet | 0 | 25 | 22 | S | 11 | 30 | 3 | 3.00 | 3.00 | 3 | 3.00 | 3.47 | 804 |
| 4 | 4 | Cet | 0 | 23 | 12 | S | 14 | 0 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 4.07 | 779 |
| 5 | 5 | Cet | 0 | 22 | 2 | S | 8 | 10 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.86 | 754 |
| 6 | 6 | Cet | 0 | 25 | 22 | S | 6 | 20 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.28 | 718 |
| 7 | 7 | Cet | 0 | 20 | 22 | S | 4 | 10 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.37 | 649 |
| 8 | 8 | Cet | 0 | 15 | 42 | S | 24 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.89 | 708 |
| 9 | 9 | Cet | 0 | 16 | 2 | S | 28 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.75 | 740 |
| 10 | 10 | Cet | 0 | 19 | 22 | S | 25 | 10 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.84 | 781 |
| 11 | 11 | Cet | 0 | 19 | 42 | S | 27 | 30 | 4(k) | 3.75 | 3.70 | 3 | 3.00 | 4.25 | 811 |
| 12 | 12 | Cet | 0 | 4 | 42 | S | 25 | 20 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.52 | 509 |
| 13 | 13 | Cet | 0 | 5 | 42 | S | 30 | 50 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.00 | 585 |
| 14 | 14 | Cet | 0 | 7 | 42 | S | 20 | 0 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.73 | 539 |
| 15 | 15 | Cet | 0 | 2 | 22 | S | 15 | 20 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.60 | 402 |
| 16 | 16 | Cet | 11(330) | 27 | 42 | S | 15 | 40 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.45 | 334 |
| 17 | 17 | Cet | 11(330) | 23 | 42 | S | 13 | 40 | 6 | 6.00 | 6.00 | 5 | 5.00 | 5.19 | 235 |
| 18 | 18 | Cet | 11(330) | 21 | 22 | S | 14 | 40 | 6 | 6.00 | 6.00 | 5 | 5.00 | 5.59 | 227 |
| 19 | 19 | Cet | 11(330) | 22 | 2 | S | 13 | 0 | 5(s) | 5.25 | 5.30 | 5(k) | 4.70 | 4.76 | 194 |
| 20 | 20 | Cet | 11(330) | 21 | 42 | S | 14 | 0 | 5(s) | 5.25 | 5.30 | 5(k) | 4.70 | 6.02 | 190 |
| 21 | 21 | Cet | 11(330) | 17 | 2 | S | 9 | 40 | 3(s) | 3.25 | 3.30 | 3(s) | 3.30 | 3.56 | 74 |
| 22 | 22 | Cet | 11(330) | 18 | 22 | S | 20 | 20 | 3(m | 2.50 | 2.70 | 3 | 3.00 | 2.04 | 188 |
| 1 | 23 | Ori | 2(60) | 9 | 42 | S | 13 | 50 | - | - | - | - | - | - | 1879 |
| 2 | 24 | Ori | 2(60) | 14 | 42 | S | 17 | 0 | 1(s) | 1.25 | 1.30 | 1(s) | 1.30 | 0.50 | 2061 |
| 3 | 25 | Ori | 2(60) | 6 | 42 | S | 17 | 30 | 2 | 2.00 | 2.00 | 2(m) | 1.50 | 1.64 | 1790 |
| 4 | 26 | Ori | 2(60) | 50 | 42 | S | 18 | 0 | 4(s) | 4.25 | 4.30 | 4(s) | 4.30 | 4.20 | 1839 |
| 5 | 27 | Ori | 2(60) | 6 | 2 | S | 14 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.21 | 2124 |
| 6 | 28 | Ori | 2(60) | 19 | 2 | S | 11 | 50 | 6 | 6.00 | 6.00 | 6 | 6.00 | 5.04 | 2241 |
| 7 | 29 | Ori | 2(60) | 19 | 12 | S | 10 | 0 | 5 | 5.00 | 5.00 | 4 | 4.00 | 4.48 | 2199 |
| 8 | 30 | Ori | 2(60) | 38 | 42 | S | 9 | 45 | 5 | 5.00 | 5.00 | 4 | 4.00 | 4.42 | 2159 |
| 9 | 31 | Ori | 2(60) | 20 | 2 | S | 8 | 15 | 6 | 6.00 | 6.00 | 6 | 6.00 | 5.30 | 2223 |
| 10 | 32 | Ori | 2(60) | 19 | 22 | S | 8 | 15 | 6 | 6.00 | 6.00 | 6 | 6.00 | 4.95 | 2198 |
| 11 | 33 | Ori | 2(60) | 14 | 22 | S | 3 | 45 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.41 | 2047 |
| 12 | 34 | Ori | 2(60) | 17 | 2 | S | 4 | 15 | 5(s) | 5.25 | 5.30 | 5 | 5.00 | 4.63 | 2135 |
| 13 | 35 | Ori | 2(60) | 10 | 12 | S | 19 | 40 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.57 | 1934 |
| 14 | 36 | Ori | 2(60) | 9 | 2 | S | 20 | 0 | 6 | 6.00 | 6.00 | 6 | 6.00 | 5.36 | 1872 |
| 15 | 37 | Ori | 2(60) | 8 | 2 | S | 20 | 20 | 6 | 6.00 | 6.00 | 6 | 6.00 | 5.46 | 1842 |


| 16 | 38 | Ori | 2(60) | 6 | 52 | S | 20 | 40 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.59 | 1811 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 17 | 39 | Ori | 2(60) | 3 | 12 | S | 8 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.82 | 1676 |
| 18 | 40 | Ori | 2(60) | 2 | 2 | S | 8 | 10 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.68 | 1638 |
| 19 | 41 | Ori | 2(60) | 0 | 42 | S | 10 | 15 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.07 | 1580 |
| 20 | 42 | Ori | 1(30) | 29 | 2 | S | 12 | 50 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.65 | 1570 |
| 21 | 43 | Ori | 1(30) | 27 | 52 | S | 14 | 15 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.36 | 1544 |
| 22 | 44 | Ori | 1(30) | 27 | 32 | S | 15 | 50 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.19 | 1543 |
| 23 | 45 | Ori | 1(30) | 27 | 32 | S | 17 | 10 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.69 | 1552 |
| 24 | 46 | Ori | 1(30) | 18 | 2 | S | 20 | 20 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.72 | 1567 |
| 25 | 47 | Ori | 1(30) | 29 | 2 | S | 21 | 30 | 4 | 3.00 | 3.00 | 3 | 3.00 | 4.47 | 1601 |
| 26 | 48 | Ori | 2(60) | 8 | 2 | S | 24 | 10 | 2 | 2.00 | 2.00 | 2 | 2.00 | 2.23 | 1852 |
| 27 | 49 | Ori | 2(60) | 10 | 2 | S | 24 | 50 | 2 | 2.00 | 2.00 | 2 | 2.00 | 1.70 | 1903 |
| 28 | 50 | Ori | 2(60) | 10 | 52 | S | 25 | 40 | 2 | 2.00 | 2.00 | 2 | 2.00 | 2.05 | 1948 |
| 29 | 51 | Ori | 2(60) | 6 | 32 | S | 25 | 50 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.36 | 1788 |
| 30 | 52 | Ori | $2(60)$ | 9 | 12 | S | 28 | 40 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.59 | 1892 |
| 31 | 53 | Ori | $2(60)$ | 9 | 22 | S | 29 | 10 | 3(s) | 3.25 | 3.30 | 3(s) | 3.30 | 6.39 | 1897 |
| 32 | 54 | Ori | 2(60) | 9 | 42 | S | 29 | 50 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 2.77 | 1899 |
| 33 | 55 | Ori | $2(60)$ | 10 | 22 | S | 30 | 40 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.80 | 1937 |
| 34 | 56 | Ori | 2(60) | 8 | 52 | S | 30 | 50 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.62 | 1855 |
| 35 | 57 | Ori | 2(60) | 2 | 32 | S | 31 | 30 | 1 | 1.00 | 1.00 | 1 | 1.00 | 0.12 | 1713 |
| 36 | 58 | Ori | 2(60) | 3 | 42 | S | 30 | 15 | 4(k) | 3.75 | 3.70 | 4(k) | 3.70 | 3.60 | 1735 |
| 37 | 59 | Ori | 2(60) | 6 | 2 | S | 31 | 10 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.14 | 1784 |
| 38 | 60 | Ori | 2(60) | 12 | 52 | S | 33 | 30 | 3(k) | 2.75 | 2.70 | 3(k) | 2.70 | 2.06 | 2004 |
| 1 | 61 | Eri | 2(60) | 1 | 2 | S | 31 | 50 | 4 | 4.00 | 4.00 | 4(m) | 3.70 | 4.27 | 1679 |
| 2 | 62 | Eri | 2(60) | 1 | 32 | S | 28 | 15 | 4 | 4.00 | 4.00 | 4 | 4.00 | 2.79 | 1666 |
| 3 | 63 | Eri | 2(60) | 0 | 42 | S | 29 | 50 | 5 | 5.00 | 5.00 | 4 | 4.00 | 4.81 | 1617 |
| 4 | 64 | Eri | 1(30) | 27 | 22 | S | 28 | 15 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.39 | 1560 |
| 5 | 65 | Eri | 1(30) | 25 | 52 | S | 25 | 50 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.02 | 1520 |
| 6 | 66 | Eri | 1(30) | 22 | 52 | S | 25 | 20 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.93 | 1463 |
| 7 | 67 | Eri | 1(30) | 19 | 2 | S | 26 | 0 | 5(s) | 5.25 | 5.30 | 5 | 5.00 | 5.17 | 1383 |
| 8 | 68 | Eri | 1(30) | 18 | 12 | S | 27 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.47 | 1325 |
| 9 | 69 | Eri | 1(30) | 15 | 32 | S | 27 | 50 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.04 | 1298 |
| 10 | 70 | Eri | 1(30) | 9 | 42 | S | 32 | 7 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 2.95 | 1231 |
| 11 | 71 | Eri | 1(30) | 7 | 22 | S | 31 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.42 | 1162 |
| 12 | 72 | Eri | 1(30) | 6 | 52 | S | 28 | 50 | 4(m) | 3.50 | 3.70 | 3 | 3.00 | 3.54 | 1136 |
| 13 | 73 | Eri | 1(30) | 4 | 42 | S | 28 | 0 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.71 | 1084 |
| 14 | 74 | Eri | 0 | 29 | 52 | S | 25 | 30 | 4 | 4.00 | 4.00 | 3 | 3.00 | 4.80 | 984 |
| 15 | 75 | Eri | 0 | 27 | 32 | S | 23 | 50 | 5 | 5.00 | 5.00 | 4 | 4.00 | 5.26 | 925 |
| 16 | 76 | Eri | 0 | 24 | 52 | S | 23 | 50 | 4(m) | 3.50 | 3.70 | 3 | 3.00 | 3.89 | 874 |
| 17 | 77 | Eri | 0 | 23 | 12 | S | 23 | 15 | 6 | 6.00 | 6.00 | 4 | 4.00 | 6.32 | 859 |
| 18 | 78 | Eri | 0 | 17 | 52 | S | 32 | 10 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.46 | 818 |
| 19 | 79 | Eri | 0 | 18 | 32 | S | 34 | 50 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.75 | 850 |
| 20 | 80 | Eri | 0 | 21 | 32 | S | 38 | 30 | 4(m) | 3.50 | 3.70 | 4 | 4.00 | 4.09 | 919 |
| 21 | 81 | Eri | 0 | 26 | 32 | S | 38 | 10 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.69 | 1003 |
| 22 | 82 | Eri | 1(30) | 0 | 12 | S | 39 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.27 | 1088 |
| 23 | 83 | Eri | 1(30) | 4 | 2 | S | 41 | 20 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.23 | 1173 |
| 24 | 84 | Eri | 1(30) | 4 | 12 | S | 42 | 30 | 5(s) | 5.25 | 5.30 | 5 | 5.00 | 5.24 | 1181 |
| 25 | 85 | Eri | 1(30) | 4 | 52 | S | 43 | 15 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.65 | 1213 |
| 26 | 86 | Eri | 1(30) | 7 | 22 | S | 43 | 20 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.66 | 1240 |
| 27 | 87 | Eri | 1(30) | 16 | 52 | S | 50 | 20 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.51 | 1453 |
| 28 | 88 | Eri | 1(30) | 17 | 42 | S | 51 | 45 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.82 | 1464 |


| 29 | 89 | Eri | 1(30) | 10 | 52 | S | 53 | 50 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.96 | 1393 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 30 | 90 | Eri | 1(30) | 8 | 32 | S | 53 | 10 | 4(m) | 3.50 | 3.70 | 4 | 4.00 | 3.56 | 1347 |
| 31 | 91 | Eri | 1(30) | 0 | 32 | S | 53 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 5.11 | 1214 |
| 32 | 92 | Eri | 0 | 27 | 32 | S | 53 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.17 | 1195 |
| 33 | 93 | Eri | 0 | 24 | 32 | S | 52 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.59 | 1143 |
| 34 | 94 | Eri | 0 | 12 | 52 | S | 53 | 30 | 1 | 1.00 | 1.00 | 1 | 1.00 | 3.24 | 897 |
| 1 | 95 | Lep | 2(60) | 2 | 22 | S | 35 | 0 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.45 | 1696 |
| 2 | 96 | Lep | 2(60) | 2 | 32 | S | 36 | 30 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.36 | 1705 |
| 3 | 97 | Lep | 2(60) | 4 | 2 | S | 35 | 40 | 5 | 5.00 | 5.00 | 5 | 5.00 | 5.30 | 1757 |
| 4 | 98 | Lep | 2(60) | 4 | 2 | S | 36 | 40 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.29 | 1756 |
| 5 | 99 | Lep | 2(60) | 1 | 52 | S | 39 | 15 | 4(k) | 3.75 | 3.70 | 4(k) | 3.70 | 3.31 | 1702 |
| 6 | 100 | Lep | 2(60) | 28 | 52 | S | 45 | 15 | 4(m) | 3.50 | 3.70 | 4(m) | 3.70 | 3.19 | 1654 |
| 7 | 101 | Lep | 2(60) | 8 | 32 | S | 41 | 30 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 2.58 | 1865 |
| 8 | 102 | Lep | 2(60) | 7 | 2 | S | 44 | 20 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 2.84 | 1829 |
| 9 | 103 | Lep | 2(60) | 18 | 42 | S | 44 | 15 | 4(k) | 3.75 | 3.70 | 4(k) | 3.70 | 3.80 | 2035 |
| 10 | 104 | Lep | 2(60) | 11 | 42 | S | 45 | 50 | 4(k) | 3.75 | 3.70 | 4(k) | 3.70 | 3.60 | 1983 |
| 11 | 105 | Lep | 2(60) | 12 | 42 | S | 38 | 20 | 4(k) | 3.75 | 3.70 | 4(k) | 3.70 | 3.55 | 1998 |
| 12 | 106 | Lep | 2(60) | 15 | 22 | S | 38 | 10 | 4(k) | 3.75 | 3.70 | 4(k) | 3.70 | 3.71 | 2085 |
| 1 | 107 | CMa | 3(90) | 0 | 22 | S | 39 | 10 | 1 | 1.00 | 1.00 | 1 | 1.00 | -1.4 | 2491 |
| 2 | 108 | CMa | 3(90) | 2 | 22 | S | 35 | 0 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.06 | 2574 |
| 3 | 109 | CMa | 3(90) | 4 | 2 | S | 36 | 30 | 5 | 5.00 | 5.00 | 5 | 5.00 | 5.00 | 2593 |
| 4 | 110 | CMa | 3(90) | 6 | 2 | S | 37 | 45 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.12 | 2657 |
| 5 | 111 | CMa | 3(90) | 8 | 2 | S | 40 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.37 | 2596 |
| 6 | 112 | CMa | 3(90) | 3 | 12 | S | 42 | 40 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.68 | 2590 |
| 7 | 113 | CMa | 2(60) | 28 | 52 | S | 41 | 15 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.43 | 2443 |
| 8 | 114 | CMa | 2(60) | 28 | 42 | S | 42 | 30 | 5 | 5.00 | 5.00 | 5 | 5.00 | 3.95 | 2429 |
| 9 | 115 | CMa | 2(60) | 23 | 42 | S | 41 | 20 | 3 | 3.00 | 3.00 | 3 | 3.00 | 1.98 | 2294 |
| 10 | 116 | CMa | 2(60) | 27 | 22 | S | 46 | 30 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.33 | 2387 |
| 11 | 117 | CMa | 2(60) | 28 | 52 | S | 45 | 50 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.54 | 2414 |
| 12 | 118 | CMa | 3(90) | 7 | 22 | S | 46 | 10 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.02 | 2653 |
| 13 | 119 | CMa | 3(90) | 4 | 22 | S | 47 | 0 | 5 | 5.00 | 5.00 | 5 | 5.00 | 3.87 | 2580 |
| 14 | 120 | CMa | 3(90) | 9 | 22 | S | 48 | 45 | 3 | 3.00 | 3.00 | 3 | 3.00 | 1.84 | 2693 |
| 15 | 121 | CMa | 3(90) | 6 | 22 | S | 51 | 30 | 3 | 3.00 | 3.00 | 3 | 3.00 | 1.50 | 2618 |
| 16 | 122 | CMa | 3(90) | 5 | 42 | S | 54 | 10 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.98 | 2538 |
| 17 | 123 | CMa | 2(60) | 22 | 22 | S | 53 | 45 | 3 | 3.00 | 3.00 | 3 | 3.00 | 3.02 | 2282 |
| 18 | 124 | CMa | 3(90) | 14 | 52 | S | 50 | 40 | 3(s) | 3.25 | 3.30 | 3(s) | 3.30 | 2.45 | 2827 |
| 19 | 125 | CMa | 3(90) | 2 | 12 | S | 25 | 15 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.99 | 2648 |
| 20 | 126 | CMa | 2(60) | 22 | 42 | S | 61 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 5.02 | 2177 |


| 21 | 127 | CMa | 2(60) | 24 | 2 | S | 58 | 45 | 5 | 5.00 | 5.00 | 4 | 4.00 | 4.37 | 2256 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 22 | 128 | CMa | 2(60) | 25 | 42 | S | 57 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.85 | 2296 |
| 23 | 129 | CMa | 2(60) | 26 | 52 | S | 56 | 0 | 5 | 5.00 | 5.00 | 4 | 4.00 | 4.48 | 2361 |
| 24 | 130 | CMa | 2(60) | 10 | 42 | S | 55 | 30 | 4(s) | 4.25 | 4.00 | 4 | 4.00 | 5.17 | 1996 |
| 25 | 131 | CMa | 2(60) | 13 | 2 | S | 57 | 40 | 5 | 5.00 | 5.00 | 4 | 4.00 | 4.87 | 2056 |
| 26 | 132 | CMa | 2(60) | 15 | 2 | S | 59 | 30 | 4(s) | 4.25 | 4.00 | 4 | 4.00 | 4.36 | 2106 |
| 27 | 133 | CMa | 2(60) | 11 | 42 | S | 59 | 40 | 3 | 3.00 | 3.00 | 2 | 2.00 | 3.11 | 2040 |
| 28 | 134 | CMa | 2(60) | 8 | 42 | S | 57 | 40 | 3 | 3.00 | 3.00 | 2 | 2.00 | 2.64 | 1956 |
| 29 | 135 | CMa | 2(60) | 4 | 52 | S | 59 | 30 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 3.87 | 1862 |
| 1 | 136 | CMi | 3(90) | 7 | 42 | S | 14 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 2.90 | 2845 |
| 2 | 137 | CMi | 3(90) | 11 | 52 | S | 16 | 10 | 1 | 1.00 | 1.00 | 1 | 1.00 | 0.38 | 2943 |
| 1 | 138 | Arg | 3(90) | 23 | 2 | S | 42 | 30 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.20 | 3102 |
| 2 | 139 | Arg | 3(90) | 27 | 2 | S | 43 | 20 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.80 | 3185 |
| 3 | 140 | Arg | 3(90) | 21 | 31 | S | 45 | 0 | 4(m) | 3.50 | 3.70 | 4 | 4.00 | 3.34 | 3045 |
| 4 | 141 | Arg | 3(90) | 21 | 22 | S | 46 | 0 | 5 | 5.00 | 5.00 | 4 | 4.00 | 4.50 | 3034 |
| 5 | 142 | Arg | 3(90) | 18 | 2 | S | 45 | 30 | 5(s) | 5.25 | 5.30 | 4 | 4.00 | 4.70 | 2944 |
| 6 | 143 | Arg | 3(90) | 19 | 2 | S | 47 | 15 | 4(m) | 3.50 | 3.70 | 3 | 3.00 | 4.50 | 2948 |
| 7 | 144 | Arg | 3(90) | 18 | 2 | S | 49 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.64 | 2922 |
| 8 | 145 | Arg | 3(90) | 22 | 2 | S | 49 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.96 | 2996 |
| 9 | 146 | Arg | 3(90) | 21 | 12 | S | 49 | 15 | 5 | 5.00 | 5.00 | 4 | 4.00 | 4.59 | 2993 |
| 10 | 147 | Arg | 3(90) | 26 | 42 | S | 49 | 50 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.79 | 3113 |
| 11 | 148 | Arg | 3(90) | 16 | 42 | S | 53 | 0 | 5(s) | 5.25 | 5.30 | 4 | 4.00 | 5.35 | 2823 |
| 12 | 149 | Arg | 3(90) | 16 | 42 | S | 58 | 40 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.70 | 2773 |
| 13 | 150 | Arg | 3(90) | 22 | 52 | S | 55 | 30 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.53 | 2937 |
| 14 | 151 | Arg | 3(90) | 24 | 52 | S | 58 | 40 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.84 | 2961 |
| 15 | 152 | Arg | 3(90) | 26 | 22 | S | 57 | 15 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.61 | 3017 |
| 16 | 153 | Arg | 3(90) | 29 | 12 | S | 57 | 45 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.49 | 3084 |
| 17 | 154 | Arg | 4(120) | 3 | 52 | S | 58 | 20 | 2 | 2.00 | 2.00 | 2 | 2.00 | 2.25 | 3165 |
| 18 | 155 | Arg | 4(120) | 0 | 52 | S | 60 | 0 | 5 | 5.00 | 5.00 | 5 | 5.00 | 3.73 | 3080 |
| 19 | 156 | Arg | 4(120) | 3 | 42 | S | 59 | 20 | 5 | 5.00 | 5.00 | 5 | 5.00 | 5.52 | 3162 |
| 20 | 157 | Arg | 4(120) | 5 | 42 | S | 56 | 40 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.45 | 3225 |
| 21 | 158 | Arg | 4(120) | 7 | 2 | S | 57 | 0 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.44 | 3243 |
| 22 | 159 | Arg | 4(120) | 18 | 22 | S | 51 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 5.82 | 3535 |
| 23 | 160 | Arg | 4(120) | 18 | 52 | S | 55 | 40 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.07 | 3477 |
| 24 | 161 | Arg | 4(120) | 16 | 42 | S | 57 | 10 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.14 | 3426 |
| 25 | 162 | Arg | 4(120) | 21 | 52 | S | 60 | 0 | 4(k) | 3.50 | 3.75 | 4(k) | 3.70 | 3.91 | 3487 |
| 26 | 163 | Arg | 4(120) | 21 | 42 | S | 61 | 15 | 4(k) | 3.50 | 3.75 | 4(k) | 3.70 | 3.84 | 3445 |
| 27 | 164 | Arg | 4(120) | 12 | 52 | S | 51 | 30 | 4 | 4.00 | 4.00 | 3 | 3.00 | 3.97 | 3438 |
| 28 | 165 | Arg | 4(120) | 12 | 2 | S | 49 | 0 | 4 | 4.00 | 4.00 | 3 | 3.00 | 3.68 | 3468 |
| 29 | 166 | Arg | 4(120) | 10 | 42 | S | 43 | 30 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.01 | 3518 |
| 30 | 167 | Arg | 4(120) | 11 | 42 | S | 43 | 30 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.89 | 3556 |
| 31 | 168 | Arg | 4(120) | 26 | 52 | S | 54 | 30 | 2 | 2.00 | 2.00 | 2 | 2.00 | 2.21 | 3634 |
| 32 | 169 | Arg | 5(150) | 0 | 12 | S | 51 | 15 | 3 | 3.00 | 3.00 | 2(s) | 2.30 | 3.60 | 3786 |


| 33 | 170 | Arg | 3(90) | 23 | 52 | S | 63 | 0 | 4(m) | 3.50 | 3.70 | 4 | 4.00 | 3.24 | 2878 |
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| 34 | 171 | Arg | 4(120) | 1 | 42 | S | 64 | 30 | 6 | 6.00 | 6.00 | 6 | 6.00 | 4.11 | 3055 |
| 35 | 172 | Arg | 4(120) | 12 | 42 | S | 63 | 50 | 2 | 2.00 | 2.00 | 2 | 2.00 | 1.78 | 3207 |
| 36 | 173 | Arg | 4(120) | 21 | 12 | S | 64 | 40 | 4 | 4.00 | 4.00 | 2 | 2.00 | 3.47 | 3117 |
| 37 | 174 | Arg | 4(120) | 27 | 52 | S | 65 | 40 | 3 | 3.00 | 3.00 | 3 | 3.00 | 3.62 | 3447 |
| 38 | 175 | Arg | 5(150) | 4 | 2 | S | 65 | 30 | 3 | 3.00 | 3.00 | 3 | 3.00 | 1.96 | 3485 |
| 39 | 176 | Arg | 5(150) | 8 | 42 | S | 66 | 20 | 3 | 3.00 | 3.00 | 2 | 2.00 | 4.49 | 3498 |
| 40 | 177 | Arg | 5(150) | 13 | 42 | S | 62 | 50 | 4 | 4.00 | 4.00 | 3 | 3.00 | 2.50 | 3734 |
| 41 | 178 | Arg | 5(150) | 20 | 42 | S | 62 | 15 | 4(m) | 3.50 | 3.70 | 2 | 2.00 | 3.13 | 3803 |
| 42 | 179 | Arg | 2(60) | 16 | 42 | S | 65 | 50 | 4 | 4.00 | 4.00 | 4(m) | 3.70 | 3.96 | 2120 |
| 43 | 180 | Arg | 3(90) | 2 | 52 | S | 65 | 40 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.17 | 2451 |
| 44 | 181 | Arg | 2(60) | 29 | 52 | S | 75 | 0 | 1 | 1.00 | 1.00 | 1 | 1.00 | 0.72 | 2326 |
| 45 | 182 | Arg | 3(90) | 11 | 42 | S | 71 | 45 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 2.93 | 2553 |
| 1 | 183 | Hya | 3(90) | 26 | 42 | S | 15 | 0 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 6.33 | 3418 |
| 2 | 184 | Hya | 3(90) | 26 | 2 | S | 13 | 10 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.16 | 3410 |
| 3 | 185 | Hya | 3(90) | 28 | 2 | S | 11 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.38 | 3482 |
| 4 | 186 | Hya | 3(90) | 28 | 12 | S | 14 | 45 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.30 | 3454 |
| 5 | 187 | Hya | 4(120) | 0 | 32 | S | 12 | 0 | 4(m) | 3.50 | 3.70 | 4 | 4.00 | 3.11 | 3547 |
| 6 | 188 | Hya | 4(120) | 3 | 2 | S | 14 | 40 | 6 | 6.00 | 6.00 | 6 | 6.00 | 4.97 | 3613 |
| 7 | 189 | Hya | 4(120) | 6 | 2 | S | 19 | 20 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.88 | 3665 |
| 8 | 190 | Hya | 4(120) | 11 | 32 | S | 15 | 20 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.57 | 3787 |
| 9 | 191 | Hya | 4(120) | 13 | 22 | S | 14 | 50 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 3.91 | 3845 |
| 10 | 192 | Hya | 4(120) | 11 | 12 | S | 17 | 10 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.60 | 3759 |
| 11 | 193 | Нуa | 4(120) | 11 | 52 | S | 19 | 45 | 6(s) | 6.25 | 6.30 | 6 | 6.00 | 5.37 | 3750 |
| 12 | 194 | Hya | 4(120) | 12 | 42 | S | 20 | 30 | 2 | 2.00 | 2.00 | 2 | 2.00 | 1.98 | 3748 |
| 13 | 195 | Hya | 4(120) | 18 | 42 | S | 26 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 5.06 | 3849 |
| 14 | 196 | Hya | 4(120) | 21 | 22 | S | 26 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.12 | 3903 |
| 15 | 197 | Hya | 4(120) | 23 | 52 | S | 23 | 15 | 4(k) | 3.75 | 3.70 | 4 | 4.00 | 4.60 | 3970 |
| 16 | 198 | Hya | 5(150) | 0 | 42 | S | 24 | 40 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 3.81 | 4094 |
| 17 | 199 | Hya | 5(150) | 2 | 42 | S | 23 | 0 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.91 | 4171 |
| 18 | 200 | Hya | 5(150) | 5 | 42 | S | 22 | 10 | 3 | 3.00 | 3.00 | 3 | 3.00 | 3.11 | 4232 |
| 19 | 201 | Hya | 5(150) | 14 | 12 | S | 25 | 45 | 4 | 4.00 | 4.00 | 4(m) | 3.70 | 4.48 | 4343 |
| 20 | 202 | Нуa | 5(150) | 15 | 2 | S | 30 | 10 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.94 | 4314 |
| 21 | 203 | Hya | 5(150) | 24 | 52 | S | 31 | 20 | 4(k) | 3.75 | 3.70 | 4 | 4.00 | 3.54 | 4450 |
| 22 | 204 | Hya | 5(150) | 27 | 12 | S | 33 | 10 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.70 | 4494 |
| 23 | 205 | Hya | 5(150) | 28 | 52 | S | 31 | 20 | 3 | 3.00 | 3.00 | 3 | 3.00 | 4.28 | 4552 |
| 24 | 206 | Нуa | 6(180) | 12 | 42 | S | 13 | 40 | 3(s) | 3.25 | 3.30 | 4(k) | 3.70 | 3.00 | 5020 |
| 25 | 207 | Hya | 6(180) | 26 | 12 | S | 17 | 40 | 3(s) | 3.25 | 3.30 | 4(k) | 3.70 | 3.27 | 5287 |
| 26 | 208 | Hya | $3(90)$ | 25 | 12 | S | 23 | 15 | 3 | 3.00 | 3.00 | 3 | 3.00 | 3.90 | 3314 |
| 27 | 209 | Hya | 4(120) | 23 | 42 | S | 16 | 0 | 4 | 4.00 | 4.00 | 3 | 3.00 | 5.24 | 4042 |
| 1 | 210 | Car | 5(150) | 9 | 2 | S | 23 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.08 | 4287 |
| 2 | 211 | Car | 5(150) | 15 | 12 | S | 19 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.08 | 4405 |
| 3 | 212 | Car | 5(150) | 12 | 42 | S | 18 | 0 | 4 | 4.00 | 4.00 | 4 | 4.00 | 3.56 | 4382 |
| 4 | 213 | Car | 5(150) | 19 | 42 | S | 18 | 30 | 5(s) | 5.25 | 5.30 | 4(k) | 3.70 | 4.73 | 4514 |
| 5 | 214 | Car | 5(150) | 52 | 2 | S | 13 | 40 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.83 | 4402 |
| 6 | 215 | Car | 5(150) | 21 | 52 | S | 16 | 10 | 4(s) | 4.25 | 4.30 | 4(s) | 4.30 | 5.18 | 4567 |


| 7 | 216 | Car | 5(150) | 14 | 22 | S | 11 | 50 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.70 | 4468 |
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| 1 | 217 | Crv | 5(150) | 28 | 2 | S | 21 | 40 | 3(s) | 3.25 | 3.30 | 3 | 3.00 | 4.02 | 4623 |
| 2 | 218 | Crv | 5(150) | 27 | 2 | S | 19 | 40 | 3 | 3.00 | 3.00 | 3 | 3.00 | 3.00 | 4630 |
| 3 | 219 | Crv | 5(150) | 29 | 22 | S | 18 | 10 | 5 | 5.00 | 5.00 | 5 | 5.00 | 5.21 | 4696 |
| 4 | 220 | Crv | 5(150) | 26 | 12 | S | 14 | 50 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.59 | 4662 |
| 5 | 221 | Crv | 5(150) | 29 | 22 | S | 12 | 30 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.95 | 4757 |
| 6 | 222 | Crv | 5(150) | 29 | 42 | S | 11 | 45 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.31 | 4775 |
| 7 | 223 | Crv | 6(180) | 3 | 12 | S | 18 | 10 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.65 | 4786 |
| 1 | 224 | Cen | 6(180) | 23 | 12 | S | 21 | 40 | 5 | 5.00 | 5.00 | 5(m) | 4.70 | 4.19 | 5192 |
| 2 | 225 | Cen | 6(180) | 22 | 42 | S | 18 | 50 | 5 | 5.00 | 5.00 | 5(m) | 4.70 | 4.73 | 5221 |
| 3 | 226 | Cen | 6(180) | 21 | 52 | S | 20 | 30 | 4 | 4.00 | 4.00 | 4(k) | 3.70 | 4.23 | 5168 |
| 4 | 227 | Cen | 6(180) | 22 | 42 | S | 20 | 0 | 5 | 5.00 | 5.00 | 5(m) | 4.70 | 4.56 | 5210 |
| 5 | 228 | Cen | 6(180) | 18 | 52 | S | 25 | 40 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.75 | 5028 |
| 6 | 229 | Cen | 6(180) | 28 | 22 | S | 22 | 30 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.06 | 5288 |
| 7 | 230 | Cen | 6(180) | 21 | 52 | S | 27 | 30 | 5 | 5.00 | 5.00 | 4 | 4.00 | 3.88 | 5089 |
| 8 | 231 | Cen | 7(210) | 0 | 52 | S | 22 | 20 | 4(s) | 4.25 | 4.30 | 4 | 4.00 | 4.25 | 5367 |
| 9 | 232 | Cen | 7(210) | 1 | 52 | S | 23 | 45 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.42 | 5378 |
| 10 | 233 | Cen | 7(210) | 4 | 42 | S | 18 | 15 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.05 | 5485 |
| 11 | 234 | Cen | 7(210) | 5 | 12 | S | 20 | 50 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.00 | 5471 |
| 12 | 235 | Cen | 6(180) | 26 | 2 | S | 28 | 20 | 4(m) | 3.50 | 3.70 | 4(m) | 3.70 | 3.41 | 5190 |
| 13 | 236 | Cen | 6(180) | 26 | 42 | S | 29 | 20 | 4(m) | 3.50 | 3.70 | 4(m) | 3.70 | 3.04 | 5193 |
| 14 | 237 | Cen | 6(180) | 27 | 52 | S | 28 | 0 | 4 | 4.00 | 4.00 | 4(m) | 3.70 | 3.83 | 5248 |
| 15 | 238 | Cen | 6(180) | 29 | 2 | S | 26 | 30 | 4(m) | 3.50 | 3.70 | 4(m) | 3.70 | 4.36 | 5285 |
| 16 | 239 | Cen | 7(210) | 5 | 32 | S | 25 | 15 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.31 | 5440 |
| 17 | 240 | Cen | 7(210) | 10 | 12 | S | 24 | 0 | 4(m) | 3.50 | 3.70 | 4 | 4.00 | 3.13 | 5576 |
| 18 | 241 | Cen | 7(210) | 0 | 42 | S | 33 | 30 | 3 | 3.00 | 3.00 | 2(m) | 2.70 | 2.55 | 5231 |
| 19 | 242 | Cen | 7(210) | 0 | 22 | S | 31 | 0 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.34 | 5260 |
| 20 | 243 | Cen | 6(180) | 29 | 32 | S | 30 | 20 | 5 | 5.00 | 5.00 | 5 | 5.00 | 3.87 | 5249 |
| 21 | 244 | Cen | 6(180) | 24 | 52 | S | 34 | 50 | 5 | 5.00 | 5.00 | 5 | 5.00 | 3.00 | 0 |
| 22 | 245 | Cen | 6(180) | 21 | 42 | S | 37 | 40 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.71 | 4940 |
| 23 | 246 | Cen | 6(180) | 18 | 52 | S | 40 | 0 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.17 | 4819 |
| 24 | 247 | Cen | 6(180) | 17 | 42 | S | 40 | 20 | 5 | 5.00 | 5.00 | 4 | 4.00 | 3.86 | 4802 |
| 25 | 248 | Cen | 6(180) | 15 | 22 | S | 41 | 0 | 5(m) | 4.50 | 4.70 | 5 | 5.00 | 3.91 | 4743 |


| 26 | 249 | Cen | $6(180)$ | 15 | 22 | S | 46 | 10 | 3 | 3.00 | 3.00 | 3 | 3.00 | 2.60 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 4621 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 27 | 250 | Cen | $6(180)$ | 16 | 12 | S | 46 | 45 | 5 | 5.00 | 5.00 | 4 | 4.00 | 3.96 |
| 28 | 251 | Cen | $7(210)$ | 1 | 2 | S | 40 | 45 | $5(\mathrm{~s})$ | 5.25 | 5.30 | 4 | 4.00 | 4.65 |


| 3 | 289 | CrA | 8(240) | 25 | 52 | S | 20 | 20 | 6 | 6.00 | 6.00 | 5 | 5.00 | 5.36 | 7122 |
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| 4 | 290 | CrA | 8(240) | 27 | 32 | S | 20 | 0 | 5 | 5.00 | 5.00 | 4 | 4.00 | 4.75 | 7188 |
| 5 | 291 | CrA | 8(240) | 28 | 52 | S | 18 | 30 | 5(s) | 5.25 | 5.30 | 5 | 5.00 | 4.59 | 7242 |
| 6 | 292 | CrA | 8(240) | 29 | 42 | S | 17 | 10 | 5 | 5.00 | 5.00 | 4 | 4.00 | 4.11 | 7259 |
| 7 | 293 | CrA | 8(240) | 29 | 32 | S | 16 | 0 | 5 | 5.00 | 5.00 | 4 | 4.00 | 4.11 | 7254 |
| 8 | 294 | CrA | 8(240) | 29 | 12 | S | 15 | 10 | 5 | 5.00 | 5.00 | 4 | 4.00 | 4.94 | 7226 |
| 9 | 295 | CrA | 8(240) | 27 | 52 | S | 15 | 20 | 6 | 6.00 | 6.00 | 6 | 6.00 | 4.86 | 7152 |
| 10 | 296 | CrA | 8(240) | 27 | 22 | S | 14 | 50 | 6 | 6.00 | 6.00 | 6 | 6.00 | 5.38 | 7129 |
| 11 | 297 | CrA | 8(240) | 24 | 32 | S | 14 | 40 | 5(s) | 5.25 | 5.30 | 5 | 5.00 | 5.13 | 7021 |
| 12 | 298 | CrA | 8(240) | 22 | 22 | S | 15 | 50 | 5(s) | 5.25 | 5.30 | 5 | 5.00 | 5.16 | 6942 |
| 13 | 299 | CrA | 8(240) | 21 | 52 | S | 18 | 30 | 5 | 5.00 | 5.00 | 5 | 5.00 | 4.64 | 6951 |
| 1 | 300 | PsA | 10(300) | 18 | 22 | S | 20 | 20 | 4 | 4.00 | 4.00 | 1 | 1.00 | 1.16 | 8728 |
| 2 | 300 | PsA | 10(300) | 18 | 22 | S | 20 | 20 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.29 | 8576 |
| 3 | 301 | PsA | 10(300) | 16 | 52 | S | 22 | 15 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.21 | 8720 |
| 4 | 302 | PsA | 10(300) | 18 | 12 | S | 22 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 4.46 | 8695 |
| 5 | 303 | PsA | 10(300) | 17 | 2 | S | 16 | 15 | 5 | 5.00 | 5.00 | 4 | 4.00 | 4.17 | 8628 |
| 6 | 304 | PsA | 10(300) | 7 | 52 | S | 19 | 30 | 6(s) | 6.25 | 6.25 | 5 | 5.00 | 4.50 | 8431 |
| 7 | 305 | PsA | 10(300) | 13 | 52 | S | 15 | 10 | 5 | 5.00 | 5.00 | 4 | 4.00 | 6.43 | 8570 |
| 8 | 306 | PsA | 10(300) | 11 | 32 | S | 14 | 40 | 5 | 5.00 | 5.00 | 4 | 4.00 | 5.43 | 8478 |
| 9 | 307 | PsA | 10(300) | 7 | 52 | S | 15 | 5 | 5(k) | 4.75 | 4.70 | 4 | 4.00 | 5.42 | 8386 |
| 10 | 308 | PsA | 10(300) | 4 | 32 | S | 16 | 30 | 4 | 4.00 | 4.00 | 4 | 4.00 | 5.01 | 8326 |
| 11 | 309 | PsA | 10(300) | 3 | 42 | S | 18 | 10 | 3(s) | 3.25 | 3.30 | 4 | 4.00 | 4.34 | 8305 |
| 12 | 310 | PsA | 10(300) | 8 | 42 | S | 22 | 15 | 3(s) | 3.25 | 3.30 | 4 | 4.00 | 3.01 | 8353 |
| 13 |  | PsA |  |  |  |  |  |  |  |  |  | 3(s) | 3.30 | 5.53 | 8069 |
| 14 |  | PsA |  |  |  |  |  |  |  |  |  | 3(s) | 3.30 | 4.82 | 8151 |
| 15 |  | PsA |  |  |  |  |  |  |  |  |  | 3(s) | 3.30 | 5.29 | 8229 |
| 16 |  | PsA |  |  |  |  |  |  |  |  |  | 5 | 5.00 | 5.77 | 8180 |
| 17 |  | PsA |  |  |  |  |  |  |  |  |  | 4 | 4.00 | 4.90 | 7965 |
| 18 |  | PsA |  |  |  |  |  |  |  |  |  | 4 | 4.00 | 4.67 | 8039 |

### 8.2 Excerpts of translation of Poem by al-Ṣūfī's Son

This is a Poem on the fixed stars. It is called "al-Urjūza li Ibn al-Ṣūfī" which means "The Poem by Ibn al-Ṣūfi". It is composed of 495 verses which are divided into 48 stanzas, one for each constellation. Every stanza describes the constellation in a simple and easy to understand language. The style is not exactly a literally poetic style; therefore it is called Urjūza, which means "Prose" rather then a poem. The writer was trying to compose an easy to memorize poem and not a scientific piece of work; therefore it does not include much detailed scientific information in many of the constellations.

Al-Qifṭī attributed this poem to al-Ṣūfī; however this poem was written by the son of al-Ṣūfĭ and not by al-Ṣūfĩ himself. The first 6 verses from this poem clearly identify the person who wrote this poem and to whom it was attributed. The second verse explains that this poem was written by $A b \bar{u}$ 'Alī the son of $A b u \bar{u}$ al-Ḥusaīn al-Ṣūfî. The fourth verse states that this poem was dedicated to Shāhenshāh Abū al-Ma‘ali Fakher al-Dīn, who was the second son of Rukn al-Dawla. Fakher al-Dawla took power in Rayy in A.D. 976 after his father's death. He took the title of Shāhenshāh in A.D. 984 until his death in A.D. 997; therefore this poem must have been composed some time between A.D. 984 and A.D. 997 and most probably after al-Ṣūfî's death in A.D. 986. However another reference (Kunitzsch, Encyclopedia Iranica) identifies Shāhenshāh Abū al-Ma'ali Fakher Din Allah as the Artuqid ruler in A.D. 1143; thus Kunitzsch rejects the claim that this poem was ever written during the time of al-Ṣūfī or by his son. However the final verses of this poem state that the information on the stars was taken from the book of al-Ṣūfi. Therefore it would be a strange coincidence that this Ibn al-Ṣūfī also has a father who was called Abū al-Ḥusaīn al-Ṣūfī who wrote a book on the stars from which the son composes a poem in this subject. A copy of this poem is to be found at the end of the below-mentioned manuscripts of al-Ṣūfís Book of the fixed stars". This is why there was sometimes a little confusion as to who wrote the poem. This also explains another confusion, which is the name of al-Ṣūfì because he was referred to as Ibn al-Ṣūfì in many historical reference works.

- Vatican Library, Manuscript: MS Rossi 1033, Copy dated A.H. 621/A.D. 1224
- Paris Bibliotheque Nationale, Manuscript: Arab 979, Copy date unknown
- Munich library, Manuscript: Arab 870, Copy date unknown

I have translated below a few lines from al-Urjūza (Poem) by al-Ṣūfí's son. The first couplet forms the introductory to this poem. The second couplet is for the constellation Ursa

Minor. The last is the final excerpt from the last constellation Piscis Austrinus and the conclusion of this poem.

In the name of God the just the one This is a treatise written by $\mathrm{Ab} \overline{\mathrm{u}}$ ' $\mathrm{Al} \overline{1}$ Describing the stars and their orbits The king of the nation, Shāhenshāh God made him the king of his time Those who ask me about the stars I took it from one who knows Behold the depiction of the great sphere

Know that the closest to the pole They are seven if you count them There are two stars in this constellation The Arabs call them al-Farqadain A small dim star not drawn Yes and a star used to find the Qiblah Called al-Juday by the Arabs It is close to the pole Called also Banāt Na'esh

They are followed by stars in the south They are called al-Hūt by the Romans None of the Arabs mentioned them These are the stars which They are known Some by scholars of al-Shām There are other stars in the sky The Arabs call them al-Suhūla Our father mentioned them in his book Finally may God always pray Muhammad the selected one Then on his disciples and family
and God's Mercy on Muḥammad the son of Abū al-Ḥusaīn al-Ṣūfī written for the king of kings Abū al-Ma'ali Fakher al-Dīn and did not take away his domain and what they hold of wonders adding my literary knowledge to it and all it holds of the stars
are stars in the image of a bear drawn with the pole on the same spot the distance between them is 2 Shibr under the brighter of the two the Arabs of the desert call it Fa's al-Raha $\bar{a}$ it is above the tail of the bear from those close and far other stars known by the Arabs together with al-Fared the old star
some with light and others dim and those which are called astronomers nor were they mentioned by other names you find in the history books by the scholars from al-Küfa also by other well informed persons nobody has heard of their names they are known by unpleasant names so every one should be aware of them for the Prophet of his righteous religion and the chosen at the Day of Judgment as long as the days and nights exist

### 8.3 Arabic Transliteration:

The Arabic language has a number of phonemes that have no equivalent in English. Therefore several different transliteration standards have been used to represent certain Arabic characters such as the ISO, DIN and the British BS standard. However I have tried to follow the Library of Congress transliteration rules in this thesis.

## Dates:

Unless mentioned, all dates in the thesis use Anno Domini system (i.e. A.D. and B.C.). When Hijri dates (Islamic calendar) are noted, they will be indicated by the suffix A.H. (i.e. A.H. 657). When double dates are mentioned A.D. dates are preceded by Hijri Dates and separated by a slash (i.e. $657 / 1261$ is A.H. /A.D.).

